

RS Aggarwal Solutions for Class 10 Maths Chapter 17 Volume and Surface Area of Solids**Exercise 17A**

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Question 1: Two cubes each of volume 27 cm^3 are joined end to end to form a solid. Find the surface area of the resulting cuboid.

Solution:

Volume of cube = 27 cm^3 (given)

Let 'a' cm be the length of each side of the cube.

We know, volume of cube = $(\text{side})^3$ cubic units

$$\Rightarrow 27 = a^3$$

$$\text{or } a = 3 \text{ cm}$$

When two cubes are joined cuboid is formed.

Find dimensions of cuboid:

$$\text{Length} = l = 2a = 2 \times 3 \text{ cm} = 6 \text{ cm}$$

$$\text{Breadth} = b = a = 3 \text{ cm}$$

$$\text{Height} = h = a = 3 \text{ cm}$$

Now,

$$\text{Surface area of cuboid} = 2(lb + bh + lh)$$

$$= 2(6 \times 3 + 3 \times 3 + 6 \times 3)$$

$$= 2(18 + 9 + 18)$$

$$= 90$$

Surface area of resulting cuboid is 90 cm^2

Question 2: The volume of a hemisphere is $2425\frac{1}{2} \text{ cm}^3$. Find its curved surface area.

Solution:

$$\text{Volume of a hemisphere} = 2425\frac{1}{2} = 4851\frac{1}{2} \text{ cm}^3$$

We know, Volume of a hemisphere = $\frac{2}{3} \pi r^3$

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$$4851/2 = \frac{2}{3} \pi r^3$$

$$r^3 = (4851 \times 21)/88$$

$$r = 10.5$$

So, radius of hemisphere is 10.5 cm.

$$\text{Curved Surface Area of hemisphere} = 2\pi r^2$$

$$\begin{aligned} &= 2 \times \frac{22}{7} \times (10.5)^2 \\ &= 693 \end{aligned}$$

Curved surface area of hemisphere is 693 cm².

Question 3: If the total surface area of a solid hemisphere is 462 cm², then find its volume.

Solution:

$$\text{Total surface area of a solid hemisphere} = 462 \text{ cm}^2$$

$$\text{We know, Total surface area of a solid hemisphere} = 3\pi r^2$$

$$462 = 3\pi r^2$$

$$r^2 = 3234/66$$

$$\text{or } r = 7$$

$$\text{Now, volume of solid hemisphere} = \frac{2}{3} \pi r^3$$

$$\begin{aligned} &= \frac{2}{3} \times \frac{22}{7} \times 7 \times 7 \times 7 \\ &= 2156/3 \\ &= 718.67 \end{aligned}$$

So, volume of solid hemisphere is 718.67 cm³

Question 4: (i) A 5-m-wide cloth is used to make a conical tent of base diameter 14 m and height 24 m. Find the cost of cloth used at the rate of Rs.25 per metre.

Solution:

Given:

Width of cloth used = 5 m

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Diameter of conical tent = 14 m
Let r be the radius of the conical tent.
Diameter of conical tent = 14 m
Radius = $r = 14/2$ m = 7 m
Height = $h = 24$ m
Let slant height of conical tent = l m

$$\text{So, } l = \sqrt{r^2 + h^2} = \sqrt{7^2 + 24^2}$$
$$l = 25 \text{ m}$$

$$\begin{aligned}\text{Curved Surface area of conical tent} &= \pi r l \\ &= 22/7 \times 7 \times 25 \text{ m}^2 \\ &= 550 \text{ m}^2\end{aligned}$$

Which is the area of cloth required to make a conical tent that is 550 m^2

Now,
Area of cloth required = Length of cloth used \times width of cloth
or
Length of cloth used = Area of cloth required \div width of cloth

$$\begin{aligned}&= 550/5 \text{ m} \\ &= 110 \text{ m}\end{aligned}$$

$$\text{Length of cloth used} = 110 \text{ m}$$

$$\text{Given, Cost of cloth used} = \text{Rs } 25 \text{ per meter}$$

$$\begin{aligned}\text{Total Cost of cloth required to make a conical tent} &= 110 \times \text{Rs } 25 \\ &= \text{Rs } 2750\end{aligned}$$

(ii) The radius and height of a right circular cone are in the ratio 5:12. If its volume is 314 cubic cm. find the total surface area [Take $\pi = 22/7$]

Solution:

Radius and height of a right circular cone are in the ratio of 5:12.
Let the radius and height be $5x$, $12x$ respectively.
Volume of cone = 314 cm^3 . (given)
We know, Volume of cone = $\frac{1}{3} \pi r^2 h$

$$\frac{1}{3} \pi r^2 h = 314$$

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$$\frac{1}{3} \times \frac{22}{7} \times (5x)^2 \times 12x = 314$$

$$300x^3 = 300$$

$$\text{or } x = 1$$

This implies,

Radius = 5 cm and

Height = 7 cm

$$\text{Slant height}(l) = \sqrt{h^2 + r^2}$$
$$\sqrt{12^2 + 5^2}$$

$$l = \sqrt{144 + 25}$$

$$l = \sqrt{169}$$

$$\text{or } l = 13 \text{ cm.}$$

We know, Total surface area = $\pi r(l + r)$

$$= \frac{22}{7} \times 5 (13 + 5)$$

$$= 282.6 \text{ cm}^2$$

Question 5: If the volumes of two cones are in the ratio of 1:4 and their diameters are in the ratio of 4:5, then find the ratio of their heights.

