

EXERCISE 20A

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- 1. Find the volume, lateral surface area and the total surface area of the cuboid whose dimensions are:
 - (i) Length=22cm, breadth=12cm and height=7.5cm
 - (ii) Length=15m, breadth=6m and height=9dm
 - (iii) Length=24m, breadth=25cm and height=6m
 - (iv) Length=48cm, breadth=6dm and height=1m Solutions:
 - (i) Given Length=22cm, breadth=12cm and height=7.5cm We know that volume of cuboid= length \times breadth \times height $V = (22 \times 12 \times 7.5)$ $V = 1980 \text{cm}^3$ We know that total surface area of cuboid= 2(I b + b h + h I) Surface area = 2 (22 \times 12 + 12 \times 7.5 + 7.5 \times 22) Surface area = 2 (264 + 165 + 90) Total Surface area = 1038cm² We know that lateral area of cuboid= 2 [(I + b) \times h] Lateral surface area = 2 [(22 + 12) \times 7.5] Lateral surface area = 510 cm²
 - (ii) Given Length=15m, breadth=6m and height=9m We know that volume of cuboid= length \times breadth \times height $V = (15 \times 6 \times 0.9)$ $V = 81m^3$ We know that total surface area of cuboid= 2(l b + b h + h l) Surface area = $2(15 \times 6 + 6 \times .9 + .9 \times 15)$ Surface area = 2(90 + 13.5 + 5.4) Total Surface area = $217.8m^2$ We know that lateral surface area of cuboid= $2[(l + b) \times h]$ Lateral surface area = $2[(15 + 6) \times 0.9]$ Lateral surface area = $37.8 m^2$
 - (iii) Given Length=24m, breadth=25cm and height=6m We know that volume of cuboid= length \times breadth \times height $V = (24 \times 0.25 \times 6)$ $V = 36m^3$ We know that total surface area of cuboid= 2(l b + b h + h l)



Surface area = $2 (24 \times .25 + .25 \times 6 + 6 \times 24)$ Surface area = 2 (6 + 155 + 1.5)Total Surface area = $303m^2$ We know that lateral area of cuboid= $2 [(l + b) \times h]$ Lateral surface area = $2 [(24 + .25) \times 6]$ Lateral surface area = $291 m^2$

(iv) Given Length=48cm, breadth=6dm and height=1m

We know that volume of cuboid= length × breadth × height

$$V = (0.48 \times 0.6 \times 1)$$

 $V = 0.288 \text{m}^3$

We know that total surface area of cuboid= 2(l b + b h + h l)

Surface area = $2(0.48 \times 0.6 + 0.6 \times 1 + 1 \times 0.48)$

Surface area = 2(.288 + 0.6 + 0.48)

Total Surface area = 2.736m²

We know that lateral surface area of cuboid= $2[(l + b) \times h]$

Lateral surface area = $2[(0.48 + 0.6) \times 1]$

Lateral surface area = 2.16 m²

2. The dimensions of a rectangular water tank are 2m 75cm by 1m 80cm by 1m 40cm.

How many litres of water does it hold when filled to the brim?

Solution:

We know that 1m=100cm

Dimension of the tank is 2m 75cm and 1m 80cm and 1m 40cm

Which can be written as $275 \text{cm} \times 180 \text{ cm} \times 140 \text{ cm}$

Also we know that volume of cuboid = length × breadth × height

$$V = 275 \times 180 \times 140$$

 $V = 6930000 \text{cm}^3$

And we know that 1000cm³= 1L

Therefore V=6930 liters of water it holds when filled to the brim.

3. A solid rectangular piece of iron measures 1.05m × 70cm × 1.5cm. Find the weight of this piece in kilograms if 1cm³ of iron weighs 8 grams.

Solution:

We know that 1m=100cm

Dimension of the tank is 1.05m and 70cm and 1.5cm.

