

## R S Aggarwal Solutions for Class 11 Maths Chapter 30 Statistics

Exercise 30A

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**Find the mean deviation about the mean for the following data: (Question 1 to Question 3)****Formula used:**

Mean Deviation about the mean

$$\text{M.D. } (\bar{x}) = \frac{\sum_{i=1}^n |x_i - \bar{x}|}{n}$$

Where  $\bar{x}$  = mean**Question 1: Find the mean deviation about the mean for 7, 8, 4, 13, 9, 5, 16, 18****Solution:**

Step 1: Find the mean

$$\bar{x} = \frac{7 + 8 + 4 + 13 + 9 + 5 + 16 + 18}{8} = \frac{80}{8} = 10$$

Step 2: Mean deviation using formula

$$\begin{aligned} \text{M.D. } (\bar{x}) &= \frac{\sum_{i=1}^8 |x_i - \bar{x}|}{8} \\ &= \frac{3 + 2 + 6 + 3 + 1 + 5 + 6 + 8}{8} = \frac{34}{8} = 4.25 \end{aligned}$$

**Question 2: Find the mean deviation about the mean for 39, 72, 48, 41, 43, 55, 60, 45, 54, 43.****Solution:**

Step 1: Find the mean

$$\bar{x} = \frac{39 + 72 + 48 + 41 + 43 + 55 + 60 + 45 + 54 + 43}{10} = \frac{500}{10} = 50$$

Step 2: Mean deviation using formula

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$$\text{M.D. } (\bar{x}) = \frac{\sum_{i=1}^{10} |x_i - \bar{x}|}{10}$$

$$= \frac{11 + 22 + 2 + 9 + 7 + 5 + 10 + 5 + 4 + 7}{10} = \frac{82}{10} = 8.2$$

**Question 3:** Find the mean deviation about the mean for 17, 20, 12, 13, 15, 16, 12, 18, 15, 19, 12, 11.

**Solution:**

Step 1: Find the mean

$$\bar{x} = \frac{17 + 20 + 12 + 13 + 15 + 16 + 12 + 18 + 15 + 19 + 12 + 11}{12}$$

Step 2: Mean deviation using formula

$$\text{M.D. } (\bar{x}) = \frac{\sum_{i=1}^{12} |x_i - \bar{x}|}{12}$$

$$= \frac{2 + 5 + 3 + 2 + 0 + 1 + 3 + 3 + 0 + 4 + 3 + 4}{12} = \frac{30}{12} = 2.5$$

**Find the mean deviation about the median for the following data: (Question 4 to Question 7)**

**Formula used:**

Mean Deviation about the median

$$\text{M.D.}(M) = \frac{\sum_{i=1}^n |x_i - M|}{n}$$

Where M = median

**Question 4:** Find the mean deviation about the median for 12, 5, 14, 6, 11, 13, 17, 8, 10.

**Solution:**

Step 1: Find the median

Arranging the data into ascending order:

5, 6, 8, 10, 11, 12, 13, 14, 17

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Total number of observations = 9, which is odd.

$$\text{Median}(M) = \left(\frac{9+1}{2}\right)^{\text{th}}$$

or 5<sup>th</sup> observation = 11

Step 2: Mean deviation using formula

$$\text{M.D.}(M) = \frac{\sum_{i=1}^9 |x_i - M|}{9}$$

$$= \frac{6 + 5 + 3 + 1 + 0 + 1 + 2 + 3 + 6}{9} = \frac{27}{9} = 3$$

**Question 5: Find the mean deviation about the median for 4, 15, 9, 7, 19, 13, 6, 21, 8, 25, 11.**

**Solution:**

Step 1: Find the median

Arranging the data into ascending order:

4, 6, 7, 8, 9, 11, 13, 15, 19, 21, 25

Total number of observations = 11, which is odd.

$$\text{Median}(M) = \left(\frac{11+1}{2}\right)^{\text{th}}$$

or 6<sup>th</sup> observation = 11

Step 2: Mean deviation using formula

$$\text{M.D.}(M) = \frac{\sum_{i=1}^{11} |x_i - M|}{11}$$

$$= \frac{7 + 5 + 4 + 3 + 2 + 0 + 2 + 4 + 8 + 10 + 14}{11} = \frac{59}{11} = 5.3$$