Solution:

Let V_1 be the volume of first cone and V_2 be the volume of second cone.

$$\text{Then, } V_1:V_2 = 1:4 \text{ (Given) } \dots\dots(1)$$

Let d_1 be the diameter of first cone and d_2 be the diameter of second cone.

$$\text{Then } d_1:d_2 = 4:5 \text{ (given) } \dots(2)$$

Let h_1 be the height of first cone and h_2 be the height of second cone.

$$\text{We know that, volume of cone} = V = \frac{1}{3}\pi\left(\frac{d^2}{4}\right)h$$

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$$\frac{V_1}{V_2} = \frac{\frac{1}{3}\pi\frac{d_1^2}{4}h_1}{\frac{1}{3}\pi\frac{d_2^2}{4}h_2}$$

$$\frac{V_1}{V_2} = \frac{d_1^2 h_1}{d_2^2 h_2}$$

$$\frac{1}{4} = \frac{d_1^2 h_1}{d_2^2 h_2}$$

(From (1))

$$\frac{1}{4} = \left(\frac{d_1}{d_2}\right)^2 \times \frac{h_1}{h_2}$$

$$\frac{1}{4} = \left(\frac{4}{5}\right)^2 \times \frac{h_1}{h_2}$$

$$\frac{h_1}{h_2} = \frac{25}{64}$$

(Using equation (2))

Therefore, Ratio of height of two cones is 25:64.

Question 6: The slant height of a conical mountain is 2.5 km and the area of its base is 1.54 km². Find the height of the mountain.

Solution:

Given:

Slant height of conical mountain = 2.5 km

Area of its base = 1.54 km²

Let the radius of base be 'r' km, height of the mountain is 'h' km and slant height be 'l' km

Area of base = πr^2

$$1.54 = \pi r^2$$

$$1.54 = \frac{22}{7} r^2$$

$$\text{or } r = 0.7 \text{ km}$$

We know that, $l^2 = r^2 + h^2$

$$(2.5)^2 = (0.7)^2 + h^2$$

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$$6.25 - 0.49 = h^2$$

$$\text{or } h = 2.4 \text{ km}$$

Question 7: The sum of the radius of the base and the height of a solid cylinder is 37 metres. If the total surface area of the cylinder be 1628 sq metres, find its volume.

Solution:

Let radius = r and

Height = h

The sum of the radius of the base and the height of a solid cylinder is 37 metres.

$$\Rightarrow r + h = 37 \text{ m} \dots(1)$$

Total surface area of the cylinder = $2\pi r(r + h)$

$$1628 = 2 \times \frac{22}{7} \times r \times 37$$

$$1628 = \frac{148}{7} \times r$$

$$r = \frac{11396}{1628}$$

$$r = 7$$

$$\text{From (1): } 7 + h = 37$$

$$h = 30$$

Again,

Volume of the cylinder = $\pi r^2 h$

$$= \frac{22}{7} \times 7 \times 7 \times 30$$

$$= 22 \times 7 \times 30$$

$$= 4620 \text{ m}^3$$

Question 8: The surface area of a sphere is 2464 cm^2 . If its radius be doubled, then what will be the surface area of the new sphere?

Solution:

Surface area of a sphere = 2464 cm^2 (Given)

$$4\pi r^2 = 2464$$

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If the radius is doubled, then new radius is $2r$

Now,

Surface area of a sphere with radius $2r = 4\pi (2r)^2$

$$= 4 \times 4\pi r^2$$

$$= 4 \times 2464$$

$$= 9856 \text{ cm}^2$$

Question 9: A military tent of height 8.25 m is in the form of a right circular cylinder of base diameter 30 m and height 5.5 m surmounted by a right circular cone of same base radius. Find the length of canvas used in making the tent, if the breadth of the canvas is 1.5 m.

Solution:

A military tent is made as a combination of right circular cylinder and right circular cone on top.

Given :

Total Height of tent = $h = 8.25 \text{ m}$

Base diameter of tent = 30 m, then

Base radius of tent = $r = 30/2 \text{ m} = 15 \text{ m}$

Height of right circular cylinder = 5.5 m

Base radius of cone = 15 m

Let slant height of cone = $l \text{ m}$

Now,

Curved surface area of right circular cylindrical part of tent = $2\pi rh$

and

Height of conical part = total height of tent – height of cylindrical part

$$\text{Height of cone} = 8.25 - 5.5 = 2.75 \text{ m}$$

$$l^2 = h^2 + r^2$$

$$= 2.75^2 + 15^2$$

$$= 232.5625$$

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$$\text{or } l = 15.25 \text{ m}$$

$$\text{Curved surface area of conical part of the tent} = \pi r l$$

Total surface area of the tent = Curved surface area of cylindrical part + curved surface area of conical part

$$\text{Total surface area of tent} = 2\pi r h + \pi r l$$

$$= \pi r (2h + l)$$

$$= \frac{22}{7} \times 15 \times (2 \times 5)$$

$$= 1237.5$$

$$\text{Total surface area of tent is } 1237.5 \text{ m}^2$$

$$\text{Breadth of canvas used} = 1.5 \text{ m}$$

$$\text{Length of canvas used} \times \text{breadth of canvas used} = \text{Total surface area of tent}$$

$$\text{Length of canvas used} = 1237.5 \div 1.5 = 825$$

$$\text{Length of canvas used is } 825 \text{ m. Answer!!}$$

Question 10: A tent is in the shape of a right circular cylinder up to a height of 3 m and conical above it. The total height of the tent is 13.5 m and the radius of its base is 14 m. Find the cost of cloth required to make the tent at the rate of Rs.80 per square metre. [take $\pi = \frac{22}{7}$]