Also we know that volume of cuboid = length × breadth × height

 $V = 105 \times 70 \times 1.5$

 $V = 11025 cm^3$

And we know that 1cm³= 8 grams



Weight of iron piece = $11025 \times 8 = 88200g$ But 1 kg = 1000gWeight of iron piece = 88.2 kg

4. The area of courtyard is 3750 m². Find the cost of covering it with gravel to a height of 1cm if the gravel costs ₹ 6.40 per cubic meter.

Solution:

We know that 1cm= 0.01m

Given that area of courtyard is 3750 m²

Volume of the gravel = area × height

 $V = 3750 \times 0.01 = 37.5 \text{ m}^3$

Also given that the cost of covering it with gravel to a height of 1cm if the gravel costs ₹ 6.40 per cubic meter.

There the cost is $37.5 \times 6.40 = ₹240$

5. How many persons can be accommodated in a hall of length 16m, breadth 12.5m and height 4.5m, assuming that 3.6 m³ of air is required for each person? Solution:

We know that volume of cuboid = $length \times breadth \times height$

 $V = 16 \times 12.5 \times 4.5 = 900 \text{ m}^3$

Also given that 3.6 m³ of air is required for each person

Therefore, total number of persons can be accommodated in a hall is

Total volume/volume required by each person

- = 900/3.6
- = 250 people.
- 6. A cardboard box is 1.2m long, 72cm wide and 54cm high. How many bars of soap can be put it into it if each bar measures 6cm × 4.5 cm × 4 cm?

 Solution:

We know that volume of cuboid = length × breadth × height

 $V = 120 \times 72 \times 54 = 466560 \text{ cm}^3$

Volume of each bar soap = $6 \times 4.5 \times 4 = 108 \text{ cm}^3$

Therefore, total number of soaps can be accommodated in a box is

Volume of the box/ volume of each soap

- = 466560/108
- = 4320 bars
- 7. The size of matchbox is 4cm × 2.5 cm × 1.5 cm. What is the volume packet containing 144 matchboxes? How many such packets can be place in a carton of size 1.5cm × 84cm × 60 cm?



Solution:

We know that volume of cuboid = $length \times breadth \times height$

Volume occupied by single matchbox = $4 \times 2.5 \times 1.5 = 15$ cm³

Volume of a packet containing 144 matchbox = $15 \times 144 = 2160 \text{ cm}^3$

Volume of carton is $1.5 \text{cm} \times 84 \text{cm} \times 60 \text{ cm} = 756000 \text{ cm}^3$

Therefore, total number of packets can be accommodated in a carton is

Volume of the carton/volume of the box

- = 75600/2160
- = 350 packets
- 8. How many planks of size 2cm × 25cm × 8 cm can be prepared from a wooden block 5m long, 70cm broad and 32 cm thick, assuming that there is no wastage? Solution:

We know that volume of cuboid = length × breadth × height

Volume of the block = $500 \times 70 \times 32 = 112000 \text{ cm}^3$

Volume of each plank = $200 \times 25 \times 8 = 40000 \text{ cm}^3$

Therefore, total number of planks that can be made

- = Volume of the block/ volume of the each plank
- = 112000/40000
- = 38 planks
- 9. How many bricks, each of size 25 cm × 13.5cm × 6 cm, will be required to build a wall 8 m long, 5.4 m high and 33cm thick?

Solution:

We know that volume of cuboid = length × breadth × height

Volume of the brick = $25 \times 13.5 \times 6 = 2025$ cm³

Volume of the wall = $800 \times 540 \times 33 = 14256000 \text{ cm}^3$

Therefore, total number of bricks required

=Volume of the wall/volume of the each brick

- = 1425000/2025
- = 7040 bricks
- 10. A wall 15m long, 30cm wide and 4m high is made of bricks, each measuring 22 cm × 12.5cm × 7.5 cm. If 1/12 of the total volume of the wall consists of mortar, how many bricks are there in the wall?