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**Question 6: Find the mean deviation about the median for 34, 23, 46, 37, 40, 28, 32, 50, 35, 44.**

**Solution:**

Step 1: Find the median

Arranging the data into ascending order:

23, 28, 32, 34, 35, 37, 40, 44, 46, 50

Total number of observations = 10, which is Even.

$$\text{Median}(M) = \left( \frac{5^{\text{th}} \text{ observation} + 6^{\text{th}} \text{ observation}}{2} \right) = \frac{35 + 37}{2} = 36$$

Step 2: Mean deviation using formula

$$\begin{aligned} \text{M.D.}(M) &= \frac{\sum_{i=1}^{10} |x_i - M|}{10} \\ &= \frac{13 + 8 + 4 + 2 + 1 + 1 + 4 + 8 + 10 + 14}{10} = \frac{65}{10} = 6.5 \end{aligned}$$

**Question 7: Find the mean deviation about the median for 70, 34, 42, 78, 65, 45, 54, 48, 67, 50, 56, 63.**

**Solution:**

Step 1: Find the median

Arranging the data into ascending order:

34, 42, 45, 48, 50, 54, 56, 63, 65, 67, 70, 78

Total number of observations = 12, which is Even.

$$\text{Median}(M) = \left( \frac{6^{\text{th}} \text{ observation} + 7^{\text{th}} \text{ observation}}{2} \right) = \frac{54 + 56}{2} = 55$$

Step 2: Mean deviation using formula

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$$\text{M.D.}(M) = \frac{\sum_{i=1}^{12} |x_i - M|}{12}$$

$$= \frac{21 + 13 + 10 + 7 + 5 + 1 + 1 + 8 + 10 + 12 + 15 + 23}{12} = \frac{126}{12} = 10.5$$

Find the mean deviation about the mean for the following data: (Question 8 to Question 10)

Question 8: Find the mean deviation about the mean for below data:

$x_i$	6	12	18	24	30	36
$f_i$	5	4	11	6	4	6

Solution:

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$$\text{Mean} = \bar{X} = \frac{\sum_{i=1}^6 f_i x_i}{\sum_{i=1}^6 f_i} = \frac{756}{36} = 21$$

$x_i$	$f_i$	$f_i x_i$	$ x_i - \bar{X} $	$f_i  x_i - \bar{X} $
6	5	30	15	75
12	4	48	9	36
18	11	198	3	33
24	6	144	3	18
30	4	120	9	36
36	6	216	15	90
	36	756		288

Mean Deviation about the mean

$$\bar{X} = \frac{\sum_{i=1}^6 f_i |x_i - \bar{X}|}{\sum_{i=1}^6 f_i} = \frac{288}{36} = 8$$

**Question 9:** Find the mean deviation about the mean for below data:

$x_i$	2	5	6	8	10	12
$f_i$	2	8	10	7	8	5

**Solution:**

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$$\text{Mean} = \bar{x} = \frac{\sum_{i=1}^6 f_i x_i}{\sum_{i=1}^6 f_i} = \frac{300}{40} = 7.5$$

$x_i$	$f_i$	$f_i x_i$	$ x_i - \bar{x} $	$f_i  x_i - \bar{x} $
2	2	4	5.5	11
5	8	40	2.5	20
6	10	60	1.5	15
8	7	56	0.5	3.5
10	8	80	2.5	20
12	5	60	4.5	22.5
	40	300		92

Mean Deviation about the mean

$$\bar{x} = \frac{\sum_{i=1}^6 f_i |x_i - \bar{x}|}{\sum_{i=1}^6 f_i} = \frac{92}{40} = 2.3$$

**Question 10: Find the mean deviation about the mean for below data:**

$x_i$	3	5	7	9	11	13
$f_i$	6	8	15	25	8	4

**Solution:**

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$$\text{Mean} = \bar{x} = \frac{\sum_{i=1}^6 f_i x_i}{\sum_{i=1}^6 f_i} = \frac{528}{66} = 8$$

