

**R D Sharma Solutions For Class 10 Maths Chapter 4 -
Triangles****Exercise 4.1****Page No: 4.3****1. Fill in the blanks using the correct word given in brackets:**

- (i) All circles are _____ (congruent, similar).
- (ii) All squares are _____ (similar, congruent).
- (iii) All _____ triangles are similar (isosceles, equilaterals).
- (iv) Two triangles are similar, if their corresponding angles are _____ (proportional, equal)
- (v) Two triangles are similar, if their corresponding sides are _____ (proportional, equal)
- (vi) Two polygons of the same number of sides are similar, if (a) _____ their corresponding angles are and their corresponding sides are (b) _____ (equal, proportional).

Solutions:

- (i) All circles are similar.
- (ii) All squares are similar.
- (iii) All equilateral triangles are similar.
- (iv) Two triangles are similar, if their corresponding angles are equal.
- (v) Two triangles are similar, if their corresponding sides are proportional.
- (vi) Two polygons of the same number of sides are similar, if (a) equal their corresponding angles are and their corresponding sides are (b) proportional.

**R D Sharma Solutions For Class 10 Maths Chapter 4 -
Triangles****Exercise 4.2**

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1. In a ΔABC , D and E are points on the sides AB and AC respectively such that $DE \parallel BC$.**i) If $AD = 6$ cm, $DB = 9$ cm and $AE = 8$ cm, Find AC.****Solution:**Given: ΔABC , $DE \parallel BC$, $AD = 6$ cm, $DB = 9$ cm and $AE = 8$ cm.

Required to find AC.

By using Thales Theorem, [As $DE \parallel BC$]

$$AD/BD = AE/CE$$

Let $CE = x$.

So then,

$$6/9 = 8/x$$

$$6x = 72 \text{ cm}$$

$$x = 72/6 \text{ cm}$$

$$x = 12 \text{ cm}$$

$$\therefore AC = AE + CE = 12 + 8 = 20.$$

ii) If $AD/DB = 3/4$ and $AC = 15$ cm, Find AE.**Solution:**Given: $AD/BD = 3/4$ and $AC = 15$ cm [As $DE \parallel BC$]

Required to find AE.

By using Thales Theorem, [As $DE \parallel BC$]

$$AD/BD = AE/CE$$

Let, $AE = x$, then $CE = 15 - x$.

$$\Rightarrow 3/4 = x/(15-x)$$

$$45 - 3x = 4x$$

$$-3x - 4x = -45$$

$$7x = 45$$

$$x = 45/7$$

$$x = 6.43 \text{ cm}$$

$$\therefore AE = 6.43 \text{ cm}$$

iii) If $AD/DB = 2/3$ and $AC = 18$ cm, Find AE.**Solution:**Given: $AD/BD = 2/3$ and $AC = 18$ cm

Required to find AE.

By using Thales Theorem, [As $DE \parallel BC$]

$$AD/BD = AE/CE$$

Let, $AE = x$ and $CE = 18 - x$

$$\Rightarrow 2/3 = x/(18-x)$$

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$$3x = 36 - 2x$$

$$5x = 36 \text{ cm}$$

$$x = 36/5 \text{ cm}$$

$$x = 7.2 \text{ cm}$$

$$\therefore AE = 7.2 \text{ cm}$$

iv) If AD = 4 cm, AE = 8 cm, DB = x - 4 cm and EC = 3x - 19, find x.

Solution:

Given: AD = 4 cm, AE = 8 cm, DB = x - 4 and EC = 3x - 19

Required to find x.

By using Thales Theorem, [As DE \parallel BC]

$$AD/BD = AE/CE$$

Then, $4/(x - 4) = 8/(3x - 19)$

$$4(3x - 19) = 8(x - 4)$$

$$12x - 76 = 8(x - 4)$$

$$12x - 8x = -32 + 76$$

$$4x = 44 \text{ cm}$$

$$x = 11 \text{ cm}$$

v) If AD = 8 cm, AB = 12 cm and AE = 12 cm, find CE.

Solution:

Given: AD = 8 cm, AB = 12 cm, and AE = 12 cm.

Required to find CE,

By using Thales Theorem, [As DE \parallel BC]

$$AD/BD = AE/CE$$

$$8/4 = 12/CE$$

$$8 \times CE = 4 \times 12 \text{ cm}$$

$$CE = (4 \times 12)/8 \text{ cm}$$

$$CE = 48/8 \text{ cm}$$

$$\therefore CE = 6 \text{ cm}$$

vi) If AD = 4 cm, DB = 4.5 cm and AE = 8 cm, find AC.

Solution:

Given: AD = 4 cm, DB = 4.5 cm, AE = 8 cm

Required to find AC.

By using Thales Theorem, [As DE \parallel BC]

$$AD/BD = AE/CE$$

$$4/4.5 = 8/AC$$

$$AC = (4.5 \times 8)/4 \text{ cm}$$

$$\therefore AC = 9 \text{ cm}$$

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vii) If $AD = 2$ cm, $AB = 6$ cm and $AC = 9$ cm, find AE .

Solution:

Given: $AD = 2$ cm, $AB = 6$ cm and $AC = 9$ cm

Required to find AE .

$$DB = AB - AD = 6 - 2 = 4 \text{ cm}$$

By using Thales Theorem, [As $DE \parallel BC$]

$$AD/BD = AE/CE$$

$$2/4 = x/(9-x)$$

$$4x = 18 - 2x$$

$$6x = 18$$

$$x = 3 \text{ cm}$$

$$\therefore AE = 3 \text{ cm}$$

viii) If $AD/BD = 4/5$ and $EC = 2.5$ cm, Find AE .

Solution:

Given: $AD/BD = 4/5$ and $EC = 2.5$ cm

Required to find AE .

By using Thales Theorem, [As $DE \parallel BC$]

$$AD/BD = AE/CE$$

Then, $4/5 = AE/2.5$

$$\therefore AE = 4 \times 2.5/5 = 2 \text{ cm}$$

ix) If $AD = x$ cm, $DB = x - 2$ cm, $AE = x + 2$ cm, and $EC = x - 1$ cm, find the value of x .

Solution:

Given: $AD = x$, $DB = x - 2$, $AE = x + 2$ and $EC = x - 1$

Required to find the value of x .

By using Thales Theorem, [As $DE \parallel BC$]

$$AD/BD = AE/CE$$

$$\text{So, } x/(x-2) = (x+2)/(x-1)$$

$$x(x-1) = (x-2)(x+2)$$

$$x^2 - x - x^2 + 4 = 0$$

$$x = 4$$

x) If $AD = 8x - 7$ cm, $DB = 5x - 3$ cm, $AE = 4x - 3$ cm, and $EC = (3x - 1)$ cm, Find the value of x .

Solution:

Given: $AD = 8x - 7$, $DB = 5x - 3$, $AER = 4x - 3$ and $EC = 3x - 1$

Required to find x .

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By using Thales Theorem, [As $DE \parallel BC$]

$$AD/BD = AE/CE$$

$$(8x-7)/(5x-3) = (4x-3)/(3x-1)$$

$$(8x-7)(3x-1) = (5x-3)(4x-3)$$

$$24x^2 - 29x + 7 = 20x^2 - 27x + 9$$

$$4x^2 - 2x - 2 = 0$$

$$2(2x^2 - x - 1) = 0$$

$$2x^2 - x - 1 = 0$$

$$2x^2 - 2x + x - 1 = 0$$

$$2x(x-1) + 1(x-1) = 0$$

$$(x-1)(2x+1) = 0$$

$$\Rightarrow x = 1 \text{ or } x = -1/2$$

We know that the side of triangle can never be negative. Therefore, we take the positive value.

$$\therefore x = 1.$$

xi) If $AD = 4x - 3$, $AE = 8x - 7$, $BD = 3x - 1$, and $CE = 5x - 3$, find the value of x .

