RD Sharma Solutions for Class 9 Maths Chapter 1 Number System

Exercise 1.1 Page No: 1.5

Question 1: Is zero a rational number? Can you write it in the form p/q, where p and q are integers and q ≠ 0?
Solution:
Yes, zero is a rational number.

It can be written in p/q form provided that q ≠ 0.

For Example: 0/1 or 0/3 or 0/4 etc.

Question 2: Find five rational numbers between 1 and 2.
Solution:
We know, one rational number between two numbers m and n = (m+n)/2

To find: 5 rational numbers between 1 and 2

Step 1: Rational number between 1 and 2

= (1+2)/2

= 3/2

Step 2: Rational number between 1 and 3/2

= (1+3/2)/2

= 5/4

Step 3: Rational number between 1 and 5/4

= (1+5/4)/2

= 9/8

Step 4: Rational number between 3/2 and 2

= 1/2 [(3/2) + 2)]

= 7/4

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Step 5: Rational number between 7/4 and 2

= 1/2 [7/4 + 2]

= 15/8

Arrange all the results: 1 < 9/8 < 5/4 < 3/2 < 7/4 < 15/8 < 2

Therefore required integers are, 9/8, 5/4, 3/2, 7/4, 15/8

Question 3: Find six rational numbers between 3 and 4.

Solution:

Steps to find n rational numbers between any two numbers:

Step 1: Multiply and divide both the numbers by n+1.

In this example, we have to find 6 rational numbers between 3 and 4. Here n = 6

Multiply 3 and 4 by 7

3 x 7/7 = 21/7 and

4 x 7/7 = 28/7

Step 2: Choose 6 numbers between 21/7 and 28/7

3 = 21/7 < 22/7 < 23/7 < 24/7 < 25/7 < 26/7 < 27/7 < 28/7 = 4

Therefore, 6 rational numbers between 3 and 4 are

22/7, 23/7, 24/7, 25/7, 26/7, 27/7

Question 4: Find five rational numbers between 3/5 and 4/5.

Solution:

Steps to find n rational numbers between any two numbers:

Step 1: Multiply and divide both the numbers by n+1.

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In this example, we have to find 5 rational numbers between 3/5 and 4/5. Here n = 5

Multiply 3/5 and 4/5 by 6

3/5 x 6/6 = 18/30 and

4/5 x 6/6 = 24/30

Step 2: Choose 5 numbers between 18/30 and 24/30

3/5 = 18/30 < 19/30 < 20/30 < 21/30 < 22/30 < 23/30 < 24/30 = 4/5

Therefore, 5 rational numbers between 3/5 and 4/5 are

19/30, 20/30, 21/30, 22/30, 23/30

Question 5: Are the following statements true or false? Give reason for your answer.

(i) Every whole number is a natural number.

(ii) Every integer is a rational number.

(iii) Every rational number is an integer.

(iv) Every natural number is a whole number,

(v) Every integer is a whole number.

(vi) Every rational number is a whole number.

Solution:

(i) False.

Reason: As 0 is not a natural number.

(ii) True.

(iii) False.

Reason: Numbers such as 1/2, 3/2, 5/3 are rational numbers but not integers.

(iv) True.

(v) False.

Reason: Negative numbers are not whole numbers.

(vi) False.

Reason: Proper fractions are not whole numbers

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Exercise 1.2 Page No: 1.12

Question 1: Express the following rational numbers as decimals.
(i) 42/100 (ii) 327/500 (iii) 15/4

Solution:

(i) By long division method

100) $\overline{42}$ (0.42

400

$\overline{200}$

200

$\overline{0}$

Therefore, $\frac{42}{100}$ = 0.42

(ii) By long division method

500) $\overline{327.000}$ (0.654

3000

$\overline{2700}$

2500

$\overline{2000}$

2000

$\overline{0}$

Therefore, $\frac{327}{500}$ = 0.654

(iii) By long division method

4) $\overline{15.00}$ (3.75

12

$\overline{30}$

28

$\overline{20}$

20

$\overline{0}$

Therefore, $\frac{15}{4} = 3.75$

Question 2: Express the following rational numbers as decimals.
(i) 2/3 (ii) -4/9 (iii) -2/15 (iv) -22/13 (v) 437/999 (vi) 33/26
Solution:

(i) Divide 2/3 using long division:

$$\begin{array}{r|l} & 0.66666 \\ 3 & 2.00000 \\ & \underline{0} \\ & 20 \\ & \underline{18} \\ & \;\;20 \\ & \;\;\underline{18} \\ & \;\;\;\;20 \\ & \;\;\;\;\underline{18} \\ & \;\;\;\;\;\;20 \\ & \;\;\;\;\;\;\underline{18} \\ & \;\;\;\;\;\;\;\;20 \\ & \;\;\;\;\;\;\;\;\underline{18} \\ & \;\;\;\;\;\;\;\;\;\;2 \end{array}$$

$\frac{2}{3} = 0.666... = 0.\bar{6}$

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(ii) Divide using long division: -4/9

9) $\overline{4.000}$ (0.444

3600

$\overline{4000}$

3600

$\overline{4000}$

3600

$\overline{400}$

$\frac{-4}{9} = -0.4444... = -0.\bar{4}$

(iii) Divide using long division: -2/15

```
      0.133
15)2.0000
    15
    --
     50
     45
     --
      50
      45
      --
       6
```

$-\frac{2}{15} = -0.133 = -0.1\bar{3}$

(iv) Divide using long division: -22/13

1.69230769
13) 22.000
13
90
78
120
117
30
26
40
39
100
91
90
78
120
117
3

$-\frac{22}{13} = -1.6923076923... = -1.\overline{692307}$

(v) Divide using long division: 437/999

999) 437.0000 (0.43743
3996
3740
2997
7430
6993
4370
3996
3740
2997
743

$\frac{437}{999} = 0.43743... = 0.\overline{437}$

(vi) Divide using long division: 33/26

```
      1.2692307692
  26)33.000000000
     26
     ---
      70
      52
     ---
      180
      156
      ---
       240
       234
       ---
         60
         52
         --
          80
          78
          --
          200
          182
          ---
           180
           156
           ---
            24
```

$\frac{33}{26} = 1.269230769... = 1.\overline{2692307}$

Question 3: Look at several examples of rational numbers in the form p/q (q ≠ 0), where p and q are integers with no common factors other than 1 and having terminating decimal representations. Can you guess what property q must satisfy?

Solution:

The decimal representation will be terminating, if the denominators have factors 2 or 5 or both. Therefore, p/q is a terminating decimal, when prime factorization of q must have only powers of 2 or 5 or both.

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Exercise 1.3 — Page No: 1.22

Question 1: Express each of the following decimals in the form p/q:
(i) 0.39
(ii) 0.750
(iii) 2.15
(iv) 7.010
(v) 9.90
(vi) 1.0001

Solution:
(i)
0.39 = 39/100
(ii)
0.750 = 750/1000 = 3/4
(iii)
2.15 = 215/100 = 43/20
(iv)
7.010 = 7010/1000 = 701/100
(v)
9.90 = 990/100 = 99/10
(vi)
1.0001 = 10001/10000

Question 2: Express each of the following decimals in the form p/q:

(i) $0.\overline{4}$ (ii) $0.\overline{37}$
(iii) $0.\overline{54}$ (iv) $0.\overline{621}$
(v) $125.\overline{3}$ (vi) $4.\overline{7}$
(vii) $0.4\overline{7}$

Solution:
(i) Let x = $0.\overline{4}$
or x = $0.\overline{4}$ = 0.444 .... (1)
Multiplying both sides by 10
10x = 4.444 .....(2)
Subtract (1) by (2), we get
10x – x = 4.444... - 0.444...
9x = 4
x = 4/9
=> $0.\overline{4}$ = 4.9