$x_i$	$f_i$	$f_i x_i$	$ x_i - \bar{x} $	$f_i  x_i - \bar{x} $
3	6	18	5	30
5	8	40	3	24
7	15	105	1	15
9	25	225	1	25
11	8	88	3	24
13	4	52	5	20
	66	528		138

Mean Deviation about the mean

$$\bar{x} = \frac{\sum_{i=1}^6 f_i |x_i - \bar{x}|}{\sum_{i=1}^6 f_i} = \frac{138}{66} = 2.09$$

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Exercise 30B

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**Question 1:** Find the mean, variance and standard deviation for the numbers 4, 6, 10, 12, 7, 8, 13, 12.**Solution:**

Given data: 4, 6, 10, 12, 7, 8, 13, 12

Sum of observations =  $4 + 6 + 10 + 12 + 7 + 8 + 13 + 12 = 72$ 

Total number of observation = 8

**Find Mean:**

Mean = (Sum of observations) / (Total number of observation)

$$= 72/8 = 9$$

Mean = 9

**Find Variance:**

$x_i$	$x_i - \bar{x}$	$(x_i - \bar{x})^2$
4	$4 - 9 = -5$	25
6	$6 - 9 = -3$	9
10	$10 - 9 = 1$	1
12	$12 - 9 = 3$	9
7	$7 - 9 = -2$	4
8	$8 - 9 = -1$	1
13	$13 - 9 = 4$	16
12	$12 - 9 = 3$	9
		Sum = 74

$$\text{Variance} = \sigma^2 = \frac{\sum (x_i - \bar{x})^2}{n} = \frac{74}{8}$$

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**Find Standard Deviation:**

$$\begin{aligned}\text{Standard Deviation } (\sigma) &= \sqrt{\text{Variance}} \\ &= \sqrt{\frac{74}{8}} \\ &= \sqrt{9.25} \\ &= 3.04\end{aligned}$$

**Question 2: Find the mean, variance and standard deviation for first six odd natural numbers.**

**Solution:**

Given data: First six odd natural numbers = 1, 3, 5, 7, 9, 11

Sum of observations =  $1 + 3 + 5 + 7 + 9 + 11 = 36$

Total number of observation = 6

**Find Mean:**

Mean = (Sum of observations) / (Total number of observation)

$$= 36/6 = 6$$

Mean = 6

**Find Variance:**

$x_i$	$x_i - \bar{x}$	$(x_i - \bar{x})^2$
1	$1 - 6 = -5$	25
3	$3 - 6 = -3$	9
5	$5 - 6 = -1$	1
7	$7 - 6 = 1$	1
9	$9 - 6 = 3$	9
11	$11 - 6 = 5$	25
		Sum = 70

$$\text{Variance} = \sigma^2 = \frac{\sum (x_i - \bar{x})^2}{n} = \frac{70}{6} = 11.67$$

**Find Standard Deviation:**

$$\begin{aligned} \text{Standard Deviation } (\sigma) &= \sqrt{\text{Variance}} \\ &= \sqrt{11.67} \\ &= 3.41 \end{aligned}$$

**Question 3: Using short cut method, find the mean, variance and standard deviation for the data :**

$x_i$	4	8	11	17	20	24	32
$f_i$	3	5	9	5	4	3	1

**Solution:**

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$x_i$	$f_i$	$x_i f_i$	$x_i - \bar{x}$ ( $\bar{x} = 14$ )	$(x_i - \bar{x})^2$	$f_i(x_i - \bar{x})^2$
4	3	12	-10	100	300
8	5	40	-6	36	180
11	9	99	-3	9	81
17	5	85	3	9	45
20	4	80	6	36	144
24	3	72	10	100	300
32	1	32	18	324	324
	$\Sigma f_i = 30$	$\Sigma f_i x_i = 420$			$\Sigma f_i(x_i - \bar{x})^2 = 1374$

**Mean:**

$$\begin{aligned}\text{Mean } (\bar{x}) &= \frac{\Sigma f_i x_i}{\Sigma f_i} \\ &= \frac{420}{30} \\ &= 14\end{aligned}$$

**Variance:**

$$\begin{aligned}\sigma^2 &= \frac{\Sigma f_i(x_i - \bar{x})^2}{N} \\ &= \frac{1374}{30} \\ &= 45.8\end{aligned}$$