Solution:

Given: $AD = 4x - 3$, $BD = 3x - 1$, $AE = 8x - 7$ and $EC = 5x - 3$

Required to find x .

By using Thales Theorem, [As $DE \parallel BC$]

$$AD/BD = AE/CE$$

$$\text{So, } (4x-3)/(3x-1) = (8x-7)/(5x-3)$$

$$(4x-3)(5x-3) = (3x-1)(8x-7)$$

$$4x(5x-3) - 3(5x-3) = 3x(8x-7) - 1(8x-7)$$

$$20x^2 - 12x - 15x + 9 = 24x^2 - 29x + 7$$

$$20x^2 - 27x + 9 = 24x^2 - 29x + 7$$

$$\Rightarrow -4x^2 + 2x + 2 = 0$$

$$4x^2 - 2x - 2 = 0$$

$$4x^2 - 4x + 2x - 2 = 0$$

$$4x(x-1) + 2(x-1) = 0$$

$$(4x+2)(x-1) = 0$$

$$\Rightarrow x = 1 \text{ or } x = -2/4$$

We know that the side of triangle can never be negative. Therefore, we take the positive value.

$$\therefore x = 1$$

xii) If $AD = 2.5$ cm, $BD = 3.0$ cm, and $AE = 3.75$ cm, find the length of AC .

Solution:

Given: $AD = 2.5$ cm, $AE = 3.75$ cm and $BD = 3$ cm

Required to find AC .

By using Thales Theorem, [As $DE \parallel BC$]

$$AD/BD = AE/CE$$

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$$\begin{aligned}2.5/3 &= 3.75/CE \\2.5 \times CE &= 3.75 \times 3 \\CE &= 3.75 \times 3/2.5 \\CE &= 11.25/2.5 \\CE &= 4.5\end{aligned}$$

$$\begin{aligned}\text{Now, } AC &= 3.75 + 4.5 \\ \therefore AC &= 8.25 \text{ cm.}\end{aligned}$$

2. In a $\triangle ABC$, D and E are points on the sides AB and AC respectively. For each of the following cases show that $DE \parallel BC$:

i) $AB = 12 \text{ cm}$, $AD = 8 \text{ cm}$, $AE = 12 \text{ cm}$, and $AC = 18 \text{ cm}$.

Solution:

Required to prove $DE \parallel BC$.

We have,

$AB = 12 \text{ cm}$, $AD = 8 \text{ cm}$, $AE = 12 \text{ cm}$, and $AC = 18 \text{ cm}$. (Given)

So,

$$BD = AB - AD = 12 - 8 = 4 \text{ cm}$$

And,

$$CE = AC - AE = 18 - 12 = 6 \text{ cm}$$

It's seen that,

$$AD/BD = 8/4 = 1/2$$

$$AE/CE = 12/6 = 1/2$$

Thus,

$$AD/BD = AE/CE$$

So, by the converse of Thale's Theorem

We have,

$$DE \parallel BC.$$

Hence Proved.

ii) $AB = 5.6 \text{ cm}$, $AD = 1.4 \text{ cm}$, $AC = 7.2 \text{ cm}$, and $AE = 1.8 \text{ cm}$.

Solution:

Required to prove $DE \parallel BC$.

We have,

$AB = 5.6 \text{ cm}$, $AD = 1.4 \text{ cm}$, $AC = 7.2 \text{ cm}$, and $AE = 1.8 \text{ cm}$. (Given)

So,

$$BD = AB - AD = 5.6 - 1.4 = 4.2 \text{ cm}$$

And,

$$CE = AC - AE = 7.2 - 1.8 = 5.4 \text{ cm}$$

It's seen that,

$$AD/BD = 1.4/4.2 = 1/3$$

$$AE/CE = 1.8/5.4 = 1/3$$

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Thus,

$$AD/BD = AE/CE$$

So, by the converse of Thale's Theorem

We have,

$$DE \parallel BC.$$

Hence Proved.

iii) AB = 10.8 cm, BD = 4.5 cm, AC = 4.8 cm, and AE = 2.8 cm.

Solution:

Required to prove $DE \parallel BC$.

We have

$$AB = 10.8 \text{ cm, } BD = 4.5 \text{ cm, } AC = 4.8 \text{ cm, and } AE = 2.8 \text{ cm.}$$

So,

$$AD = AB - DB = 10.8 - 4.5 = 6.3$$

And,

$$CE = AC - AE = 4.8 - 2.8 = 2$$

It's seen that,

$$AD/BD = 6.3/4.5 = 2.8/2.0 = AE/CE = 7/5$$

So, by the converse of Thale's Theorem

We have,

$$DE \parallel BC.$$

Hence Proved.

iv) AD = 5.7 cm, BD = 9.5 cm, AE = 3.3 cm, and EC = 5.5 cm.

Solution:

Required to prove $DE \parallel BC$.

We have

$$AD = 5.7 \text{ cm, } BD = 9.5 \text{ cm, } AE = 3.3 \text{ cm, and } EC = 5.5 \text{ cm}$$

Now,

$$AD/BD = 5.7/9.5 = 3/5$$

And,

$$AE/CE = 3.3/5.5 = 3/5$$

Thus,

$$AD/BD = AE/CE$$

So, by the converse of Thale's Theorem

We have,

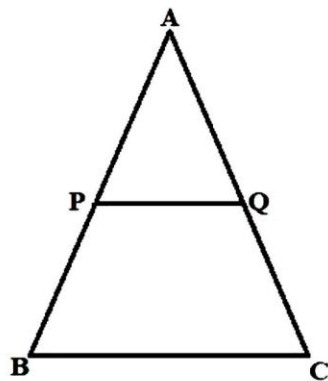
$$DE \parallel BC.$$

Hence Proved.

3. In a $\triangle ABC$, P and Q are the points on sides AB and AC respectively, such that $PQ \parallel BC$. If AP = 2.4 cm, AQ = 2 cm, QC = 3 cm and BC = 6 cm. Find AB and PQ.

R D Sharma Solutions For Class 10 Maths Chapter 4 - Triangles**Solution:**

Given: $\triangle ABC$, $AP = 2.4$ cm, $AQ = 2$ cm, $QC = 3$ cm, and $BC = 6$ cm. Also, $PQ \parallel BC$.
Required to find: AB and PQ .



By using Thales Theorem, we have [As it's given that $PQ \parallel BC$]

$$AP/PB = AQ/QC$$

$$2.4/PB = 2/3$$

$$2 \times PB = 2.4 \times 3$$

$$PB = (2.4 \times 3)/2 \text{ cm}$$

$$\Rightarrow PB = 3.6 \text{ cm}$$

Now finding, $AB = AP + PB$

$$AB = 2.4 + 3.6$$

$$\Rightarrow AB = 6 \text{ cm}$$

Now, considering $\triangle APQ$ and $\triangle ABC$

We have,

$$\angle A = \angle A$$

$$\angle APQ = \angle ABC \text{ (Corresponding angles are equal, } PQ \parallel BC \text{ and } AB \text{ being a transversal)}$$

Thus, $\triangle APQ$ and $\triangle ABC$ are similar to each other by AA criteria.

Now, we know that

Corresponding parts of similar triangles are proportional.

$$\Rightarrow AP/AB = PQ/BC$$

$$\Rightarrow PQ = (AP/AB) \times BC$$
$$= (2.4/6) \times 6 = 2.4$$

$$\therefore PQ = 2.4 \text{ cm.}$$

4. In a $\triangle ABC$, D and E are points on AB and AC respectively, such that $DE \parallel BC$. If $AD = 2.4$ cm, $AE = 3.2$ cm, $DE = 2$ cm and $BC = 5$ cm. Find BD and CE .