(ii) Let x = 0.3737.. .... (1)
Multiplying both sides by 100
100x = 37.37... .....(2)
Subtract (1) from (2), we get

100x – x = 37.37... - 0.3737...
100x – x = 37
99x = 37
x = 37/99

(iii) Let x = 0.5454... (1)
Multiplying both sides by 100
100x = 54.5454.... (2)
Subtract (1) from (2), we get
100x – x = 54.5454.... – 0.5454....
99x = 54
x = 54/99

(iv) Let x = 0.621621... (1)
Multiplying both sides by 1000
1000x = 621.621621.... (2)
Subtract (1) from (2), we get
1000x – x = 621.621621.... – 0.621621....
999x = 621
x = 621/999
or x = 23/37

(v) Let x = 125.3333.... (1)
Multiplying both sides by 10
10x = 1253.3333.... (2)
Subtract (1) from (2), we get
10x – x = 1253.3333.... – 125.3333....
9x = 1128
or x = 1128/9
or x = 376/3

(vi) Let x = 4.7777.... (1)
Multiplying both sides by 10
10x = 47.7777.... (2)

Subtract (1) from (2), we get

10x – x = 47.7777…. – 4.7777….
9x = 43
x = 43/9

(vii) Let x = 0.47777….
Multiplying both sides by 10
10x = 4.7777….   ...(1)
Multiplying both sides by 100
100x = 47.7777….   (2)
Subtract (1) from (2), we get
100x – 10x = 47.7777…. – 4.7777…
90x = 43
x = 43/90

(iii) $2 + \sqrt{3}$

Here, 2 is a rational number but $\sqrt{3}$ is an irrational number

Therefore, the sum of a rational and irrational number is an irrational number.

(iv) $\sqrt{3} + \sqrt{2}$

$\sqrt{3}$ is not a perfect square thus an irrational number.

$\sqrt{2}$ is not a perfect square, thus an irrational number.

Therefore, sum of $\sqrt{2}$ and $\sqrt{3}$ gives an irrational number.

(v) $\sqrt{3} + \sqrt{5}$

$\sqrt{3}$ is not a perfect square and hence, it is an irrational number

Similarly, $\sqrt{5}$ is not a perfect square and also an irrational number.

Since, sum of two irrational number, is an irrational number, therefore $\sqrt{3} + \sqrt{5}$ is an irrational number.

(vi) $(\sqrt{2} - 2)^2$

$(\sqrt{2} - 2)^2 = 2 + 4 - 4\sqrt{2}$

$= 6 + 4\sqrt{2}$

Here, 6 is a rational number but $4\sqrt{2}$ is an irrational number.

Since, the sum of a rational and an irrational number is an irrational number, therefore, $(\sqrt{2} - 2)2$ is an irrational number.

(vii) $(2 - \sqrt{2})(2 + \sqrt{2})$

We can write the given expression as;

$(2 - \sqrt{2})(2 + \sqrt{2}) = ((2)^2 - (\sqrt{2})^2)$

[Since, $(a + b)(a - b) = a^2 - b^2$]

(iii) $2 + \sqrt{3}$

Here, 2 is a rational number but $\sqrt{3}$ is an irrational number

Therefore, the sum of a rational and irrational number is an irrational number.

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$(\sqrt{2} – 2)^2 = 2 + 4 – 4\sqrt{2}$

$= 6 + 4\sqrt{2}$

Here, 6 is a rational number but $4\sqrt{2}$ is an irrational number.

Since, the sum of a rational and an irrational number is an irrational number, therefore, $(\sqrt{2} – 2)2$ is an irrational number.

(vii) $(2 – \sqrt{2})(2 + \sqrt{2})$

We can write the given expression as;

$(2 – \sqrt{2})(2 + \sqrt{2}) = ((2)^2 − (\sqrt{2})^2)$

[Since, $(a + b)(a – b) = a^2 – b^2$]

= 4 – 2 = 2 or 2/1

Since, 2 is a rational number, therefore, (2 – √2)(2 + √2) is a rational number.