**Standard deviation**

$$\begin{aligned}\sigma &= \sqrt{\text{Variance}} \\ &= \sqrt{45.8} \\ &= 6.77\end{aligned}$$

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Question 4: Using short cut method, find the mean, variance and standard deviation for the data :

$x_i$	6	10	14	18	24	28	30
$f_i$	2	4	7	12	8	4	3

Solution:

$x_i$	$f_i$	$x_i f_i$	$x_i - \bar{x}$ ( $\bar{x} = 19$ )	$(x_i - \bar{x})^2$	$f_i(x_i - \bar{x})^2$
6	2	12	-13	169	338
10	4	40	-9	81	324
14	7	98	-5	25	175
18	12	216	-1	1	12
24	8	192	5	25	200
28	4	112	9	81	324
30	3	90	11	121	363
	$\sum f_i = 40$	$\sum f_i x_i = 760$			$\sum f_i(x_i - \bar{x})^2 = 1736$

Mean:

$$\begin{aligned}\text{Mean } (\bar{x}) &= \frac{\sum f_i x_i}{\sum f_i} \\ &= \frac{760}{40} \\ &= 19\end{aligned}$$

Variance:

$$\begin{aligned}\sigma^2 &= \frac{\sum f_i(x_i - \bar{x})^2}{N} \\ &= \frac{1736}{40} \\ &= 43.4\end{aligned}$$

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Standard deviation:

$$\begin{aligned}\sigma &= \sqrt{\text{Variance}} \\ &= \sqrt{43.4} \\ &= 6.59\end{aligned}$$

Question 5: Using short cut method, find the mean, variance and standard deviation for the data :

$x_i$	10	15	18	20	25
$f_i$	3	2	5	8	2

Solution:

$x_i$	$f_i$	$x_i f_i$	$x_i - \bar{x}$ ( $\bar{x}=19.5$ )	$(x_i - \bar{x})^2$	$f_i(x_i - \bar{x})^2$
10	3	30	-9.5	90.25	270.75
15	2	30	-4.5	20.25	40.5
18	5	90	-1.5	2.25	11.25
20	8	160	0.5	0.25	2
25	2	50	5.5	30.25	60.5
	$\sum f_i = 20$	$\sum f_i x_i = 390$			$\sum f_i(x_i - \bar{x})^2 = 385$

Mean:

$$\begin{aligned}\text{Mean } (\bar{x}) &= \frac{\sum f_i x_i}{\sum f_i} \\ &= \frac{390}{20} \\ &= 19.5\end{aligned}$$

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Variance:

$$\begin{aligned}\sigma^2 &= \frac{\sum f_i(x_i - \bar{x})^2}{N} \\ &= \frac{385}{20} \\ &= 19.25\end{aligned}$$

Standard deviation:

$$\begin{aligned}\sigma &= \sqrt{\text{Variance}} \\ &= \sqrt{19.25} \\ &= 4.39\end{aligned}$$

Question 6: Using short cut method, find the mean, variance and standard deviation for the data :

$x_i$	92	93	97	98	102	104	109
$f_i$	3	2	3	2	6	3	3

Solution:

$x_i$	$f_i$	$x_i f_i$	$x_i - \bar{x}$ ( $\bar{x}=100$ )	$(x_i - \bar{x})^2$	$f_i(x_i - \bar{x})^2$
92	3	276	-8	64	192
93	2	186	-7	49	98
97	3	291	-3	9	27
98	2	196	-2	4	8
102	6	612	2	4	24
104	3	312	4	16	48
109	3	327	9	81	243
	$\sum f_i = 22$	$\sum f_i x_i = 2200$			$\sum f_i(x_i - \bar{x})^2 = 640$

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**Mean:**

$$\begin{aligned}\text{Mean } (\bar{x}) &= \frac{\sum f_i x_i}{\sum f_i} \\ &= \frac{2200}{22} \\ &= 100\end{aligned}$$

**Variance:**

$$\begin{aligned}\sigma^2 &= \frac{\sum f_i (x_i - \bar{x})^2}{N} \\ &= \frac{640}{22} \\ &= 29.09\end{aligned}$$

**Standard deviation:**

$$\begin{aligned}\sigma &= \sqrt{\text{Variance}} \\ &= \sqrt{29.09} \\ &= 5.39\end{aligned}$$

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## Exercise 30C

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**Question 1:** If the standard deviation of the numbers 2, 3, 2x, 11 is 3.5, calculate the possible values of x.