Solution:

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Given: $\triangle ABC$ such that $AD = 2.4$ cm, $AE = 3.2$ cm, $DE = 2$ cm and $BE = 5$ cm. Also $DE \parallel BC$.
Required to find: BD and CE .

As $DE \parallel BC$, AB is transversal,
 $\angle APQ = \angle ABC$ (corresponding angles)

As $DE \parallel BC$, AC is transversal,
 $\angle AED = \angle ACB$ (corresponding angles)

In $\triangle ADE$ and $\triangle ABC$,
 $\angle ADE = \angle ABC$
 $\angle AED = \angle ACB$
 $\therefore \triangle ADE \sim \triangle ABC$ (AA similarity criteria)

Now, we know that
Corresponding parts of similar triangles are proportional.

$$\begin{aligned}\Rightarrow \quad AD/AB &= AE/AC = DE/BC \\ AD/AB &= DE/BC \\ 2.4/(2.4 + DB) &= 2/5 \text{ [Since, } AB = AD + DB\text{]} \\ 2.4 + DB &= 6 \\ DB &= 6 - 2.4 \\ DB &= 3.6 \text{ cm}\end{aligned}$$

$$\begin{aligned}\text{In the same way,} \\ \Rightarrow \quad AE/AC &= DE/BC \\ 3.2/(3.2 + EC) &= 2/5 \text{ [Since } AC = AE + EC\text{]} \\ 3.2 + EC &= 8 \\ EC &= 8 - 3.2 \\ EC &= 4.8 \text{ cm}\end{aligned}$$

$$\therefore BD = 3.6 \text{ cm and } CE = 4.8 \text{ cm.}$$

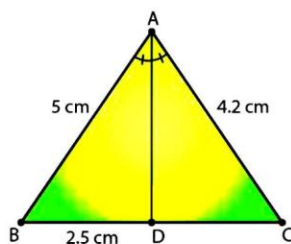
**R D Sharma Solutions For Class 10 Maths Chapter 4 -
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1. In a $\triangle ABC$, AD is the bisector of $\angle A$, meeting side BC at D.**(i) if $BD = 2.5$ cm, $AB = 5$ cm, and $AC = 4.2$ cm, find DC.****Solution:**

Given: $\triangle ABC$ and AD bisects $\angle A$, meeting side BC at D. And $BD = 2.5$ cm, $AB = 5$ cm, and $AC = 4.2$ cm.

Required to find: DC



Since, AD is the bisector of $\angle A$ meeting side BC at D in $\triangle ABC$

$$\Rightarrow \frac{AB}{AC} = \frac{BD}{DC}$$

$$\frac{5}{4.2} = \frac{2.5}{DC}$$

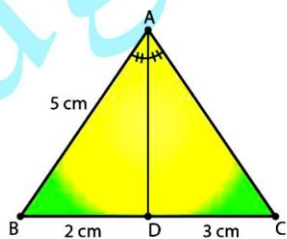
$$5DC = 2.5 \times 4.2$$

$$\therefore DC = 2.1 \text{ cm}$$

(ii) if $BD = 2$ cm, $AB = 5$ cm, and $DC = 3$ cm, find AC.**Solution:**

Given: $\triangle ABC$ and AD bisects $\angle A$, meeting side BC at D. And $BD = 2$ cm, $AB = 5$ cm, and $DC = 3$ cm.

Required to find: AC



Since, AD is the bisector of $\angle A$ meeting side BC at D in $\triangle ABC$

$$\Rightarrow \frac{AB}{AC} = \frac{BD}{DC}$$

$$\frac{5}{AC} = \frac{2}{3}$$

$$2AC = 5 \times 3$$

$$\therefore AC = 7.5 \text{ cm}$$

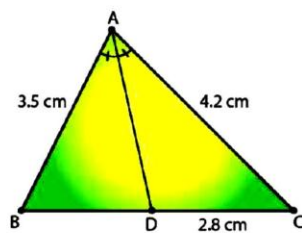
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(iii) if $AB = 3.5$ cm, $AC = 4.2$ cm, and $DC = 2.8$ cm, find BD .

Solution:

Given: $\triangle ABC$ and AD bisects $\angle A$, meeting side BC at D . And $AB = 3.5$ cm, $AC = 4.2$ cm, and $DC = 2.8$ cm.

Required to find: BD



Since, AD is the bisector of $\angle A$ meeting side BC at D in $\triangle ABC$

$$\Rightarrow \frac{AB}{AC} = \frac{BD}{DC}$$

$$\frac{3.5}{4.2} = \frac{BD}{2.8}$$

$$4.2 \times BD = 3.5 \times 2.8$$

$$BD = \frac{7}{3}$$

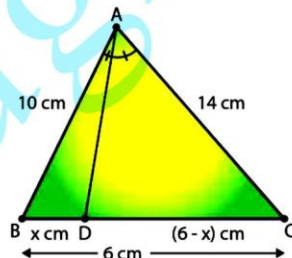
$$\therefore BD = 2.3 \text{ cm}$$

(iv) if $AB = 10$ cm, $AC = 14$ cm, and $BC = 6$ cm, find BD and DC .

Solution:

Given: In $\triangle ABC$, AD is the bisector of $\angle A$ meeting side BC at D . And, $AB = 10$ cm, $AC = 14$ cm, and $BC = 6$ cm

Required to find: BD and DC .



Since, AD is bisector of $\angle A$

We have,

$$\frac{AB}{AC} = \frac{BD}{DC} \quad (\text{AD is bisector of } \angle A \text{ and side BC})$$

$$\text{Then, } \frac{10}{14} = \frac{x}{(6 - x)}$$

$$14x = 60 - 6x$$

$$20x = 60$$

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$$x = 60/20$$

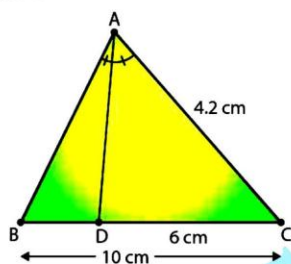
$$\therefore BD = 3 \text{ cm and } DC = (6 - 3) = 3 \text{ cm.}$$

(v) if $AC = 4.2 \text{ cm}$, $DC = 6 \text{ cm}$, and $BC = 10 \text{ cm}$, find AB .

Solution:

Given: $\triangle ABC$ and AD bisects $\angle A$, meeting side BC at D . And $AC = 4.2 \text{ cm}$, $DC = 6 \text{ cm}$, and $BC = 10 \text{ cm}$.

Required to find: AB



Since, AD is the bisector of $\angle A$ meeting side BC at D in $\triangle ABC$

$$\Rightarrow AB/AC = BD/DC$$

$$AB/4.2 = BD/6$$

We know that,

$$BD = BC - DC = 10 - 6 = 4 \text{ cm}$$

$$\Rightarrow AB/4.2 = 4/6$$

$$AB = (4 \times 4.2)/3$$

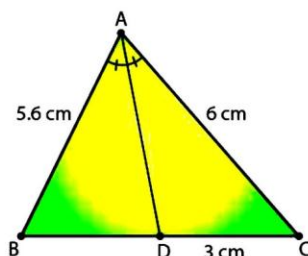
$$\therefore AB = 2.8 \text{ cm}$$

(vi) if $AB = 5.6 \text{ cm}$, $AC = 6 \text{ cm}$, and $DC = 3 \text{ cm}$, find BC .

Solution:

Given: $\triangle ABC$ and AD bisects $\angle A$, meeting side BC at D . And $AB = 5.6 \text{ cm}$, $AC = 6 \text{ cm}$, and $DC = 3 \text{ cm}$.