Solution:

We know that volume of cuboid = $length \times breadth \times height$

Volume of the wall = $150 \times 30 \times 400 = 18000000 \text{ cm}^3$

The quantity of mortar= $1/12 \times 18000000 = 1500000$

Volume of bricks= $18000000 - 1500000 = 16500000 \text{ cm}^3$



Volume of single brick = $22 \times 12.5 \times 7.5 = 2062.5 \text{ cm}^3$

Therefore, total number of bricks required

- =total volume of the bricks/ volume of the each brick
- = 16500000/2062.5
- = 8000 bricks
- 11. Find the capacity of rectangular cistern in liters whose dimensions are 11.2 m × 6m × 5.8m. Find the area of the iron sheet required to make the cistern.

Solution:

We know that volume of cuboid = length \times breadth \times height

Volume of the cistern = $11.2 \times 6 \times 5.8$

- $= 389.76 \text{ m}^3$
- $= 389.76 \times 1000$
- = 389760 liters.

Area of the sheet that required to make the cistern = total surface area of the cistern we know that total surface area of cuboid= 2(l b + b h + h l)

$$= 2 (11.22 \times 6 + 6 \times 5.8 + 5.8 \times 11.2)$$

- = 2 (67.2 + 64.96 + 34.8)
- $= 333.92 \text{ cm}^2$
- 12. The volume of a block of gold is 0.5 m^{3.} If it is hammered into a sheet to cover an area of 1 hectare, find the thickness of the sheet.

Solution:

Given that volume of the block of gold is 0.5 m³

We know that 1 hectare = 10000 m²

Thickness of the sheet = volume/ area

- = 0.5/1000
- =0.00005m
- =0.005cm
- 13. The rainfall recorded on a certain day was 5cm. Find the volume of water that fell on a 2-hectare field.

Solution:

Given that rainfall recorded in a certain day= 5cm = 0.05m

Area of the field = 2 hectare

We know that 1 hectare = 10000 m²

Area = 2×10000

Area = 20000 m^2

Total rain in the field= area of the field × height of the field

 $=0.05 \times 20000 = 1000 \text{ m}^3$



14. A river 2m deep and 45m wide is flowing at the rate of 3km/h. Find the quantity of water that runs into the sea per minute.

Solution:

Given that rate of flow 3 km/hArea of cross section of river = $45 \times 2 = 90 \text{ m}^2$ Rate of flow $3 \text{km/h} = 3 \times 1000/60 = 50 \text{m/min}$ Volume of water is flowing in cross section in 1 minute is= $90 \times 50 = 4500 \text{ m}^3$ per minute

15. A pit 5m long and 3.5m wide is dug to a certain depth. If the volume of earth taken out of it is 14 m³, what is the depth of the pit?

Solution:

We know that volume of cuboid = length \times breadth \times height Let the depth of the pit is x m. Therefore, V= $5 \times 3.5 \times x$ But volume is 14 m^3

 $x = V/5 \times 3.5$ $x = 14/5 \times 3.5$

0.0 00

x = 0.8 m = 80 cm



EXERCISE 20B

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- 1. Find the volume, curved surface area and total surface area of each of the cylinders whose dimensions are:
 - (i) Radius of the base = 7cm and height = 50cm
 - (ii) Radius of the base = 5.6m and height = 1.25 m
 - (iii) Radius of the base = 14dm and height = 15m Solution:
 - (i) We know that volume of the cylinder = $\pi r^2 h$

Here r = 7cm h = 50cm

 $V = 22/7 \times 7 \times 7 \times 50$

 $V = 22 \times 7 \times 50$

 $V = 7700 \text{ cm}^3$

Also we know that curved surface area of cylinder= $2 \pi r h$

Curved surface area = $2 \times 22/7 \times 7 \times 50$

Curved surface area = 2200 cm²

We know that total surface area of cylinder = $2 \pi r(r + h)$

Total surface area = $2 \times 22/7 \times 7 (7 + 50)$

Total surface area = 2580 cm²

(ii) We know that volume of the cylinder = $\pi r^2 h$

Here r = 5.6m h = 1.25m

 $V = 22/7 \times 5.6 \times 5.6 \times 1.25$

 $V = 123.2 \text{ m}^3$

Also we know that curved surface area of cylinder= $2 \pi r h$

Curved surface area = $2 \times 22/7 \times 5.6 \times 1.25$

Curved surface area = 44 m²

We know that total surface area of cylinder = $2 \pi r(r + h)$

Total surface area = $2 \times 22/7 \times 5.6$ (5.6 + 1.25)