**Solution:**

Standard Deviation ( $\sigma$ ) = 3.5

Sum of observations:  $2 + 3 + 2x + 11 = 16 + 2x$

Total number of observations = 4

Mean =  $(16+2x)/4 = (8+x)/2$

$x_i$	$x_i - \bar{x}$	$(x_i - \bar{x})^2$
2	$2 - \frac{8+x}{2} = \frac{-4-x}{2}$	$\frac{16 + 8x + x^2}{4}$
3	$3 - \frac{8+x}{2} = \frac{-2-x}{2}$	$\frac{4 + 4x + x^2}{4}$
2x	$2x - \frac{8+x}{2} = \frac{3x-8}{2}$	$\frac{64 - 48x + 9x^2}{4}$
11	$11 - \frac{8+x}{2} = \frac{14-x}{2}$	$\frac{196 - 28x + x^2}{4}$

$$\text{Variance, } \sigma^2 = \frac{1}{n} \sum (x_i - \bar{x})^2$$

$$(3.5)^2 = \frac{1}{4} \left[ \frac{16 + 8x + x^2}{4} + \frac{4 + 4x + x^2}{4} + \frac{64 - 48x + 9x^2}{4} + \frac{9 - 6x + x^2}{4} \right]$$

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$$12.25 \times 16 = 280 - 64x + 12x^2$$

$$196 = 280 - 64x + 12x^2$$

$$12x^2 - 64x + 84 = 0$$

$$\text{or } 3x^2 - 16x + 21 = 0$$

$$\text{or } (3x - 7)(x - 3) = 0$$

$$\Rightarrow \text{Either } 3x - 7 = 0 \text{ or } x - 3 = 0$$

$$\Rightarrow x = 7/3 \text{ or } x = 3$$

Therefore, possible values of  $x$  are 3 and  $7/3$ .

**Question 2:** The variance of 15 observations is 6. If each observation is increased by 8, find the variance of the resulting observations.

**Solution:** Let  $x_1, x_2, x_3, x_4, \dots, x_{15}$  are any random 15 observations.

Variance = 6 and  $n = 15$  (Given)

We know that,

$$\text{Variance, } \sigma^2 = \frac{1}{n} \sum (x_i - \bar{x})^2$$

$$6 = \frac{1}{15} \sum (x_i - \bar{x})^2$$

$$90 = \sum (x_i - \bar{x})^2 \dots (1)$$

If each observation is increased by 8, then let new observations be  $y_1, y_2, y_3, y_4, \dots, y_{15}$ ;  
where  $y_i = x_i + 8 \dots (2)$

Now, find the variance for new observations:

$$\text{New Variance} = \frac{1}{n} \sum (y_i - \bar{y})^2$$

Mean of new observations,

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$$\bar{y} = \frac{\sum_{i=1}^n y_i}{n}$$

$$\bar{y} = \frac{\sum_{i=1}^{15} x_i + 8}{15}$$

[Using equation (2)]

$$\bar{y} = \frac{1}{15} \left[ \sum_{i=1}^{15} x_i + 8 \sum_{i=1}^{15} 1 \right]$$

$$\bar{y} = \frac{1}{15} \sum_{i=1}^{15} x_i + 8 \times \frac{15}{15}$$

$$\bar{y} = \bar{x} + 8 \quad \dots\dots(3)$$

Using equation (2) and (3) in equation (1), we get

$$\sum (x_i - \bar{x})^2 = 90$$

$$\sum (y_i - 8 - (\bar{y} - 8))^2 = 90$$

$$\sum (y_i - 8 - \bar{y} + 8)^2 = 90$$

$$\sum (y_i - \bar{y})^2 = 90$$

$$\text{New Variance} = \frac{1}{n} \sum (y_i - \bar{y})^2$$

$$= \frac{1}{15} \times 90$$

$$= 6$$

**Question 3:** The variance of 20 observations is 5. If each observation is multiplied by 2. Find the variance of the resulting observations.