Required to find: BC

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Since, AD is the bisector of $\angle A$ meeting side BC at D in $\triangle ABC$

$$\Rightarrow \frac{AB}{AC} = \frac{BD}{DC}$$

$$\frac{5.6}{6} = \frac{BD}{3}$$

$$BD = \frac{5.6}{2} = 2.8 \text{ cm}$$

And, we know that,

$$BD = BC - DC$$

$$2.8 = BC - 3$$

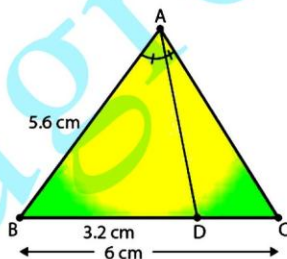
$$\therefore BC = 5.8 \text{ cm}$$

(vii) if $AB = 5.6 \text{ cm}$, $BC = 6 \text{ cm}$, and $BD = 3.2 \text{ cm}$, find AC.

Solution:

Given: $\triangle ABC$ and AD bisects $\angle A$, meeting side BC at D. And $AB = 5.6 \text{ cm}$, $BC = 6 \text{ cm}$, and $BD = 3.2 \text{ cm}$.

Required to find: AC



Since, AD is the bisector of $\angle A$ meeting side BC at D in $\triangle ABC$

$$\Rightarrow \frac{AB}{AC} = \frac{BD}{DC}$$

$$\frac{5.6}{AC} = \frac{3.2}{DC}$$

And, we know that

$$BD = BC - DC$$

$$3.2 = 6 - DC$$

$$\therefore DC = 2.8 \text{ cm}$$

$$\Rightarrow \frac{5.6}{AC} = \frac{3.2}{2.8}$$

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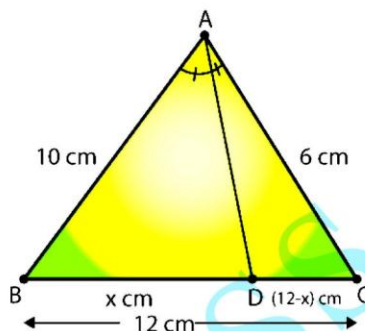
$$AC = (5.6 \times 2.8) / 3.2$$
$$\therefore AC = 4.9 \text{ cm}$$

(viii) if $AB = 10 \text{ cm}$, $AC = 6 \text{ cm}$, and $BC = 12 \text{ cm}$, find BD and DC .

Solution:

Given: $\triangle ABC$ and AD bisects $\angle A$, meeting side BC at D . $AB = 10 \text{ cm}$, $AC = 6 \text{ cm}$, and $BC = 12 \text{ cm}$.

Required to find: DC



Since, AD is the bisector of $\angle A$ meeting side BC at D in $\triangle ABC$

$$\Rightarrow AB/AC = BD/DC$$

$$10/6 = BD/DC \dots\dots\dots (i)$$

And, we know that

$$BD = BC - DC = 12 - DC$$

Let $BD = x$,

$$\Rightarrow DC = 12 - x$$

Thus (i) becomes,

$$10/6 = x/(12 - x)$$

$$5(12 - x) = 3x$$

$$60 - 5x = 3x$$

$$\therefore x = 60/8 = 7.5$$

Hence, $DC = 12 - 7.5 = 4.5 \text{ cm}$ and $BD = 7.5 \text{ cm}$

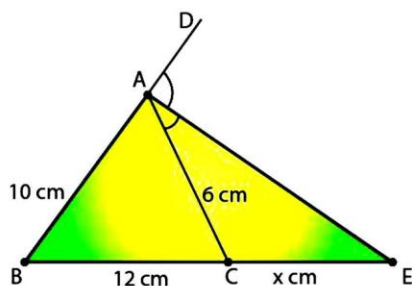
2. In figure 4.57, AE is the bisector of the exterior $\angle CAD$ meeting BC produced in E . If $AB = 10 \text{ cm}$, $AC = 6 \text{ cm}$, and $BC = 12 \text{ cm}$, find CE .

Solution:

Given: AE is the bisector of the exterior $\angle CAD$ and $AB = 10 \text{ cm}$, $AC = 6 \text{ cm}$, and $BC = 12 \text{ cm}$.

Required to find: CE

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Since AE is the bisector of the exterior $\angle CAD$.

$$BE / CE = AB / AC$$

Let's take CE as x.

So, we have

$$BE / CE = AB / AC$$

$$(12+x) / x = 10 / 6$$

$$6x + 72 = 10x$$

$$10x - 6x = 72$$

$$4x = 72$$

$$\therefore x = 18$$

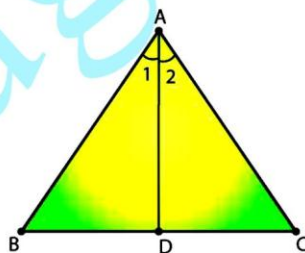
Therefore, CE = 18 cm.

3. In fig. 4.58, $\triangle ABC$ is a triangle such that $AB/AC = BD/DC$, $\angle B = 70^\circ$, $\angle C = 50^\circ$, find $\angle BAD$.

Solution:

Given: $\triangle ABC$ such that $AB/AC = BD/DC$, $\angle B = 70^\circ$ and $\angle C = 50^\circ$

Required to find: $\angle BAD$



We know that,

In $\triangle ABC$,

$$\angle A = 180 - (70 + 50)$$

$$= 180 - 120$$

$$= 60^\circ$$

[Angle sum property of a triangle]

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Since,

$$AB/AC = BD/DC,$$

AD is the angle bisector of angle $\angle A$.

Thus,

$$\angle BAD = \angle A/2 = 60/2 = 30^\circ$$

R D Sharma Solutions For Class 10 Maths Chapter 4 - Triangles

Exercise 4.4

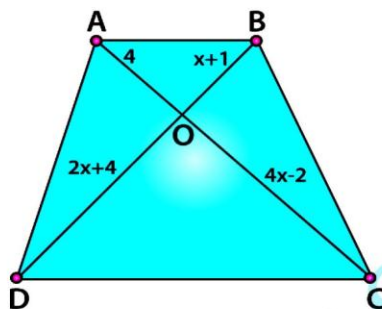
Page No: 4.37

1. (i) In fig. 4.70, if $AB \parallel CD$, find the value of x .

Solution:

It's given that $AB \parallel CD$.

Required to find the value of x .



We know that,

Diagonals of a parallelogram bisect each other.

So,

$$AO/CO = BO/DO$$

$$\Rightarrow 4/(4x-2) = (x+1)/(2x+4)$$

$$4(2x+4) = (4x-2)(x+1)$$

$$8x+16 = x(4x-2) + 1(4x-2)$$

$$8x+16 = 4x^2 - 2x + 4x - 2$$

$$-4x^2 + 8x + 16 + 2 - 2x = 0$$

$$-4x^2 + 6x + 8 = 0$$

$$4x^2 - 6x - 18 = 0$$

$$4x^2 - 12x + 6x - 18 = 0$$

$$4x(x-3) + 6(x-3) = 0$$

$$(4x+6)(x-3) = 0$$

$$\therefore x = -6/4 \text{ or } x = 3$$

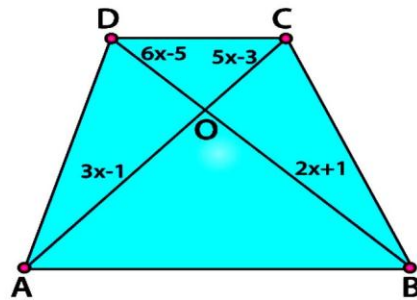
(ii) In fig. 4.71, if $AB \parallel CD$, find the value of x .