Total surface area = 241.12 m²

(iii) We know that volume of the cylinder = $\pi r^2 h$

Here r = 14dm h = 15cm

 $V = 22/7 \times 1.4 \times 1.4 \times 15$

 $V = 92.4 \text{ cm}^3$

Also we know that curved surface area of cylinder= $2 \pi r h$

Curved surface area = $2 \times 22/7 \times 1.4 \times 15$



Curved surface area = 132 cm^2 We know that total surface area of cylinder = $2 \pi r(r + h)$ Total surface area = $2 \times 22/7 \times 1.4 (1.4 + 15)$ Total surface area = 144.32 cm^2

2. A milk tank is in the form of cylinder whose radius is 1.5m hand height is 10.5 m. find the quantity of milk in liters that can be stored in the tank.

Solution:

Given r= 1.5m and h=10.5 m
To find the quantity of milk stored is equal to volume of the cylinder But we know that volume of the cylinder = $\pi r^2 h$
V = $22/7 \times 1.5 \times 1.5 \times 10.5$
V = 74.25 m³
But 1 m³=1000L
Therefore quantity of milk is 74250 L

3. A wooden cylindrical pole is 7m high and its base radius is 10cm. Find its weight if the wood weighs 225kg per cubic meter.

Solution:

Given r= 7m and h=10 cm But we know that volume of the cylinder = $\pi r^2 h$ V = 22/7 × 0.1 × 0.1 × 7 V = 0.22 cm³ Given weight of the wood 225kg per cubic meter Weight of the pole = 0.22 × 225 = 49.5 kg

4. Find the height of the cylinder whose volume is 1.54m³ and diameter of the base is 140cm?

Solution:

Given that volume of the cylinder = 1.54m^3 Diameter = 140cmTherefore, radius = diameter/2 = 140/2 = 70cm = 0.7mBut we know that Volume of cylinder = $\pi r^2 h$ $1.54 = 22/7 \times 0.7 \times 0.7 \times h$ h = 1m

5. The volume of a circular iron rod of length 1m is 3850 cm³. Find its diameter. Solution:

Given volume of circular iron rod is 3850 cm³ But we know that Volume of cylinder = $\pi r^2 h$



 $3850 = 22/7 \times r \times r \times 100$ $r^2 = 3850 \times 7/100 \times 22$ $r = 1.75 \times 7$ r = 3.5cm Therefore diameter = $2 \times r$ Diameter = $2 \times 3.5 = 7$ cm

6. A closed cylindrical tank of diameter 12m and height 5m is made from a sheet of metal. How much sheet of metal will be required? Solution:

Given that diameter = 12m Therefore r= diameter /2 =12/2 = 6 m Also given that height is 5m Now we have to find the total surface area We know that total surface area of cylinder = $2 \pi r(r + h)$ Total surface area = $2 \times 22/7 \times 6 (6 + 5)$ Total surface area = $528 m^2$

7. The circumference of the base of a cylinder is 88cm and its height is 60cm. Find the volume of the cylinder and its curved surface area.

Solution:

Given that circumference of the base of a cylinder is 88cm Height of cylinder = 60cm Curved surface area = circumference × height = 88×60 = 5280 cm^2 Circumference = $2 \pi r$ $60 = 2 \times 22/7 \times r$ r = 14 cm Therefore volume of the cylinder = $\pi r^2 h$ $V = 22/7 \times 14 \times 14 \times 60$ $V = 36960 \text{ cm}^3$

8. The lateral surface area of a cylinder of length 14m is 220 m². Find the volume of the cylinder.

Solution:

Given that length is 14m and lateral surface area is 220 m² Lateral surface area of cylinder= $2 \pi r h$ 220= $2 \times 22/7 \times r \times 14$ r = 2.5m



Therefore volume of the cylinder = $\pi r^2 h$ V= 22/7 × 14 × 14 × 60 V = 36960 cm³

9. The volume of a cylinder of height 8cm is 1232cm³. Find its curved surface area and total surface area.

Solution:

Given that height of the cylinder is 8cm and volume is 1232cm³.