**Solution:**

Given: Variance = 5 and  $n = 20$

Let  $x_1, x_2, x_3, x_4, \dots, x_{20}$  are any random 20 observations.

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$$\text{Variance, } \sigma^2 = \frac{1}{n} \sum (x_i - \bar{x})^2$$

$$5 = \frac{1}{20} \sum (x_i - \bar{x})^2$$

$$100 = \sum (x_i - \bar{x})^2 \dots\dots(1)$$

If each observation is multiplied by 2, then let new observations be  $y_1, y_2, y_3, y_4, \dots, y_{20}$ .

where  $y_i = 2x_i \dots\dots(2)$

Now, find the variance for new observations:

$$\text{New Variance} = \frac{1}{n} \sum (y_i - \bar{y})^2$$

Mean of new observations,

$$\bar{y} = \frac{\sum y_i}{n}$$

$$\bar{y} = \frac{\sum (2x_i)}{20}$$

[Using equation (2)]

$$\bar{y} = 2 \left( \frac{\sum x_i}{20} \right)$$

$$\bar{y} = 2\bar{x} \dots(3)$$

Using equation (2) and (3) in equation (1), we get

$$\sum (x_i - \bar{x})^2 = 100$$

$$\sum \left( \frac{1}{2} y_i - \frac{1}{2} \bar{y} \right)^2 = 100$$

$$\left( \frac{1}{2} \right)^2 \sum (y_i - \bar{y})^2 = 100$$

$$\sum (y_i - \bar{y})^2 = 400$$

$$\text{New Variance} = \frac{1}{n} \sum (y_i - \bar{y})^2$$

$$= \frac{1}{20} \times 400$$

$$= 20$$

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**Question 4:** The mean and variance of five observations are 6 and 4 respectively. If three of these are 5, 7 and 9, find the other two observations.

**Solution:**

Mean of five observations = 6 and

Variance of five observations = 4

Let the other two observations be  $x$  and  $y$ , then new set of observations be 5, 7, 9,  $x$  and  $y$

Total number of observations = 5

Sum of all the observations =  $5 + 7 + 9 + x + y = 21 + x + y$

We know, Mean = (Sum of all the observations) / (Total number of observations)

$$\Rightarrow 6 = (21 + x + y)/5$$

$$\Rightarrow 9 = x + y \dots\dots(1)$$

Also,

$x_i$	$x_i - \bar{x}$	$(x_i - \bar{x})^2$
5	$5 - 6 = -1$	1
7	$7 - 6 = 1$	1
9	$9 - 6 = 3$	9
$x$	$x - 6$	$(x - 6)^2$
$y$	$y - 6$	$(y - 6)^2$

$$\sum (x_i - \bar{x})^2 = 11 + (x - 6)^2 + (y - 6)^2$$

$$\text{Variance, } \sigma^2 = \frac{\sum (x_i - \bar{x})^2}{n}$$

$$4 = \frac{11 + (x - 6)^2 + (y - 6)^2}{5}$$

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$$20 = 11 + (x^2 + 36 - 12x) + (y^2 + 36 - 12y)$$

$$9 = x^2 + y^2 + 72 - 12(x + y)$$

$$x^2 + y^2 + 72 - 12(9) - 9 = 0$$

(using equation (1))

$$x^2 + y^2 + 63 - 108 = 0$$

$$x^2 + y^2 - 45 = 0$$

$$\text{or } x^2 + y^2 = 45 \dots(2)$$

Form (1);  $x + y = 9$

Squaring both sides,  
 $(x + y)^2 = (9)^2$

$$(x^2 + y^2) + 2xy = 81$$

$$45 + 2xy = 81 \text{ (using equation (2))}$$

$$2xy = 81 - 45$$

$$\text{or } xy = 18$$

$$\text{or } x = 18/y$$

$$(1) \Rightarrow 18/y + y = 9$$

$$y^2 - 9y + 18 = 0$$

$$(y - 3)(y - 6) = 0$$

Either  $(y - 3) = 0$  or  $(y - 6) = 0$   
 $\Rightarrow y = 3, 6$

For  $y = 3$

$$x = 18/3 = 6$$

and for  $y = 6$

$$x = 18/6 = 3$$

Thus, remaining two observations are 3 and 6.