Solution:

It's given that $AB \parallel CD$.

Required to find the value of x .

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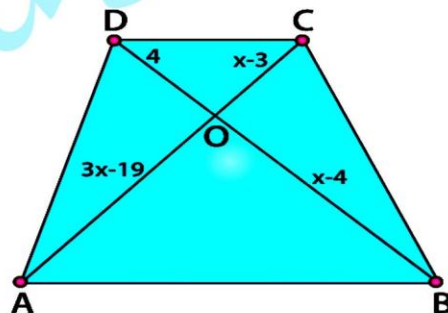


We know that,
Diagonals of a parallelogram bisect each other
So,

$$\begin{aligned}
 &AO/CO = BO/DO \\
 \Rightarrow &(6x-5)/(2x+1) = (5x-3)/(3x-1) \\
 &(6x-5)(3x-1) = (2x+1)(5x-3) \\
 &3x(6x-5) - 1(6x-5) = 2x(5x-3) + 1(5x-3) \\
 &18x^2 - 10x^2 - 21x + 5 + x + 3 = 0 \\
 &8x^2 - 16x - 4x + 8 = 0 \\
 &8x(x-2) - 4(x-2) = 0 \\
 &(8x-4)(x-2) = 0 \\
 &x = 4/8 = 1/2 \text{ or } x = -2 \\
 &\therefore x = 1/2
 \end{aligned}$$

(iii) In fig. 4.72, if $AB \parallel CD$. If $OA = 3x - 19$, $OB = x - 4$, $OC = x - 3$ and $OD = 4$, find x .
Solution:

It's given that $AB \parallel CD$.
Required to find the value of x .



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We know that,

Diagonals of a parallelogram bisect each other

So,

$$AO/CO = BO/DO$$

$$(3x - 19)/(x - 3) = (x - 4)/4$$

$$4(3x - 19) = (x - 3)(x - 4)$$

$$12x - 76 = x(x - 4) - 3(x - 4)$$

$$12x - 76 = x^2 - 4x - 3x + 12$$

$$-x^2 + 7x - 12 + 12x - 76 = 0$$

$$-x^2 + 19x - 88 = 0$$

$$x^2 - 19x + 88 = 0$$

$$x^2 - 11x - 8x + 88 = 0$$

$$x(x - 11) - 8(x - 11) = 0$$

$$\therefore x = 11 \text{ or } x = 8$$

**R D Sharma Solutions For Class 10 Maths Chapter 4 -
Triangles****Exercise 4.5**

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1. In fig. 4.136, $\triangle ACB \sim \triangle APQ$. If $BC = 8$ cm, $PQ = 4$ cm, $BA = 6.5$ cm and $AP = 2.8$ cm, find CA and AQ .

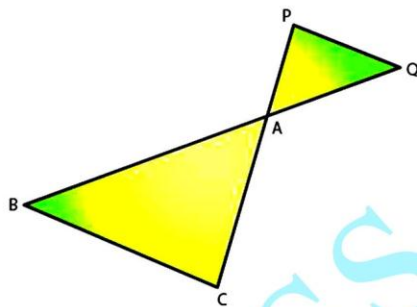
Solution:

Given,

$$\triangle ACB \sim \triangle APQ$$

$$BC = 8 \text{ cm}, PQ = 4 \text{ cm}, BA = 6.5 \text{ cm and } AP = 2.8 \text{ cm}$$

Required to find: CA and AQ



We know that,

$$\triangle ACB \sim \triangle APQ \quad [\text{given}]$$

$$BA/AQ = CA/AP = BC/PQ$$

[Corresponding Parts of Similar Triangles]

So,

$$6.5/AQ = 8/4$$

$$AQ = (6.5 \times 4)/8$$

$$AQ = 3.25 \text{ cm}$$

Similarly, as

$$CA/AP = BC/PQ$$

$$CA/2.8 = 8/4$$

$$CA = 2.8 \times 2$$

$$CA = 5.6 \text{ cm}$$

Hence, $CA = 5.6$ cm and $AQ = 3.25$ cm.

2. In fig.4.137, $AB \parallel QR$, find the length of PB .

Solution:

Given,

$$\triangle PQR, AB \parallel QR \text{ and}$$

$$AB = 3 \text{ cm}, QR = 9 \text{ cm and } PR = 6 \text{ cm}$$

Required to find: PB

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In $\triangle AXY$ and $\triangle ABC$

We have,

$$\angle A = \angle A$$

[Common]

$$\angle AXY = \angle ABC$$

[Corresponding angles as $AB \parallel QR$ with PQ as the transversal]

$$\Rightarrow \triangle AXY \sim \triangle ABC$$

[By AA similarity criteria]

Hence,

$$XY/BC = AX/AB \quad [\text{Corresponding Parts of Similar Triangles are proportional}]$$

We know that,

$$(AB = AX + XB = 1 + 3 = 4)$$

$$XY/6 = 1/4$$

$$XY/1 = 6/4$$

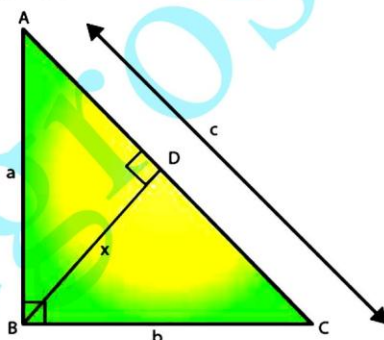
Therefore, $XY = 1.5$ cm

4. In a right-angled triangle with sides a and b and hypotenuse c , the altitude drawn on the hypotenuse is x . Prove that $ab = cx$.

Solution:

Consider $\triangle ABC$ to be a right angle triangle having sides a and b and hypotenuse c . Let BD be the altitude drawn on the hypotenuse AC .

Required to prove: $ab = cx$



We know that,

In $\triangle ACB$ and $\triangle CDB$

$$\angle B = \angle B$$

[Common]

$$\angle ACB = \angle CDB = 90^\circ$$

$$\Rightarrow \triangle ACB \sim \triangle CDB$$

[By AA similarity criteria]

Hence,

$$AB/BD = AC/BC$$

[Corresponding Parts of Similar Triangles are proportional]

$$a/x = c/b$$

$$\Rightarrow xc = ab$$

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Therefore, $ab = cx$

5. In fig. 4.139, $\angle ABC = 90^\circ$ and $BD \perp AC$. If $BD = 8$ cm, and $AD = 4$ cm, find CD .

Solution:

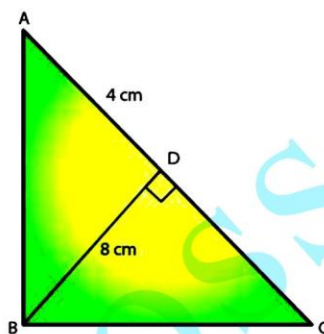
Given,

$$\angle ABC = 90^\circ \text{ and } BD \perp AC$$

$$BD = 8 \text{ cm}$$

$$AD = 4 \text{ cm}$$

Required to find: CD .



We know that,

ABC is a right angled triangle and $BD \perp AC$.

Then, $\triangle DBA \sim \triangle DCB$

[By AA similarity]

$$BD/CD = AD/BD$$

$$BD^2 = AD \times DC$$

$$(8)^2 = 4 \times DC$$

$$DC = 64/4 = 16 \text{ cm}$$

Therefore, $CD = 16$ cm

6. In fig. 4.140, $\angle ABC = 90^\circ$ and $BD \perp AC$. If $AC = 5.7$ cm, $BD = 3.8$ cm and $CD = 5.4$ cm, Find BC .