(viii) (√3 + √2)^2

We can write the given expression as;

(√3 + √2)^2 = (√3)^2 + (√2)^2 + 2√3 x √2

= 3 + 2 + 2√6

= 5 + 2√6

[using identity, (a+b)^2 = a^2 + 2ab + b^2]

Since, the sum of a rational number and an irrational number is an irrational number, therefore, (√3 + √2)^2 is an irrational number.

(ix) √5 – 2

√5 is an irrational number whereas 2 is a rational number.

The difference of an irrational number and a rational number is an irrational number.

Therefore, √5 – 2 is an irrational number.

(x) √23

Since, √23 = 4.795831352331…

As decimal expansion of this number is non-terminating and non-recurring therefore, it is an irrational number.

(xi) √225

√225 = 15 or 15/1

√225 is rational number as it can be represented in the form of p/q and q not equal to zero.

(xii) 0.3796

As the decimal expansion of the given number is terminating, therefore, it is a rational number.

(xiii) 7.478478……

As the decimal expansion of this number is non-terminating recurring decimal, therefore, it is a rational number.

(xiv) 1.101001000100001……

As the decimal expansion of given number is non-terminating and non-recurring, therefore, it is an irrational number

Question 4: Identify the following as rational or irrational numbers. Give the decimal representation of rational numbers:

(i) $\sqrt{4}$ (ii) $3\sqrt{18}$ (iii) $\sqrt{1.44}$

(iv) $\sqrt{\frac{9}{27}}$ (v) $-\sqrt{64}$ (vi) $\sqrt{100}$

Solution:

(i) √4

√4 = 2, which can be written in the form of a/b. Therefore, it is a rational number.

Its decimal representation is 2.0.

(ii) 3√18

3√18 = 9√2

Since, the product of a rational and an irrational number is an irrational number.

Therefore, 3√18 is an irrational.

Or 3 × √18 is an irrational number.

(iii) √1.44

√1.44 = 1.2

Since, every terminating decimal is a rational number, Therefore, √1.44 is a rational number.

And, its decimal representation is 1.2.

(iv) √9/27

√9/27 = 1/√3

Since, we know, quotient of a rational and an irrational number is irrational numbers, therefore, √9/27 is an irrational number.

(v) – √64

– √64 = – 8 or – 8/1

Therefore, – √64 is a rational number.

Its decimal representation is –8.0.

(vi) √100

√100 = 10

Since, 10 can be expressed in the form of a/b, such as 10/1,

Therefore, √100 is a rational number.

And it's decimal representation is 10.0.

Question 5: In the following equation, find which variables x, y, z etc. represent rational or irrational numbers:

(i) $x^2 = 5$

(ii) $y^2 = 9$

(iii) $z^2 = 0.04$

(iv) $u^2 = 17/4$

(v) $v^2 = 3$

(vi) $w^2 = 27$

(vii) $t^2 = 0.4$

Solution:

(i) x^2 = 5

Taking square root both the sides,

x = √5

√5 is not a perfect square root, so it is an irrational number.

(ii) y^2 = 9

y^2 = 9
or y = 3

3 can be expressed in the form of a/b, such as 3/1, so it a rational number.

(iii) z^2 = 0.04

z^2 = 0.04

Taking square root both the sides, we get

z = 0.2

0.2 can be expressed in the form of a/b such as 2/10, so it is a rational number.

(iv) u^2 = 17/4

Taking square root both the sides, we get

u = √17/2

Since, quotient of an irrational and a rational number is irrational, therefore, u is an Irrational number.

(v) v^2 = 3

Taking square root both the sides, we get

v = √3

Since, √3 is not a perfect square root, so v is irrational number.

(vi) $w^2 = 27$

Taking square root both the sides, we get

$w = 3\sqrt{3}$

Since, the product of a rational and irrational is an irrational number. Therefore, w is an irrational number.