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**Question 5:** The mean and variance of five observations are 4.4 and 8.24 respectively. If three of these are 1, 2 and 6, find the other two observations.

**Solution:**

Mean of five observations = 4.4 and

Variance of five observations = 8.24

Let the other two observations be  $x$  and  $y$ , then new set of observations be 1, 2, 6,  $x$  and  $y$ .

Total number of observations = 5

Sum of all the observations =  $1 + 2 + 6 + x + y = 9 + x + y$

We know, Mean = (Sum of all the observations) / (Total number of observations)

$$\Rightarrow 4.4 = (9 + x + y)/5$$

$$\Rightarrow 13 = x + y \dots\dots(1)$$

Also,

$x_i$	$x_i - 4.4$	$(x_i - \bar{x})^2$
1	-3.4	11.56
2	-2.4	5.76
6	1.6	2.56
$x$	$x - 4.4$	$(x - 4.4)^2$
$y$	$y - 4.4$	$(y - 4.4)^2$

$$\sum (x_i - \bar{x})^2 = 19.88 + (x - 4.4)^2 + (y - 4.4)^2$$

$$\text{Variance, } \sigma^2 = \frac{\sum (x_i - \bar{x})^2}{n}$$

$$8.24 = \frac{19.88 + (x - 4.4)^2 + (y - 4.4)^2}{5}$$

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$$41.2 = 19.88 + (x^2 + 19.36 - 8.8x) + (y^2 + 19.36 - 8.8y)$$

$$21.32 = x^2 + y^2 + 38.72 - 8.8(x + y)$$

$$x^2 + y^2 + 38.72 - 8.8(13) - 21.32 = 0$$

(using equation (1))

$$x^2 + y^2 - 97 = 0 \dots(2)$$

Squaring equation (1) both the sides, we get

$$(x + y)^2 = (13)^2$$

$$x^2 + y^2 + 2xy = 169$$

$$97 + 2xy = 169$$

(using equation (2))

$$xy = 36$$

$$\text{or } x = 36/y$$

$$(1) \Rightarrow 36/y + y = 13$$

$$y^2 + 36 = 13y$$

$$y^2 - 13y + 36 = 0$$

$$(y - 4)(y - 9) = 0$$

Either  $(y - 4) = 0$  or  $(y - 9) = 0$

$$\Rightarrow y = 4 \text{ or } y = 9$$

For  $y = 4$

$$x = 36/y = 36/4 = 9$$

For  $y = 9$

$$x = 36/9 = 4$$

Thus, remaining two observations are 4 and 9.

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Exercise 30D

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**Question 1:** The following results show the number of workers and the wages paid to them in two factories  $F_1$  and  $F_2$ .

Factory	A	B
Number of workers	3600	3200
Mean wages	Rs 5300	Rs 5300
Variance of distribution of wage	100	81

Which factory has more variation in wages?

**Solution:**

Mean wages of both the factories = Rs. 5300

Find the coefficient of variation (CV) to compare the variation.

We know,  $CV = SD/Mean \times 100$ , where SD is the standard deviation.

The variance of factory A is 100 and the variance of factory B is 81.

Now, SD of factory A =  $\sqrt{100} = 10$

And, SD of factory B =  $\sqrt{81} = 9$

Therefore,

The CV of factory A =  $10/5300 \times 100 = 0.189$

The CV of factory B =  $9/5300 \times 100 = 0.169$

Here, the CV of factory A is greater than the CV of factory B.

Hence, factory A has more variation in wages.

**Question 2:** Coefficient of variation of the two distributions are 60% and 80% respectively, and their standard deviations are 21 and 16 respectively. Find their arithmetic means.

**Solution:**

Step 1: Coefficient of variation (CV) is 60%, and the standard deviation (SD) is 21.

We know,  $CV = SD/Mean \times 100$ , where SD is the standard deviation.

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or  $\text{Mean} = \text{SD}/\text{CV} \times 100$

$$= 21/60 \times 100$$

$$= 35$$

Step 2: Coefficient of variation (CV) is 80%, and the standard deviation (SD) is 16.