Solution:

Given:

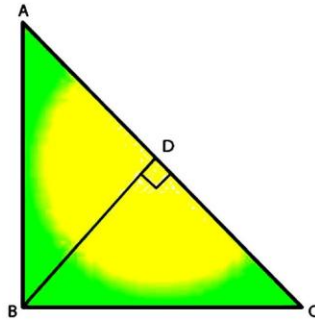
$$BD \perp AC$$

$$AC = 5.7 \text{ cm, } BD = 3.8 \text{ cm and } CD = 5.4 \text{ cm}$$

$$\angle ABC = 90^\circ$$

Required to find: BC

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We know that,

$$\triangle ABC \sim \triangle BDC \quad [\text{By AA similarity}]$$

$$\angle BCA = \angle DCA = 90^\circ$$

$$\angle ABC = \angle BDC \quad [\text{Common}]$$

Thus,

$$\frac{AB}{BD} = \frac{BC}{CD} \quad [\text{Corresponding Parts of Similar Triangles are proportional}]$$

$$5.7 / 3.8 = BC / 5.4$$

$$BC = (5.7 \times 5.4) / 3.8 = 8.1$$

Therefore, $BC = 8.1$ cm

7. In the fig.4.141 given, $DE \parallel BC$ such that $AE = (1/4)AC$. If $AB = 6$ cm, find AD .

Solution:

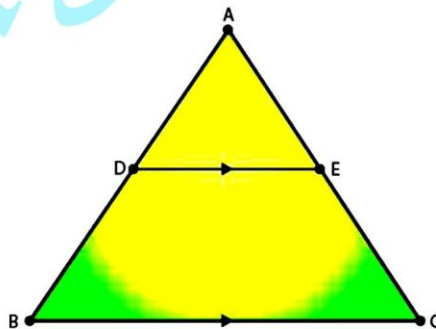
Given:

$$DE \parallel BC$$

$$AE = (1/4)AC$$

$$AB = 6 \text{ cm.}$$

Required to find: AD .



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In $\triangle ADE$ and $\triangle ABC$

We have,

$$\angle A = \angle A$$

[Common]

$$\angle ADE = \angle ABC$$

[Corresponding angles as $AB \parallel QR$ with PQ as the transversal]

$$\Rightarrow \triangle ADE \sim \triangle ABC$$

[By AA similarity criteria]

Then,

$$AD/AB = AE/AC \quad [\text{Corresponding Parts of Similar Triangles are proportional}]$$

$$AD/6 = 1/4$$

$$4 \times AD = 6$$

$$AD = 6/4$$

Therefore, $AD = 1.5$ cm

8. In the fig.4.142 given, if $AB \perp BC$, $DC \perp BC$, and $DE \perp AC$, prove that $\triangle CED \sim \triangle ABC$

Solution:

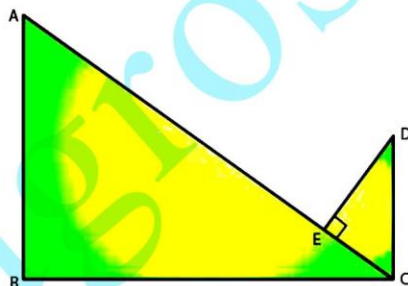
Given:

$$AB \perp BC,$$

$$DC \perp BC,$$

$$DE \perp AC$$

Required to prove: $\triangle CED \sim \triangle ABC$



We know that,

From $\triangle ABC$ and $\triangle CED$

$$\angle B = \angle E = 90^\circ$$

[given]

$$\angle BAC = \angle ECD$$

[alternate angles since, $AB \parallel DC$ with BC as transversal]

Therefore, $\triangle CED \sim \triangle ABC$

[AA similarity]

9. Diagonals AC and BD of a trapezium ABCD with $AB \parallel DC$ intersect each other at the point O.

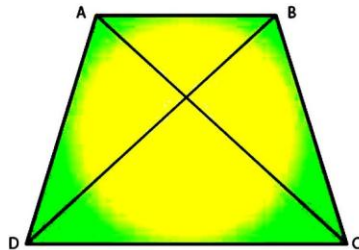
Using similarity criterion for two triangles, show that $OA/OC = OB/OD$

Solution:

Given: OC is the point of intersection of AC and BD in the trapezium ABCD, with $AB \parallel DC$.

Required to prove: $OA/OC = OB/OD$

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We know that,

In $\triangle AOB$ and $\triangle COD$

$$\angle AOB = \angle COD$$

[Vertically Opposite Angles]

$$\angle OAB = \angle OCD$$

[Alternate angles]

Then, $\triangle AOB \sim \triangle COD$

Therefore, $OA/OC = OB/OD$

[Corresponding sides are proportional]

10. If $\triangle ABC$ and $\triangle AMP$ are two right triangles, right angled at B and M, respectively such that $\angle MAP = \angle BAC$. Prove that

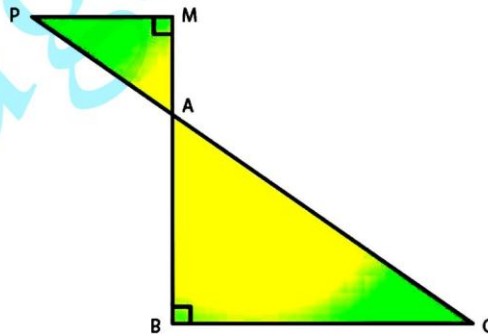
(i) $\triangle ABC \sim \triangle AMP$

(ii) $CA/PA = BC/MP$

Solution:

(i) Given:

$\triangle ABC$ and $\triangle AMP$ are the two right triangles.



We know that,

$$\angle AMP = \angle B = 90^\circ$$

$$\angle MAP = \angle BAC$$

[Vertically Opposite Angles]

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$$\Rightarrow \triangle ABC \sim \triangle AMP \quad [\text{AA similarity}]$$

(ii) Since, $\triangle ABC \sim \triangle AMP$
 $CA/PA = BC/MP$ [Corresponding sides are proportional]
 Hence proved.

11. A vertical stick 10 cm long casts a shadow 8 cm long. At the same time, a tower casts a shadow 30 m long. Determine the height of the tower.

Solution:

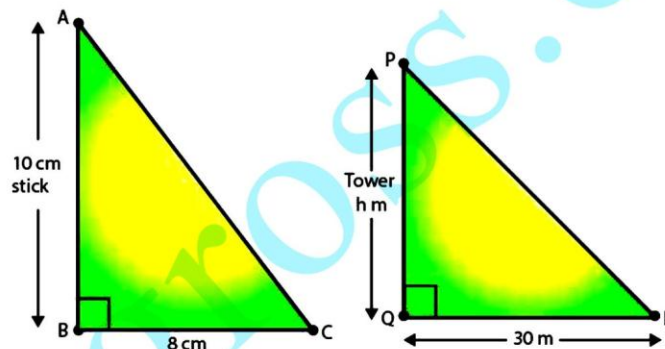
Given:

Length of stick = 10 cm

Length of the stick's shadow = 8 cm

Length of the tower's shadow = 30 m = 3000 cm

Required to find: the height of the tower = PQ.



In $\triangle ABC \sim \triangle PQR$

$\angle ABC = \angle PQR = 90^\circ$

$\angle ACB = \angle PRQ$

$\Rightarrow \triangle ABC \sim \triangle PQR$

[Angular Elevation of Sun is same for a particular instant of time]

[By AA similarity]

So, we have

$$AB/BC = PQ/QR$$

[Corresponding sides are proportional]

$$10/8 = PQ/3000$$

$$PQ = (3000 \times 10)/8$$

$$PQ = 30000/8$$

$$PQ = 3750/100$$

Therefore, $PQ = 37.5$ m

12. In fig.4.143, $\angle A = \angle CED$, prove that $\triangle CAB \sim \triangle CED$. Also find the value of x.

Solution:

Therefore, $x = 6$ cm

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Exercise 4.6

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1. Triangles ABC and DEF are similar.