(vii) $t^2 = 0.4$

Taking square root both the sides, we get

$t = \sqrt{(4/10)}$

$t = 2/\sqrt{10}$

Since, quotient of a rational and an irrational number is irrational number. Therefore, t is an irrational number.

Exercise 1.5 Page No: 1.35

Question 1: Complete the following sentences:
(i) Every point on the number line corresponds to a …… number which many be either …… or …….
(ii) The decimal form of an irrational number is neither ….. nor ……
(iii) The decimal representation of a rational number is either ….. or …..
(iv) Every real number is either … number or … number.

Solution:
(i) Every point on the number line corresponds to a **real** number which many be either **rational** or **irrational**.
(ii) The decimal form of an irrational number is neither **terminating** nor **repeating**.
(iii) The decimal representation of a rational number is either **terminating** or **non-terminating recurring**.
(iv) Every real number is either **rational** number or **an irrational** number.

Question 2: Represent √6, √7, √8 on the number line.
Solution:
Find the equivalent values of √6, √7, √8

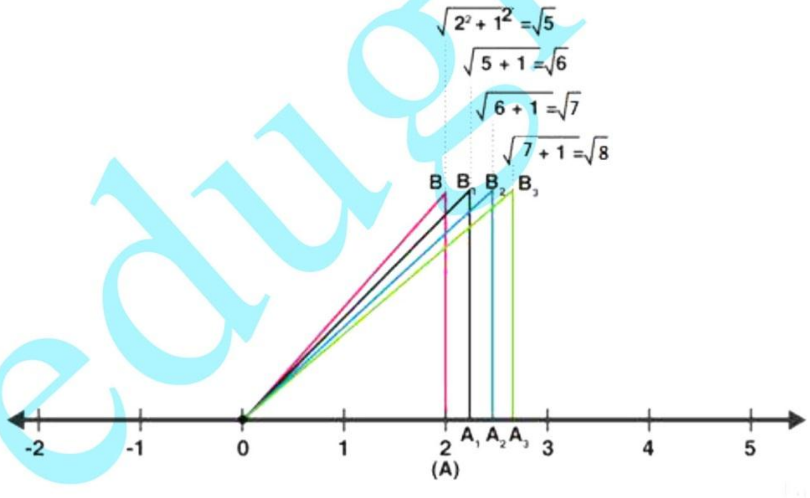
√6 = 2.449

√7 = 2.645

√8 = 2.828

We can see that, all the given numbers lie between 2 and 3.

Draw on number line:



Question 3: Represent √3.5, √9.4, √10.5 and on the real number line.
Solution:
Represent √3.5 on number line
Step 1: Draw a line segment AB = 3.5 units

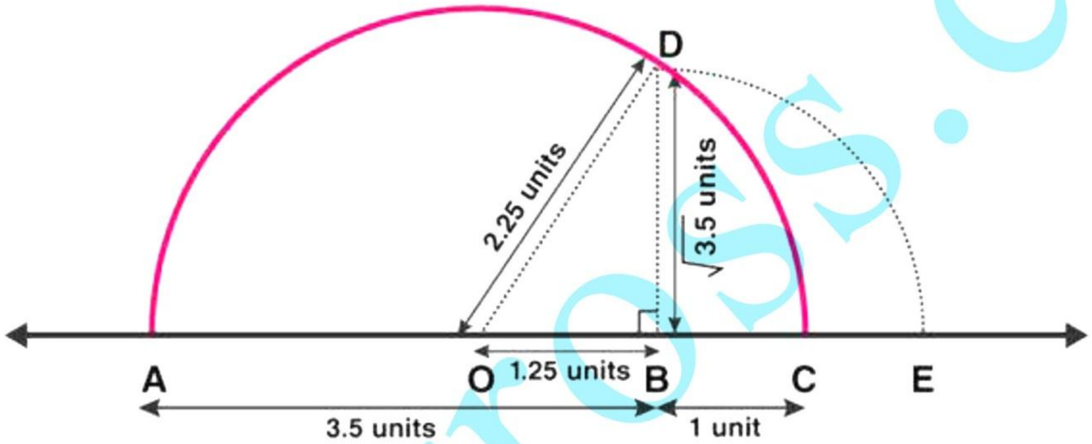
Step 2: Produce B till point C, such that BC = 1 unit

Step 3: Find the mid-point of AC, say O.