Solution:

The tent is made as a combination of right circular cylinder and right circular cone on top.

$$\text{Height of cylindrical part of the tent} = h = 3 \text{ m}$$

$$\text{Radius of its base} = r = 14 \text{ m}$$

$$\text{Total height of the tent} = 13.5 \text{ m}$$

$$\text{Curved surface area of cylindrical part of tent} = 2\pi r h$$

$$= 2 \times \frac{22}{7} \times 14 \times 3$$

$$= 264 \text{ m}^2$$

$$\text{Height of conical part of the tent} = \text{total height of tent} - \text{height of cylindrical part}$$

$$\text{Height of conical part of the tent} = 13.5 - 3 \text{ m} = 10.5 \text{ m}$$

Let the slant height of the conical part be l .

$$l^2 = h^2 + r^2 \text{ (used cone height)}$$

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$$= 110.25 + 196$$

$$= 306.25$$

$$\text{or } l = 17.5 \text{ m}$$

Curved surface area of conical part of tent = πrl

$$= 22/7 \times 14 \times 17.5$$

$$= 770$$

Total surface area of tent = Curved surface area of cylindrical part of tent + Curved surface area of conical part of tent.

$$\text{Total Surface area of tent} = 264 + 770$$

$$= 1034 \text{ m}^2$$

$$\text{Cloth required} = \text{Total Surface area of tent} = 1034 \text{ m}^2$$

$$\text{Cost of cloth} = \text{Rs } 80/\text{m}^2 \text{ (given)}$$

$$\text{Total cost of cloth required} = \text{Total surface area of tent} \times \text{Cost of cloth}$$

$$= 1034 \times \text{Rs. } 80$$

$$= \text{Rs. } 82720$$

Cost of cloth required to make the tent is Rs. 82720

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Question 1: A solid metallic cuboid of dimensions $9\text{m} \times 8\text{m} \times 2\text{m}$ is melted and recast into solid cubes of edge 2m . Find the number of cubes so formed.

Solution:

A solid metallic cuboid of dimensions $9\text{m} \times 8\text{m} \times 2\text{m}$ (given)

Length (l) = 9 m

Breadth (b) = 8 m

Height (h) = 2 m

Edge of a cube (a) = 2 m

Let n be the number of required cubes.

To find: Value of n

Number of cubes = (volume of a cuboid)/ volume of each cube)

$$= lbh/a^3$$

$$= (9 \times 8 \times 2)/(2 \times 2 \times 2)$$

$$= 18$$

Therefore, total number of 18 cubes required.

Question 2: A cone of height 20 cm and radius of base 5 cm is made up of modelling clay. A child reshapes it in the form of a sphere. Find the diameter of the sphere.

Solution:

Radius of the cone = $r = 5\text{ cm}$ and

Height of the cone = $h = 20\text{ cm}$

Let the radius of the sphere = R

As per given statement,

Volume of sphere = Volume of cone

$$\frac{4}{3} \pi R^3 = \frac{1}{3} \pi r^2 h$$

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$$4R^3 = 5 \times 5 \times 20$$

$$R = 5 \text{ cm}$$

$$\text{Diameter of the sphere} = 2R = 2 \times 5 = 10 \text{ cm}$$

Question 3: Metallic spheres of radii 6 cm, 8 cm and 10 cm respectively are melted to form a single solid sphere. Find the radius of the resulting sphere.

Solution:

Radius of 1st sphere = $r_1 = 6 \text{ cm}$

Radius of 2nd sphere = $r_2 = 8 \text{ cm}$ and

Radius of third sphere = $r_3 = 10 \text{ cm}$

Let radius of the resulting sphere = R

Now,

Volume of resulting sphere = Volume of three metallic spheres

$$\frac{4}{3} \pi R^3 = \frac{4}{3} \pi (r_1^3 + r_2^3 + r_3^3)$$

$$= \frac{4}{3} \pi (6^3 + 8^3 + 10^3)$$

$$R^3 = 1728$$

$$\text{or } R = 12 \text{ cm}$$

Radius of the resulting sphere is 12cm.

Question 4: A solid metal cone with base radius of 12 cm and height 24 cm is melted to form solid spherical balls of diameter 6 cm each. Find the number of balls thus formed.

Solution:

Let the number of balls formed are n

As per statement,

Volume of metal cone = Total volume of n spherical balls

Volume of cone = $n(\text{Volume of any spherical ball})$

$$\frac{1}{3} \pi r^2 h = n \left(\frac{4}{3} \pi r^3 \right)$$

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$$12^2 \times 24 = n \times 108$$

$$\text{or } n = 32$$

Therefore, 32 spherical balls can be formed.