(i) If area of $(\triangle ABC) = 16 \text{ cm}^2$, area $(\triangle DEF) = 25 \text{ cm}^2$ and $BC = 2.3 \text{ cm}$, find EF.

(ii) If area $(\triangle ABC) = 9 \text{ cm}^2$, area $(\triangle DEF) = 64 \text{ cm}^2$ and $DE = 5.1 \text{ cm}$, find AB.

(iii) If $AC = 19 \text{ cm}$ and $DF = 8 \text{ cm}$, find the ratio of the area of two triangles.

(iv) If area of $(\triangle ABC) = 36 \text{ cm}^2$, area $(\triangle DEF) = 64 \text{ cm}^2$ and $DE = 6.2 \text{ cm}$, find AB.

(v) If $AB = 1.2 \text{ cm}$ and $DE = 1.4 \text{ cm}$, find the ratio of the area of two triangles.

Solutions:

As we know that, the ratio of areas of two similar triangles is equal to the ratio of squares of their corresponding sides, we get

$$(i) \quad \frac{\text{ar}\triangle ABC}{\text{ar}\triangle DEF} = \left(\frac{BC}{EF}\right)^2 \quad \frac{16}{25} = \left(\frac{2.3}{EF}\right)^2 \quad \frac{4}{5} = \frac{2.3}{EF}$$

Therefore, $EF = 2.875 \text{ cm}$

$$(ii) \quad \frac{\text{ar}\triangle ABC}{\text{ar}\triangle DEF} = \left(\frac{AB}{DE}\right)^2 \quad \frac{9}{64} = \left(\frac{AB}{5.1}\right)^2 \quad \frac{3}{8} = \frac{AB}{5.1}$$

Therefore, $AB = 1.9125 \text{ cm}$

$$(iii) \quad \frac{\text{ar}\triangle ABC}{\text{ar}\triangle DEF} = \left(\frac{AC}{DF}\right)^2 \quad \frac{\text{ar}\triangle ABC}{\text{ar}\triangle DEF} = \left(\frac{19}{8}\right)^2 \quad \frac{\text{ar}\triangle ABC}{\text{ar}\triangle DEF} = \left(\frac{361}{64}\right)$$

Therefore, the ratio of the areas of the two triangles are 361: 64

$$(iv) \quad \frac{\text{ar}\triangle ABC}{\text{ar}\triangle DEF} = \left(\frac{AB}{DE}\right)^2 \quad \frac{36}{64} = \left(\frac{AB}{6.2}\right)^2 \quad \frac{6}{8} = \frac{AB}{6.2}$$

Therefore, $AB = 4.65 \text{ cm}$

$$(v) \quad \frac{\text{ar}\triangle ABC}{\text{ar}\triangle DEF} = \left(\frac{AB}{DE}\right)^2 \quad \frac{\text{ar}\triangle ABC}{\text{ar}\triangle DEF} = \left(\frac{1.2}{1.4}\right)^2 \quad \frac{\text{ar}\triangle ABC}{\text{ar}\triangle DEF} = \left(\frac{36}{49}\right)$$

Therefore, the ratio of the areas of the two triangles are 36: 49

2. In the fig 4.178, $\triangle ACB \sim \triangle APQ$. If $BC = 10 \text{ cm}$, $PQ = 5 \text{ cm}$, $BA = 6.5 \text{ cm}$, $AP = 2.8 \text{ cm}$, find CA and AQ. Also, find the area $(\triangle ACB)$: area $(\triangle APQ)$.

Solution:

Given:

$\triangle ACB$ is similar to $\triangle APQ$

$BC = 10 \text{ cm}$

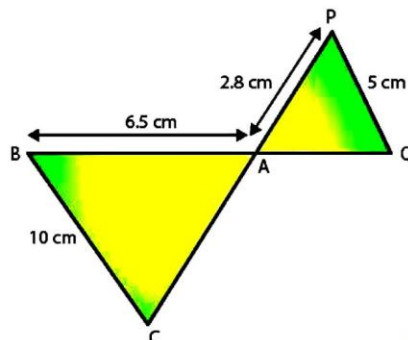
$PQ = 5 \text{ cm}$

$BA = 6.5 \text{ cm}$

$AP = 2.8 \text{ cm}$

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Required to Find: CA, AQ and that the area ($\triangle ACB$): area ($\triangle APQ$).



Since, $\triangle ACB \sim \triangle APQ$

We know that,

$$AB/AQ = BC/PQ = AC/AP \text{ [Corresponding Parts of Similar Triangles]}$$

$$AB/AQ = BC/PQ$$

$$6.5/AQ = 10/5$$

$$\Rightarrow AQ = 3.25 \text{ cm}$$

Similarly,

$$BC/PQ = CA/AP$$

$$CA/2.8 = 10/5$$

$$\Rightarrow CA = 5.6 \text{ cm}$$

Next,

Since the ratio of areas of two similar triangles is equal to the ratio of squares of their corresponding sides, we have,

$$\text{ar}(\triangle ACB) : \text{ar}(\triangle APQ) = (BC/PQ)^2$$

$$= (10/5)^2$$

$$= (2/1)^2$$

$$= 4/1$$

Therefore, the ratio is 4:1.

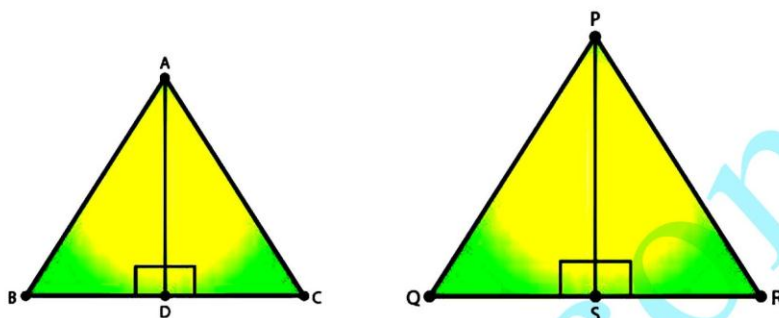
3. The areas of two similar triangles are 81 cm^2 and 49 cm^2 respectively. Find the ratio of their corresponding heights. What is the ratio of their corresponding medians?

Solution:

Given: The areas of two similar triangles are 81 cm^2 and 49 cm^2 .

Required to find: The ratio of their corresponding heights and the ratio of their corresponding medians.

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Let's consider the two similar triangles as ΔABC and ΔPQR , AD and PS be the altitudes of ΔABC and ΔPQR respectively.

So,

By area of similar triangle theorem, we have

$$\text{ar}(\Delta ABC) / \text{ar}(\Delta PQR) = AB^2 / PQ^2$$

$$\Rightarrow 81 / 49 = AB^2 / PQ^2$$

$$\Rightarrow 9 / 7 = AB / PQ$$

In ΔABD and ΔPQS

$$\angle B = \angle Q$$

[Since $\Delta ABC \sim \Delta PQR$]

$$\angle ABD = \angle PSQ = 90^\circ$$

$$\Rightarrow \Delta ABD \sim \Delta PQS$$

[By AA similarity]

Hence, as the corresponding parts of similar triangles are proportional, we have

$$AB / PQ = AD / PS$$

Therefore,

$$AD / PS = 9 / 7 \text{ (Ratio of altitudes)}$$

Similarly,

The ratio of two similar triangles is equal to the ratio of the squares of their corresponding medians also.

Thus, ratio of altitudes = Ratio of medians = $9 / 7$

4. The areas of two similar triangles are 169 cm^2 and 121 cm^2 respectively. If the longest side of the larger triangle is 26 cm , find the longest side of the smaller triangle.