Step 4: Taking O as the centre draw a semi circle, passing through A and C.

Step 5: Draw a line passing through B perpendicular to OB, and cut semicircle at D.

Step 6: Consider B as a centre and BD as radius draw an arc cutting OC produced at E.



Now, from right triangle OBD,

BD^2 = OD^2 - OB^2

= OC^2 - (OC - BC)^2

(As, OD = OC)

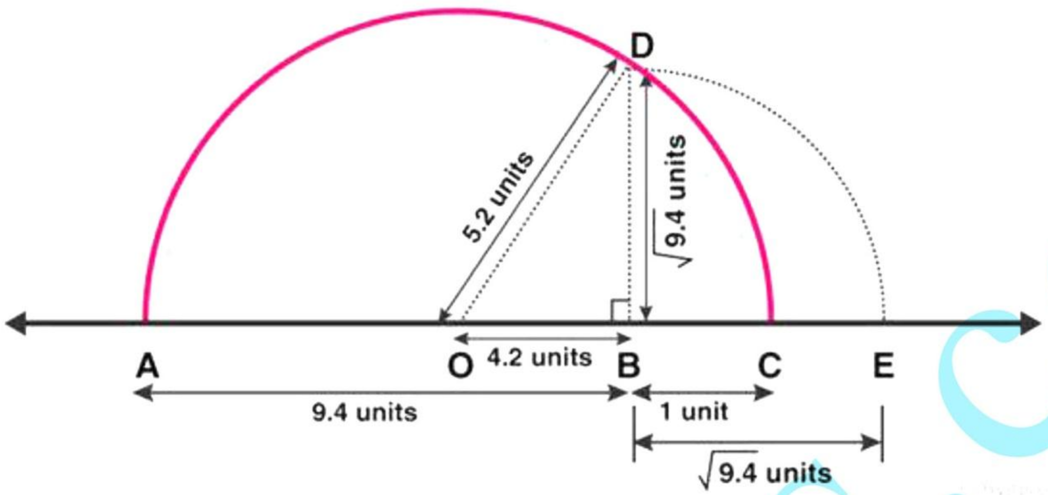
BD^2 = 2OC x BC - (BC)^2

= 2 x 2.25 x 1 - 1
= 3.5
=> BD = √3.5

Represent √9.4 on number line

Step 1: Draw a line segment AB = 9.4 units

Follow step 2 to Step 6 mentioned above.