Now,  $\text{Mean} = \text{SD}/\text{CV} \times 100$

$$= 16/80 \times 100$$

$$= 20$$

Therefore, the arithmetic mean of both the distribution are 35 and 20.

**Question 3: The mean and variance of the heights and weights of the students of a class are given below:**

	Heights	Weights
Mean	63.2 inches	63.2 kg
SD	11.5 inches	5.6 kg

**Which shows more variability, heights or weights?**

**Solution:**

Step 1: In case of heights

Mean = 63.2 inches and SD = 11.5 inches.

Coefficient of variation:

We know,  $\text{CV} = \text{SD}/\text{Mean} \times 100$ , where SD is the standard deviation.

$$\text{CV} = 11.5/63.2 \times 100 = 18.196$$

Step 2: In case of weights

Mean = 63.2 inches and SD = 5.6 inches.

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Coefficient of variation:

$$CV = 5.6/63.2 \times 100 = 8.86$$

From both the steps, we found

CV of heights > CV of weights

So, heights show more variability.

**Question 4:** The mean and variance of the heights and weights of the students of a class are given below:

Firm	A	B
Number of workers	560	650
Mean monthly wages	Rs 5460	Rs 5460
Variance of distribution of wage	100	121

(i) Which firm pays a larger amount as monthly wages?

(ii) Which firm shows greater variability in individual wages?

**Solution:**

(i)

Both the factories pay the same mean monthly wages i.e. Rs 5460

Number of workers for factory A = 560

Number of workers for factory B = 650

Factory A totally pays as monthly wage = Rs.(5460 x 560) = Rs. 3057600

Factory B totally pays as monthly wage = Rs.(5460 x 650) = Rs. 3549000

That means, factory B pays a larger amount as monthly wages.

(ii)

Find the coefficient of variation (CV) to compare the variation.

We know,  $CV = SD/Mean \times 100$ , where SD is the standard deviation.

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The variance of factory A is 100 and the variance of factory B is 121.

Now,

SD of factory A =  $\sqrt{100} = 10$

SD of factory B =  $\sqrt{121} = 11$

Therefore,

The CV of factory A =  $10/5460 \times 100 = 0.183$

The CV of factory B =  $11/5460 \times 100 = 0.201$

Here, CV of factory B is greater than the CV of factory A.

Hence, factory B shows greater variability.

**Question 5: The sum and the sum of squares of length  $x$  (in cm) and weight  $y$  (in g) of 50 plant products are given below:**

$$\sum_{i=1}^{50} x_i = 212, \quad \sum_{i=1}^{50} x_i^2 = 902.8, \quad \sum_{i=1}^{50} y_i = 261 \text{ and } \sum_{i=1}^{50} y_i^2 = 1457.6$$

**Which is more variable, the length or weight?**

**Solution:**

Compare the coefficients of variation (CV) to get required result.

Here the number of products are  $n = 50$  for length and weight both.

Step 1: For length

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$$\text{Mean} = \frac{\sum x_i}{n} = \frac{212}{50} = 4.24$$

$$\text{Variance} = \frac{1}{n^2} [n \sum x_i^2 - (\sum x_i)^2]$$

$$= \frac{1}{50^2} [(50 \times 902.8) - (212)^2]$$

$$= \frac{196}{2500}$$

$$= 0.0784$$

$$\text{SD} = \sqrt{\text{Variance}} = \sqrt{0.0784} = 0.28$$

Coefficient of variation of length:

$$\text{CV} = \frac{0.28}{4.24} \times 100 = 6.603$$

Step 2: For weight

$$\text{Mean} = \frac{\sum y_i}{n} = \frac{261}{50} = 5.22$$

$$\text{Variance} = \frac{1}{n^2} [n \sum y_i^2 - (\sum y_i)^2]$$

$$= \frac{1}{50^2} [(50 \times 1457.6) - (261)^2]$$

$$= \frac{4759}{2500}$$

$$= 1.9036$$

$$\text{SD} = \sqrt{\text{Variance}} = \sqrt{1.9036} = 1.37$$

Coefficient of variation of length:

$$\text{CV} = \frac{1.37}{5.22} \times 100 = 26.245$$

From above results, we can say CV of weight) > CV of length

Therefore, the weight is more variable than height.