Question 5: The radii of internal and external surfaces of a hollow spherical shell are 3 cm and 5 cm respectively. It is melted and recast into a solid cylinder of diameter 14 cm. Find the height of the cylinder.

Solution:

Let r_1 and r_2 be the internal and external base radii of spherical shell.

$$r_1 = 3 \text{ cm, and } r_2 = 5 \text{ cm}$$

Base radius of solid cylinder, $r = 7 \text{ cm}$

Let the height of the cylinder = h

As per given statement:

The hollow spherical shell is melted into a solid cylinder, so

Volume of solid cylinder = Volume of spherical shell

$$\pi r^2 h = \frac{4}{3} \pi (r_2^3 - r_1^3)$$

$$\Rightarrow 49h = \frac{4}{3}(125 - 27)$$

$$\text{or } h = \frac{8}{3} \text{ cm}$$

Question 6: The internal and external diameters of a hollow hemispherical shell are 6 cm and 10 cm, respectively. It is melted and recast into a solid cone of base diameter 14 cm. Find the height of the cone so formed.

Solution:

Internal radius of hemisphere = 3 cm and external radius of hemisphere = 5 cm

Diameter of cone = 14 cm

Radius of cone = 7 cm

Now,

Volume of the hollow hemisphere = Volume of the cone

$$\text{Volume of cone} = \frac{1}{3} \pi r^2 h$$

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Volume of the hollow hemisphere = $\frac{2}{3} \pi (R^3 - r^3)$

$$\frac{2}{3} \pi (R^3 - r^3) = \frac{1}{3} \pi r^2 h$$

$$\frac{2}{3} \times \frac{22}{7} (5^3 - 3^3) = \frac{1}{3} \times \frac{22}{7} \times 72 \times h$$

$$2 \times 98 = 49h$$

$$\text{or } h = 4 \text{ cm}$$

Height of the cone formed is 4 cm.

Question 7: A copper rod of diameter 2 cm and length 10 cm is drawn into a wire of uniform thickness and length 10 m. Find the thickness of the wire.

Solution:

Recall MU: 1m = 1000 mm and 1 cm = 10 mm

Diameter of the copper Rod = 2cm

Radius of the copper rod = $r = 1$ cm

Length of the Rod = $h = 10$ cm

Length of the wire = $h = 10$ m = 1000cm

Let suppose the radius of the wire = R

From the statement: Volume of the rod = volume of the wire

$$\pi r^2 h = \pi R^2 H$$

$$1 \times 1 \times 10 = 1000 \times R$$

$$\text{or } R = \frac{1}{10} \text{ cm or } 0.1 \text{ cm}$$

$$\text{Diameter of the wire} = 2r = 2 \times 0.1 = 0.2 \text{ cm}$$

Therefore, the thickness of the wire is 0.2 cm or 2mm.

Question 8: A hemispherical bowl of internal diameter 30 cm contains some liquid. This liquid is to be poured into cylindrical bottles of diameter 5 cm and height 6 cm each. Find the number of bottles necessary to empty the bowl.

RS Aggarwal Solutions for Class 10 Maths Chapter 17 Volume and Surface Area of Solids**Solution:**

Internal diameter of hemispherical bowl = 30 cm

Radius = 15 cm

$$\text{Volume} = \frac{2}{3} \pi r^3$$

$$= \frac{2}{3} \pi (15)^3$$

$$= 2250 \pi \text{ cm}^3$$

Diameter of the cylindrical bottle = 5 cm

Radius = 2.5 cm

$$\text{Volume of one cylindrical bottle} = \pi r^2 h$$

$$= \pi \times (2.5)^2 \times 6$$

$$= 37.5 \pi \text{ cm}^3$$

Now,

Amount of water in n bottles = Amount of water in bowl

$$n \times 37.5 \pi = 2,250 \pi$$

$$\text{or } n = 60$$

So, 60 numbers of bottles are required to empty the bowl.

Question 9: A solid metallic sphere of diameter 21 cm is melted and recast into a number of smaller cones, each of diameter 3.5 cm and height 3 cm. Find the number of cones so formed.

Solution:

Diameter of sphere = 21 cm

Radius = $\frac{21}{2}$ cm

Height of the cone = 3 cm

Radius of the cone = $\frac{7}{4}$ cm

$$\text{Volume of the sphere} = \frac{4}{3} \pi r^3 = \frac{4}{3} \times \pi \times \left(\frac{21}{2}\right)^3 \text{ cm}^3$$

$$\text{Volume of cone} = \frac{1}{3} \pi r^2 h = \frac{1}{3} \pi \left(\frac{7}{4}\right)^2 \times 3 \text{ cm}^3$$

Let n be the number of cone formed, then

$$n = (\text{Volume of the sphere}) / (\text{Volume of cone})$$

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$$n = (4/3 \times \pi \times (21/2)^3) / (1/3 \pi (7/4)^2 \times 3)$$

$$= 504$$

Number of cones formed = 504

Question 10: A spherical cannon ball, 28 cm in diameter is melted and recast into a right circular conical mould, base of which is 35 cm in diameter. Find the height of the cone.

Solution:

Radius of cannon ball = 14 cm

$$\text{Volume of cannon ball} = 4/3 \pi r^3 = 4/3 \pi (14)^3$$

Radius of Cone = 35/2 cm

$$\text{Volume of Cone} = 1/3 \pi r^2 h = 1/3 \pi (35/2)^2 h$$

Let h be the height of the cone.