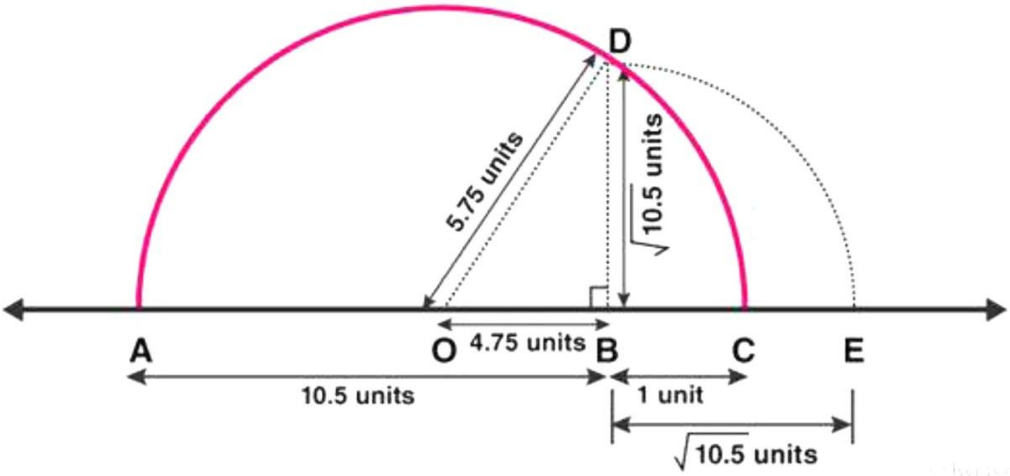
BD^2 = 2OC x BC - (BC)^2

= 2 x 5.2 x 1 - 1
= 9.4
=> BD = √9.4

Represent √10.5 on number line

Step 1: Draw a line segment AB = 10.5 units

Follow step 2 to Step 6 mentioned above, we get



BD^2 = 2OC x BC - (BC)^2

= 2 x 5.75 x 1 - 1
= 10.5
=> BD = √10.5

Question 4: Find whether the following statements are true or false:
(i) Every real number is either rational or irrational.
(ii) π is an irrational number.
(iii) Irrational numbers cannot be represented by points on the number line.

Solution:
(i) True.
(ii) True.
(ii) False.

Exercise 1.6 Page No: 1.39

Question 1: Visualise 2.665 on the number line, using successive magnification.

Solution:
2.665 is lies between 2 and 3 on the number line.

Divide selected segment into 10 equal parts and mark each point of division as 2.1, 2.2, ...,2.9, 2.10

2.665 is lies between 2.6 and 2.7

Divide line segment between 2.6 and 2.7 in 10 equal parts such as 2.661, 2.662, and so on.

Here we can see that 5th point will represent 2.665.

Question 2: Visualise the representation of 5.37 on the number line upto 5 decimal places, that is upto 5.37777.

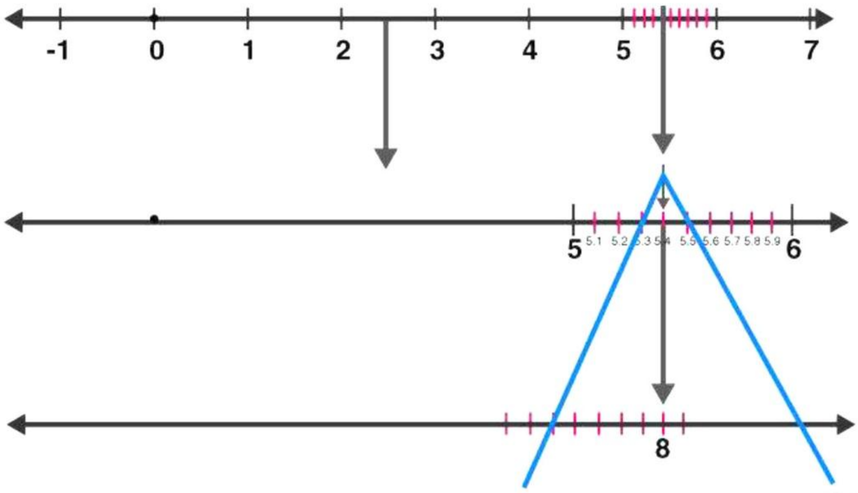
Solution:

Clearly 5.37 is located between 5 and 6.
Again by successive magnification, and successively decrease 5.37 located between 5.3 and 5.4.

For more clarity, divide 5.3 and 5.4 portion of the number line into 10 equal parts and we can see 5.37 lies between 5.37 and 5.38.

To visualize 5.37 more accurately, divide line segment between 5.37 and 5.38 in ten equal parts.
5.37 lies between 5.377 and 5.378.

Again divide above portion between 5.377 and 5.378 into 10 equal parts, which shows 5.37 is located closer to 5.3778 than to 5.3777


-1
0
1
2
3
4
5
6
7
5
5.1
5.2
5.3
5.4
5.5
5.6
5.7
5.8
5.9
6
8