Therefore volume of the cylinder = $\pi r^2 h$

$$1232 = 22/7 \times r \times r \times 8$$

$$r^2 = 1232 \times 7/8$$

$$r = 7cm$$

Also we know that curved surface area of cylinder= $2 \pi r h$

Curved surface area = $2 \times 22/7 \times 7 \times 8$

Curved surface area = 252 cm²

We know that total surface area of cylinder = $2 \pi r(r + h)$

Total surface area = $2 \times 22/7 \times 7$ (7 + 8)

Total surface area = 2580 cm²

10. The radius and height of a cylinder are in the ratio 7:2. If the volume of the cylinder is 8316cm³, find the surface area of cylinder.

Solution:

Given that radius and height of a cylinder are in the ratio 7:2

Hence radius/height =7/2

$$r = (7/2) h$$

Therefore volume of the cylinder = $\pi r^2 h$

$$8316 = 22/7 \times (7/2) h \times (7/2) h \times h$$

 $h^3 = 216$

h = 6cm

Therefore r = 21cm

We know that total surface area of cylinder = $2 \pi r(r + h)$

Total surface area = $2 \times 22/7 \times 21 (21 + 6)$

Total surface area = 3564 cm²



EXERCISE 20C

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Select the correct answer in each of the following:

- 1. The maximum length of a pencil that can be kept in rectangular box of dimensions 12cm × 9cm × 8cm, is
 - (a) 13cm
- (b) 17cm
- (c) 18cm
- (d) 19cm

Solution:

(b) 17cm

Explanation:

We know that length of diagonal of the cuboid= $\sqrt{(l^2+b^2+h^2)}$

$$=\sqrt{(12^2+9^2+8^2)}$$

$$=\sqrt{(144+81+64)}$$

=17

2. The total surface area of a cube is 150 cm².lts volume is (a)216 cm³ (b) 125 cm³ (c) 64 cm³ (d) 1000 cm³

Solution:

(b) 125 cm³

Explanation:

Total surface area of the cube = $6 a^2$

$$150 = 6 a^2$$

$$a^2 = 150/6 = 25$$

$$a = 5$$

Volume of the cube = a^3

$$V = 5^3 = 125$$

3. The volume of a cube is 343 cm³. Its total surface area s
(a)196 cm² (b) 49 cm² (c) 294 cm² (d) 147 cm²

Solution:

 $(c)294 cm^2$

Explanation:

Volume of the cube = a^3

 $343 = a^3$

a = 7cm

Total surface area of the cube = $6 a^2$



$$= 6 (7)^2$$

= 294

4. The cost of painting the whole surface area of a cube at the rate of 10 paise per cm² is ₹ 264.40. then, the volume of the cube is

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(a) 6859 \text{ cm}^2 (b) 9261 \text{ cm}^2 (c) 8000 \text{ cm}^2 (d) 10648 \text{ cm}^2
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Solution:

(b)9261 cm²

Explanation:

Total surface area of the cube = $6 a^2$ Cost of the painting the cube = $6 a^2 \times 10$ $246.6 = 6 a^2 \times 10$ $a^2 = 4.41$ a = 2.1Volume of the cube = a^3 V= $(2.1)^3$

5. How many bricks, each measuring 25cm × 11.25cm × 6cm, will be needed to build a wall 8m long, 6m high and 22.5 cm thick?