From statement:

Volume of cannon ball = Volume of Cone

$$\Rightarrow 4/3 \pi (14)^3 = 1/3 \pi (35/2)^2 h$$

$$h = 35.84$$

Therefore, height of the cone is 35.84 cm.

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Question 1: A drinking glass is in the shape of a frustum of a cone of height 14 cm. The diameters of its two circular ends are 16 cm and 12 cm. Find the capacity of the glass.

Solution:

Diameter of lower circular end of glass = 12 cm

Radius of lower circular end = $r = 12/2 = 6$ cm

Diameter of upper circular end of glass = 16 cm

Radius of lower circular end = $R = 16/2 = 8$ cm

Height of glass = $h = 14$ cm

Capacity of glass = $\frac{1}{3} \pi h (R^2 + r^2 + Rr)$

$$= \frac{1}{3} \times \frac{22}{7} \times 14 (8^2 + 6^2 + 8 \times 6)$$

$$= \frac{44}{3} (64 + 36 + 48)$$

$$= 2170.67$$

Capacity of glass is 2170.67 cm³

Question 2: The radii of the circular ends of a solid frustum of a cone are 18 cm and 12 cm and its height is 8 cm. Find its total surface area. [Use $\pi = 3.14$]

Solution:

Height of frustum = $h = 8$ cm

Radius of lower circular end = $r = 12$ cm

Radius of upper circular end = $R = 18$ cm

Let l = slant height

Slant height = $l^2 = (R-r)^2 + h^2$ cm

$$= 36 + 64$$

$$= 100$$

or $l = 10$ cm

We know, Total surface area of frustum = $\pi r^2 + \pi R^2 + \pi(R + r)l$ cm²

$$= \pi \times 12^2 + \pi \times 18^2 + \pi \times (18 + 12) \times 10 \text{ cm}^2$$

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$$= 3.14(144 + 324 + 300) \\ = 2411.52$$

Total surface area of frustum is 2411.52 cm^2

Question 3: A metallic bucket, open at the top, of height 24 cm is in the form of the frustum of a cone, the radii of whose lower and upper circular ends are 7 cm and 14 cm, respectively. Find

(i) the volume of water which can completely fill the bucket;

(ii) the area of the metal sheet used to make the bucket.

Solution:

Radius of lower circular end = $r = 7 \text{ cm}$

Radius of upper circular end = $R = 14 \text{ cm}$

Height of bucket = $h = 24 \text{ cm}$

Slant height of frustum:

$$l = \sqrt{(R - r)^2 + h^2} \\ = \sqrt{(14 - 7)^2 + 24^2} \\ = \sqrt{7^2 + 24^2} \\ = \sqrt{49 + 576} \\ = \sqrt{625} \\ = 25 \text{ cm}$$

(i)

$$\text{Volume of frustum of cone} = \frac{1}{3} \pi h (R^2 + r^2 + Rr) \text{ cm}^3$$

$$= \frac{1}{3} \times \frac{22}{7} \times 24 \times (14^2 + 14 \times 7 + 7^2)$$

$$= \frac{1}{3} \times \frac{22}{7} \times 24 \times (196 + 98 + 49)$$

$$= \frac{1}{3} \times \frac{22}{7} \times 24 \times (343)$$

$$= 8624 \text{ cm}^3$$

(ii)

$$\text{Curved surface area} = \pi (R + r) l$$

$$= \frac{22}{7} \times 25 \times (14 + 7)$$

$$= 1650 \text{ cm}^2$$

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Area of the base of bucket = πr^2
(consider lower base of bucket)
 $= \frac{22}{7} \times 7 \times 7$
 $= 154 \text{ cm}^2$

Area of metal sheet used to make the bucket = curved surface area + Area of the base
 $= 1650 + 154$
 $= 1804$
Area of metal sheet used to make the bucket is 1804 cm^2

Question 4: A container, open at the top, is in the form of a frustum of a cone of height 24 cm with radii of its lower and upper circular ends as 8 cm and 20 cm, respectively. Find the cost of milk which can completely fill the container at the rate of Rs. 21 per litre.

Solution:

Radius of lower circular end = $r = 8 \text{ cm}$

Radius of upper circular end = $R = 20 \text{ cm}$

Cost of 1 litre milk = Rs. 24

Height of frustum container = $h = 24 \text{ cm}$

Volume of frustum of cone = $\frac{1}{3} \pi h (R^2 + r^2 + Rr) \text{ cm}^3$

Volume of milk completely fill the container = Volume of frustum of cone

$= \frac{1}{3} \pi \times 24 (20^2 + 8^2 + 20 \times 8)$

$= 15689.14 \text{ cm}^3$

$= 15.68914 \text{ litres}$

Since 1 litre is 1000 cm^3

Cost of 1 liter milk = Rs. 21

Cost of 15.68914 liter milk = Rs. 21 \times 15.68914 = Rs. 329.47

Question 5: A container made of a metal sheet open at the top is of the form of a frustum of cone, whose height is 16 cm and the radii of its lower and upper circular edges are 8 cm and 20 cm respectively. Find

(i) the cost of metal sheet used to make the container if it costs Rs. 10 per 100 cm^2 .

(ii) the cost of milk at the rate of Rs. 35 per liter which can fill it completely.

