

## EXERCISE 6 PAGE: 188

# 1. What is the difference between a theorem and an axiom? Solution:

A statement where proof is required is called a theorem whereas a basic fact where proof is not required is called as an axiom.

#### Example:

Theorem – Pythagoras theorem

Axiom – A line can be drawn through two points.

### 2. Define the following terms:

- (i) Line segment
- (ii) Ray
- (iii) Intersecting Lines
- (iv) Parallel Lines
- (v) Half-line
- (vi) Concurrent lines
- (vii) Collinear points
- (viii) Plane

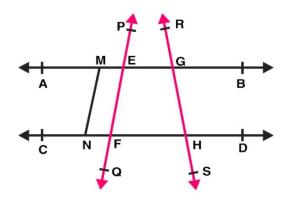
#### **Solution:**

- (i) Line Segment A straight path between two points is called the line segment.
- (ii) Ray A line segment when extended indefinitely in one direction is the ray.
- (iii) Intersecting Lines Two lines having a common point are called intersecting lines.
- (iv) Parallel Lines Two lines in a plane are said to be parallel, if they have no point in common.
- (v) Half-line A straight line which extends from a point indefinitely in one direction only is as a half-line.
- (vi) Concurrent lines Three or more lines intersecting at the same point are said to be concurrent.
- (vii) Collinear points Three or more than three points are said to be collinear, if there is a line which contains them all.
- (viii) Plane A plane is a surface such that every point of the line joining any two points on it, lies on it.

### 3. In the adjoining figure, name:

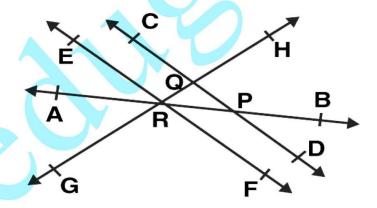
- (i) Six points
- (ii) Five line segments
- (iii) Four rays
- (iv) Four lines
- (v) Four collinear points





### **Solution:**

- (i) A, B, C, D, E, F
- (ii)  $\overline{EG}, \overline{FH}, \overline{EF}, \overline{GH}, \overline{MN}$
- (iii)  $\overrightarrow{EP}, \overrightarrow{GR}, \overrightarrow{GB}, \overrightarrow{HD}$
- (iv)  $\overrightarrow{AB}, \overrightarrow{CD}, \overrightarrow{PQ}, \overrightarrow{RS}$
- (v) M, E, G, B
- 4. In the adjoining figure, name:
- (i) Two pairs of intersecting lines and their corresponding points of intersection
- (ii) Three concurrent lines and their points of intersection
- (iii) Three rays
- (iv) Two line segments



### **Solution:**

(i) 
$$\left\{ \overrightarrow{EF}, \overrightarrow{GH}, R \right\}, \left\{ \overrightarrow{AB}, \overrightarrow{CD}, P \right\}$$

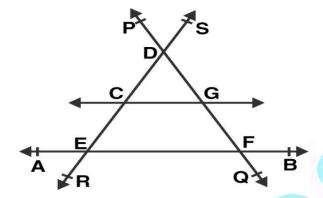


$$(ii)$$
  $\overrightarrow{AB}, \overrightarrow{EF}, \overrightarrow{GH}, R$ 

(iii) 
$$\overrightarrow{RB}, \overrightarrow{RH}, \overrightarrow{RG}$$

(iv) 
$$\overline{RQ}, \overline{RP}$$

- 5. From the given figure, name the following:
- (i) Three lines
- (ii) One rectilinear figure
- (iii) Four concurrent points



### **Solution:**

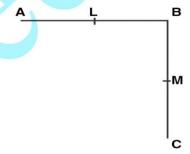
- (i) Three lines are line AB, line PQ and line RS
- (ii) One rectilinear figure is CEFG
- (iii) Four concurrent points are A, E, F and B.

6.

- (i) How many lines can be drawn to pass through a given point?
- (ii) How many lines can be drawn to pass through two given points?
- (iii) In how many points can the two lines at the most intersect?
- (iv) If A, B, C are three collinear points, name all the line segments determined by them. Solution:
- (i) Infinite number of lines can be drawn to pass through a given point.
- (ii) Only one line can be drawn to pass through two given points.
- (iii) Two lines at the most can intersect at one point only.
- (iv)  $\overline{AB}, \overline{BC}, \overline{AC}$
- 7. Which of the following statements are true?
- (i) A line segment has no definite length.



- (ii) A ray has no end point.
- (iii) A line has a definite length.
- (iv) A line
- (v) A ray
- (vi) Two distinct points always determine a unique line.
- (vii) Three lines are concurrent if they have a common point.
- (viii) Two distinct lines cannot have more than one point in common.
- (ix) Two intersecting lines cannot be both parallel to the same line.
- (x) Open half-line is the same thing as ray.
- (xi) Two lines may intersect in two points.
- (xii) Two lines are parallel only when they have no point in common. Solution:
- (i) False. A line segment has definite length.
- (ii) False. A ray has one end point.
- (iii) False. A line has no definite length.
- (iv) True.
- (v) False. BA and AB have different end points.
- (vi) True.
- (vii) True.
- (viii) True.
- (ix) True.
- (x) True.
- (xi) False. Two lines intersect at only one point.
- (xii) True.
- 8. In the given figure, L and M are the mid-points of AB and BC respectively.
- (i) If AB = BC, prove that AL = MC.
- (ii) If BL = BM, prove that AB = BC.





#### **Solution:**

(i) According to the diagram
We know that L is the midpoint of the line AB
So we get

$$AL = BL = 1/2 AB \dots (1)$$

We know that M is the midpoint of the line BC So we get BM = MC = 1/2 BC....(2)

According to the question It is given that AB = BC

We can also write it as 1/2 AB = 1/2 BC According to equation (1) and (2) We can write it as AL = MC

(ii) According to the diagram
We know that L is the midpoint of the line AB
So we get AL = BL = 1/2 ABThe above equation can be written as  $2AL = 2BL = AB \dots (3)$ 

We also know that M is the midpoint of the line BC BM = MC = 1/2 BCThe above equation can be written as  $2BM = 2MC = BC \dots (4)$ 

According to the question It is given that BL = BM

According to the equation (3) and (4) We can write it as AB = BC