(a)5600

Solution:

(c)6400

Explanation:

We know that volume of cuboid= length \times breadth \times height Volume of brick = $25 \text{cm} \times 11.25 \text{cm} \times 6 \text{cm}$ = 1678.5 cm^3 Volume of the wall = $80 \times 60 \times 22.5$

= 10800000 cm³ Number of bricks = 10800000/ 1678.5 = 6400

6. How many cubes 0f 10cm edge can be put in a cubical box of 1m edge?
(a)10 (b)100 (c)1000 (d)10000

Solution:

(c)1000

Explanation:

Volume of the cube = a^3



Volume of the smaller cube = 10^3 =1000 Volume of the box = a^3 = $(100)^3$ =1000000 Total number of cubes = 1000000/1000=1000

7. The edges of a cuboid have their volumes in the ratio 1:2:3 and its surface area is 88cm². The volume of the cuboid is

(a)48 cm³

(b) 64 cm³

(c) 96 cm³

(d) 120 cm³

Solution:

(a) 48 cm^3

Explanation:

Let a be the length of smallest edge.

The edges are in the proportion a: 2a: 3a

We know that total surface area of cuboid= 2(l b + b h + h l)

Surface area = $2(2 a^2 + 3 a^2 + 6 a^2)$

 $88 = 22 a^2$

a = 2

2a=4

3a = 6

We know that volume of cuboid= length × breadth × height

 $V = 2 \times 4 \times 6$

V = 48

8. Two cubes have their volumes in the ratio 1:27. The ratio of their surface areas is

(a)1:3

(b)1:9

(c)1:27

(d)none of these

Solution:

(b)1:9

Explanation:

Volume in the ratio 1:27

$$1/27 = 1/3 = a^3/b^3$$

b/a = 3

Therefore on squaring 1:9

9. The surface area of a 10cm × 4cm × 6cm brick is



(a)84cm² (b) 124cm² (c)164cm² (d) 180cm²

Solution:
(c)164cm²

Explanation:
We know that total surface area of cuboid= 2(l b + b h + h l)
= 2 (40 + 30 + 12)

10. The surface area is 9m long, 40cm wide and 20cm high. If 1 cubic meter of iron weighs 50 kg, what is the weight of the beam?

(a)56kg

= 164

(b)48kg

(c)36kg

(d)27kg

Solution:

(c)36kg

Explanation:

We know that volume of cuboid= length × breadth × height

 $V = 9 \times 0.2 \times 0.4$

 $V = 0.72 \text{m}^3$

Weight = $0.72 \times 50 = 36 \text{kg}$

11. A rectangular water reservoir contains 42000 liters of water. If the length of reservoir is 6m and its breadth is 3.5m, the depth of the reservoir is

(a)2m

(b)5m

(c)6m

(d)8m

Solution:

(a)2m

Explanation:

We know that volume of cuboid= length × breadth × height

h = volume / I b

 $h = 42/6 \times 3.5$

h = 2

12. The dimensions of a room are 10cm × 8cm × 3.3cm. How many men can be accommodated in this room if each man requires 3m³ of space?

(a)99

(b)88

(c)77

(d)75

Solution:

(b)88

Explanation:



We know that volume of cuboid= length × breadth × height

 $V = 10 \times 8 \times 3.3$

 $V = 264m^3$

Total number of people can be accommodated = 264/3 = 88

- 13. A rectangular water tank is 3m long, 2m wide and 5m high. How many liters of water can it hold?
 - (a)30000
- (b)15000
- (c)25000
- (d)35000

Solution:

(a)30000

Explanation:

We know that volume of cuboid= length × breadth × height

 $V = 3 \times 2 \times 5$

 $V = 30m^3$

V= 30000I

- 14. The area of the cardboard needed to make a box of size 25cm × 15cm × 8cm will
 - (a)390cm²
- (b) 1390cm² (c)2780cm² (d) 1000cm²

Solution:

(b) 1390cm²

Explanation:

We know that total surface area of cuboid= 2(l b + b h + h l)

- = 2 (375 + 120 + 200)
- = 1390
- **15.** The diagonal of a cube measures 4 $\sqrt{3}$ cm. its volume is
 - (a)8cm³
- (b) 16cm³
- (c)27cm³
- (d) 64cm³

Solution:

(d) 64cm³

Explanation:

Diagonal of cube = a $\sqrt{3}$ = 4 $\sqrt{3}$

a = 4

Volume of cube = a^3 = 4^3 = 64 cm^3