Solution:

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Radius of lower end = $r = 8$ cm

Radius of upper end = $R = 20$ cm

Height of container frustum = $h = 16$ cm

Cost of 100 cm^2 metal sheet = Rs 10

So, Cost of 1 cm^2 metal sheet = $10/100 = \text{Rs } 0.1$

Let l be the slant height.

$$l^2 = (R-r)^2 + h^2$$

$$= (20-8)^2 + 16^2$$

$$= 256 + 144$$

$$= 400$$

$$\text{or } l = 20 \text{ cm}$$

Surface area of frustum of the cone = $\pi r^2 + \pi(R+r)l \text{ cm}^2$

$$= \pi[(20+8)20 + 8^2]$$

$$= \pi[560 + 64]$$

$$= 624 \times \frac{22}{7}$$

$$= 1961.14 \text{ cm}^2$$

(i) Find cost of metal sheet used to make the container if it costs Rs. 10 per 100 cm^2

Cost of metal sheet per $100 \text{ cm}^2 = \text{Rs. } 10$

Cost of metal for Rs. $1961.14 \text{ cm}^2 = (1961.14 \times 10)/100 = \text{Rs. } 196.114$

(ii) Find the volume of frustum:

$$\text{Volume of frustum} = \frac{1}{3} \pi h(r^2 + R^2 + rR)$$

$$= \frac{1}{3} \times \frac{22}{7} \times 16(8^2 + 20^2 + 8 \times 20)$$

$$= \frac{1}{3} \times \frac{22}{7} \times 16(64 + 400 + 160)$$

$$= 10345.4208 \text{ cm}^3$$

$$= 10.345 \text{ liters}$$

Using

$$1000 \text{ cm}^3 = 1 \text{ litre}$$

$$1 \text{ cm}^3 = \frac{1}{1000} \text{ litre}$$

Cost of 1 liter milk = Rs. 35

Cost of 10.345 liter milk = Rs. $35 \times 10.345 = \text{Rs. } 363$ (approx)

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Question 6: The radii of the circular ends of a solid frustum of a cone are 33 cm and 27 cm, and its slant height is 10 cm. Find its capacity and total surface area. [take $\pi = 22/7$]

Solution:

The radii of the circular ends of a solid frustum of a cone are 33 cm and 27 cm, and its slant height is 10 cm.

$$\begin{aligned}h &= \sqrt{l^2 - (R^2 - r^2)} \text{ cm} \\&= \sqrt{(10)^2 - (33 - 27)^2} \text{ cm} \\&= \sqrt{(10)^2 - (6)^2} = \sqrt{64} \text{ cm} = 8 \text{ cm}\end{aligned}$$

Height is 8 cm

Capacity of frustum:

$$\begin{aligned}&= \frac{1}{3} \pi h (R^2 + r^2 + Rr) \\&= \frac{1}{3} \times \frac{22}{7} \times 8 [(33)^2 + (27)^2 + 33 \times 27] \\&= (8.38 \times 2709) \text{ cm}^3 = 22701.4\end{aligned}$$

Capacity of frustum is 22701.4 cm^3

Total Surface area:

$$\begin{aligned}&= [\pi R^2 + \pi r^2 + \pi l (R + r)] \\&= \pi [R^2 + r^2 + l (R + r)] \\&= \frac{22}{7} [(33)^2 + (27)^2 + 10 \times (33 + 27)] \\&= \left(\frac{22}{7} \times 2418 \right) \\&= 7599.43\end{aligned}$$

Total Surface area of cone is 7599.43 cm^2 .

Question 7.

A bucket is in the form of a frustum of a cone. Its depth is 15 cm and the diameters of the top and the bottom are 56 cm and 42 cm respectively. Find how many litres of water the bucket can hold. [take $\pi = 22/7$]

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Solution:

Depth of the bucket = height of frustum = $h = 15$ cm

Diameter of top of bucket = 56 cm

Radius of top = $R = 56/2 = 28$ cm

Diameter of bottom of bucket = 42 cm

Radius of bottom = $r = 42/2 = 21$ cm

$$\text{Volume of frustum of cone} = \frac{1}{3}\pi h(R^2 + r^2 + Rr) \text{ cm}^3$$

$$= \frac{1}{3} \times \frac{22}{7} \times 15(28^2 + 21^2 + 28 \times 21)$$

$$= 22 \times 5 \times 259$$

$$= 28490$$

Since Volume of water bucket can hold = volume of bucket which is in form of frustum

So, volume of water bucket can hold is 28490 cm^3 or = 28.49 litres

Question 8: A bucket made up of a metal sheet is in the form of a frustum of a cone of height 16 cm and radii of its lower and upper ends are 8 cm and 20 cm respectively. Find the cost of the bucket if the cost of metal sheet used is Rs. 15 per 100 cm^2 . [use $\pi = 3.14$]

Solution:

Radius of lower circular end = $r = 8$ cm

Radius of upper circular end = $R = 20$ cm

Height of container frustum = $h = 16$ cm

Cost of 100 cm^2 metal sheet = rs. 15

Cost of 1 cm^2 metal sheet = $15/100 = \text{Rs. } 0.15$

$$\text{Slant height, } l^2 = (R-r)^2 + h^2$$

$$= (20-8)^2 + 16^2$$

$$= 144 + 256$$

$$= 400$$

$$\text{or } l = 20 \text{ cm}$$

Now,

$$\text{Area of metal sheet used} = (\text{Total surface area of frustum}) - (\text{Area of upper circle}) \dots(1)$$

$$\text{Area of upper circle} = \pi R^2$$

$$\text{Total surface area of frustum} = \pi r^2 + \pi R^2 + \pi(R+r)l \text{ cm}^2$$

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(1)=>

$$\text{Area of metal sheet used} = (\pi r^2 + \pi R^2 + \pi(R + r)l) - \pi R^2$$

$$= \pi r^2 + \pi(R + r)l$$

$$= \pi(8^2 + (20 + 8)20)$$

$$= 1959.36 \text{ cm}^2$$

Again,

$$\text{Cost of } 1959.36 \text{ cm}^2 \text{ metal sheet} = 1959.36 \times \text{cost of } 1 \text{ cm}^2 \text{ metal sheet}$$

$$= 1959.36 \times \text{Rs. } 0.15$$

$$= \text{Rs. } 293.904$$

Question 9: A bucket made up of a metal sheet is in the form of frustum of a cone. Its depth is 24 cm and the diameters of the top and bottom are 30 cm and 10 cm respectively. Find the cost of milk which can completely fill the bucket at the rate of Rs. 20 per litre and the cost of metal sheet used if it costs Rs. 10 per 100 cm². [use $\pi = 3.14$]

Solution:

Let $r = 5$ cm, $R = 15$ cm and $h = 24$ cm

Slant height:

$$\begin{aligned} l &= \sqrt{h^2 + (R - r)^2} \\ &= \sqrt{(24)^2 + (10)^2} \text{ cm} \\ &= \sqrt{576 + 100} \text{ cm} \\ &= \sqrt{676} \text{ cm} \\ &= 26 \text{ cm} \end{aligned}$$

Volume of bucket = Volume of frustum

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$$\begin{aligned} &= \frac{1}{3} \pi h (R^2 + r^2 + Rr) \\ &= \frac{1}{3} \times 3.14 \times 24 \times [(15)^2 + (5)^2 + 15 \times 5] \\ &= (25.12 \times 325) \text{ cm}^3 \\ &= 8164 \text{ cm}^3 = 8.164 \text{ litres} \end{aligned}$$

$$\text{Cost of milk} = \text{Rs. } 20 \times 8.164 = \text{Rs. } 163.28$$

Total surface area of the bucket:

$$\begin{aligned} &= \pi l (R + r) + \pi r^2 \\ &= (3.14 \times 26 \times 20 + 3.14 \times 5 \times 5) \\ &= 1711.3 \text{ cm}^2 \end{aligned}$$

$$\text{Cost of sheet} = 1711.3 \times 10/100 = \text{Rs. } 171.13$$

Question 10: A container in the shape of a frustum of a cone having diameters of its two circular faces as 35 cm and 30 cm and vertical height 14 cm, is completely filled with oil. If each cm^3 of oil has mass 1.2 g, then find the cost of oil in the container if it costs Rs. 40 per kg.

Solution:

Diameter of top of container = 35 cm

Radius of top = $R = 35/2 = 17.5$ cm

Diameter of bottom of container = 30 cm

Radius of bottom = $r = 30/2 = 15$ cm

1 cm^3 of oil = 1.2g of oil, so, Cost of 1 kg oil = Rs. 40

Height of frustum = $h = 14$ cm

$$\text{Volume of frustum of cone} = \frac{1}{3} \pi h (R^2 + r^2 + Rr) \text{ cm}^3$$

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$$\text{Volume of oil in container} = \frac{1}{3} \times \frac{22}{7} \times 14(17.5^2 + 15^2 + 17.5 \times 15)$$

$$= \frac{22}{3} \times 2 \times 793.75$$

$$= \frac{34925}{3}$$

$$\text{Volume of oil in container} = 11641.667 \text{ cm}^3 \text{ or } 11641.667 \times 1.2 \text{ g} = 13970.0004 \text{ g or } 13.970 \text{ kg}$$

(As $1000 \text{ g} = 1 \text{ kg}$)

$$\text{Cost of } 13.970 \text{ kg oil} = \text{Rs. } 20 \times 13.970 = \text{Rs. } 558.8 \text{ Answer!!}$$

RS Aggarwal Solutions for Class 10 Maths Chapter 17 Volume and Surface Area of Solids**Exercise 17D**

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Question 1: A river 1.5 m deep and 36 m wide is flowing at the rate of 3.5 km/hr. Find the amount of water (in cubic metres) that runs into the sea per minute.

Solution:

Depth of the river = 1.5 m

Width of the river = 36 m

Using units:

1 hour = 60 minutes

1 km = 1000 m

Flow rate of river = 3.5 km/hr

= $(3.5 \times 1000) / (1 \times 60)$ m/min

= $350/6$ m/min

The amount of water that runs into sea per minute =

$$350/6 \times 1.5 \times 36 = 350 \times 1.5 \times 6 = 3150$$

The amount of water that runs into sea per minute is $3150 \text{ m}^3/\text{min}$.

Question 2: The volume of a cube is 729 cm^3 . Find its surface area.

Solution:

Volume of a cube is 729 cm^3 (given)

we know, Volume of the cube = $(\text{side})^3$

$$(\text{side})^3 = 729$$

or Side = 9

Each side measure of a cube is 9 cm.

Now,

Total surface area of the cube = $6(\text{side})^2$

$$= 6 \times 9^2$$

$$= 6 \times 81$$

$$= 486$$

Total surface area of the cube is 486 cm^2 .

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Question 3: How many cubes of 10 cm edge can be put in a cubical box of 1 m edge?

Solution:

Let 'a' be edge of a cube, so edge = 1m or 100 cm

Volume of cube of 100 cm edge = $(\text{side})^3$

$$= (100)^3$$

$$= 1000000 \text{ cm}^3$$

Volume of cubes of 10cm edge = $10^3 = 1000 \text{ cm}^3$

Now,

Number of required cubes = $(\text{Volume of cube of 100 cm edge}) / (\text{Volume of cubes of 10cm edge})$

$$= 1000000 / 1000000$$

$$= 1000$$

Answer!!

Question 4: Three cubes of iron whose edges are 6 cm, 8 cm and 10 cm, respectively are melted and formed into a single cube. Find the edge of the new cube formed.

Solution:

Edge of the first cube = 6 cm

Volume of the first cube = $(\text{side})^3 = (6)^3 \text{ cm}^3$

Edge of the second cube = 8 cm

Volume of the second cube = $(\text{side})^3 = (8)^3 \text{ cm}^3$

Edge of the third cube = 10 cm

Volume of the third cube = $(\text{side})^3 = (10)^3 \text{ cm}^3$

Let "a" be side edge of the new formed cube.

Volume of the formed cube = Volume of the First cube + Volume of the Second cube + Volume of the Third Cube

$$a^3 = 6^3 + 8^3 + 10^3$$

$$= 216 + 512 + 1000$$

$$= 1728$$

$$\text{Or } a = 12$$

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Edge of the new cube is 12 cm.

Question 5: Five identical cubes, each of edge 5 cm, are placed adjacent to each other. Find the volume of the resulting cuboid.

Solution:

Edge of the given Cube = 5 cm

When 5 identical cubes are placed adjacent to each other, the length of cuboid formed is $5 \times 5 = 25$ cm

Now, Volume of the resulting cuboid = $l b h$

$$= 25 \times 5 \times 5$$

$$= 625 \text{ cm}^3$$

Question 6: The volumes of two cubes are in the ratio 8 : 27. Find the ratio of their surface areas.

Solution:

Ratio of two cube = 8:27

Let volumes of the two cubes be $8x$ and $27x$

Let a and b be the sides of first cube and second cube respectively.

Volume of cube = $(\text{side})^3$

$$8x = a^3$$

$$\text{and } 27x = b^3$$

Formula to find surface area = $6(\text{side})^2$

$$\frac{6(2\sqrt[3]{x})^2}{6(3\sqrt[3]{x})^2} = \frac{4}{9}$$

The required ratio is 4:9.

Question 7: The volume of a right circular cylinder with its height equal to the radius is $25\frac{1}{7} \text{ cm}^3$. Find the height of the cylinder.

Solution:

Volume of the right circular Cylinder = $176\frac{2}{7} \text{ cm}^3$

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Height of the right circular cylinder = Radius of the right circular cylinder
 $\Rightarrow h = r$

We know, Volume of the right circular Cylinder = $\pi r^2 h$

$$\pi r^2 h = 176/7$$

$$22/7 \times h^2 \times h = 176/7$$

$$h^3 = 8$$

$$\text{or } h = 2 \text{ cm}$$

Height of the cylinder is 2 cm.

Question 8: The ratio between the radius of the base and the height of a cylinder is 2 : 3. If the volume of the cylinder is 12936 cm^3 , then find the radius of the base of the cylinder.

Solution:

Volume of the cylinder = 12936 cm^3

Ratio of the base and the height of a cylinder is 2:3

Let $2x$ be the radius and $3x$ be the height.

Volume of the cylinder = 12936 cm^3

$$\pi r^2 h = 12936$$

$$22/7 \times (2x)^2 (3x) = 12936$$

$$x^3 = 343$$

$$\text{or } x = 7$$

Radius of the base is 14 cm.

Question 9: The radii of two cylinders are in the ratio of 2 : 3 and their heights are in the ratio of 5 : 3. Find the ratio of their volumes.

Solution:

The radii of two cylinders are in the ratio of 2 : 3 and their heights are in the ratio of 5 : 3.

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Let $2r$ and $3r$ are the radii and $5h$ and $3h$ be the heights.

$$\text{Ratio of their volumes} = \frac{\pi(2r)^2(5h)}{\pi(3r)^2(3h)}$$

$$= 20/27$$

Ratio of their volumes is 20:27

Question 10: 66 cubic cm of silver is drawn into a wire 1 mm in diameter. Calculate the length of the wire in metres.

Solution:

Diameter of the wire = 1 mm

Radius of wire = $r = 1/2$ mm = 0.5 mm = 0.05 cm

Let the length of the wire be h

Volume of the wire = 66 cm^3

$$\pi r^2 h = 66$$

$$22/7 \times 0.05 \times 0.05 \times h = 66$$

$$h = (66 \times 7 \times 400) / 22$$

$$h = 8400$$

Length of the wire is 8400 cm or 84 m.