Solution:

Given:

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The area of two similar triangles is 169cm^2 and 121cm^2 .

The longest side of the larger triangle is 26cm .

Required to find: the longest side of the smaller triangle

Let the longer side of the smaller triangle = x

We know that, the ratio of areas of two similar triangles is equal to the ratio of squares of their corresponding sides, we have

$$\frac{\text{ar}(\text{larger triangle})}{\text{ar}(\text{smaller triangle})} = \left(\frac{\text{side of the larger triangle}}{\text{side of the smaller triangle}}\right)^2$$
$$= 169/121$$

Taking square roots of LHS and RHS, we get

$$= 13/11$$

Since, sides of similar triangles are proportional, we can say

$$3/11 = (\text{longer side of the larger triangle}) / (\text{longer side of the smaller triangle})$$

$$\Rightarrow 13/11 = 26/x$$

$$x = 22$$

Therefore, the longest side of the smaller triangle is 22 cm .

5. The area of two similar triangles are 25 cm^2 and 36 cm^2 respectively. If the altitude of the first triangle is 2.4 cm , find the corresponding altitude of the other.

Solution:

Given: The area of two similar triangles are 25 cm^2 and 36 cm^2 respectively, the altitude of the first triangle is 2.4 cm

Required to find: the altitude of the second triangle

We know that the ratio of areas of two similar triangles is equal to the ratio of squares of their corresponding altitudes, we have

$$\Rightarrow \frac{\text{ar}(\text{triangle1})}{\text{ar}(\text{triangle2})} = \left(\frac{\text{altitude1}}{\text{altitude2}}\right)^2$$

$$\Rightarrow \frac{25}{36} = \frac{(2.4)^2}{(\text{altitude2})^2}$$

Taking square roots of LHS and RHS, we get

$$5/6 = 2.4/\text{altitude2}$$

$$\Rightarrow \text{altitude2} = (2.4 \times 6)/5 = 2.88\text{cm}$$

Therefore, the altitude of the second triangle is 2.88cm .

6. The corresponding altitudes of two similar triangles are 6 cm and 9 cm respectively. Find the ratio of their areas.

Solution:

Given:

The corresponding altitudes of two similar triangles are 6 cm and 9 cm .

Required to find: Ratio of areas of the two similar triangles

We know that the ratio of areas of two similar triangles is equal to the ratio of squares of their

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corresponding altitudes, we have

$$\begin{aligned}\frac{\text{ar}(\text{triangle1})}{\text{ar}(\text{triangle2})} &= \left(\frac{\text{altitude1}}{\text{altitude2}}\right)^2 = \left(\frac{6}{9}\right)^2 \\ &= \frac{36}{81} \\ &= \frac{4}{9}\end{aligned}$$

Therefore, the ratio of the areas of two triangles = 4: 9.

7. ABC is a triangle in which $\angle A = 90^\circ$, $AN \perp BC$, $BC = 12$ cm and $AC = 5$ cm. Find the ratio of the areas of $\triangle ANC$ and $\triangle ABC$.

Solution:

Given:

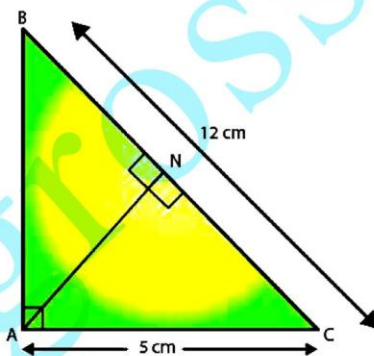
Given,

$\triangle ABC$, $\angle A = 90^\circ$, $AN \perp BC$

$BC = 12$ cm

$AC = 5$ cm.

Required to find: $\text{ar}(\triangle ANC) / \text{ar}(\triangle ABC)$.



We have,

In $\triangle ANC$ and $\triangle ABC$,

$\angle ACN = \angle ACB$

[Common]

$\angle A = \angle ANC$

[each 90°]

$\Rightarrow \triangle ANC \sim \triangle ABC$

[AA similarity]

Since the ratio of areas of two similar triangles is equal to the ratio of squares of their corresponding sides, we get have

$$\frac{\text{ar}(\triangle ANC)}{\text{ar}(\triangle ABC)} = \left(\frac{AC}{BC}\right)^2 = \left(\frac{5}{12}\right)^2 = \frac{25}{144}$$

Therefore, $\text{ar}(\triangle ANC) / \text{ar}(\triangle ABC) = 25:144$

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8. In Fig 4.179, $DE \parallel BC$

(i) If $DE = 4\text{m}$, $BC = 6\text{ cm}$ and $\text{Area}(\triangle ADE) = 16\text{cm}^2$, find the area of $\triangle ABC$.

(ii) If $DE = 4\text{cm}$, $BC = 8\text{ cm}$ and $\text{Area}(\triangle ADE) = 25\text{cm}^2$, find the area of $\triangle ABC$.

(iii) If $DE:BC = 3:5$. Calculate the ratio of the areas of $\triangle ADE$ and the trapezium $BCED$.

Solution:

Given,

$DE \parallel BC$.

In $\triangle ADE$ and $\triangle ABC$

We know that,

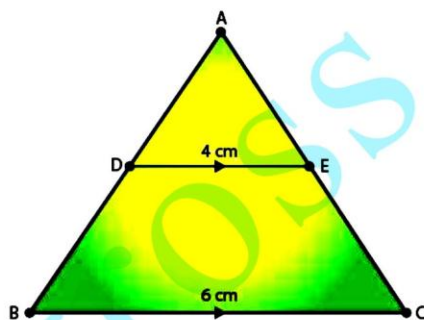
$\angle ADE = \angle B$

[Corresponding angles]

$\angle DAE = \angle BAC$

[Common]

Hence, $\triangle ADE \sim \triangle ABC$ (AA Similarity)



(i) Since the ratio of areas of two similar triangles is equal to the ratio of squares of their corresponding sides, we have,

$$\frac{\text{Ar}(\triangle ADE)}{\text{Ar}(\triangle ABC)} = \frac{DE^2}{BC^2}$$

$$\frac{16}{\text{Ar}(\triangle ABC)} = \frac{4^2}{6^2}$$

$$\Rightarrow \text{Ar}(\triangle ABC) = \frac{6^2 \times 16}{4^2}$$

$$\Rightarrow \text{Ar}(\triangle ABC) = 36 \text{ cm}^2$$

(ii) Since the ratio of areas of two similar triangles is equal to the ratio of squares of their corresponding sides, we have,

$$\frac{\text{Ar}(\triangle ADE)}{\text{Ar}(\triangle ABC)} = \frac{DE^2}{BC^2}$$

$$\frac{25}{\text{Ar}(\triangle ABC)} = \frac{4^2}{8^2}$$

$$\Rightarrow \text{Ar}(\triangle ABC) = \frac{8^2 \times 25}{4^2}$$

$$\Rightarrow \text{Ar}(\triangle ABC) = 100 \text{ cm}^2$$

(iii) According to the question,

$$\frac{\text{Ar}(\triangle ADE)}{\text{Ar}(\triangle ABC)} = \frac{DE^2}{BC^2}$$

$$\frac{\text{Ar}(\triangle ADE)}{\text{Ar}(\triangle ABC)} = \frac{3^2}{5^2}$$

$$\frac{\text{Ar}(\triangle ADE)}{\text{Ar}(\triangle ABC)} = \frac{9}{25}$$

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Assume that the area of $\triangle ADE = 9x$ sq units
And, area of $\triangle ABC = 25x$ sq units
So,
Area of trapezium BCED = Area of $\triangle ABC$ – Area of $\triangle ADE$
 $= 25x - 9x$
 $= 16x$

Now, $\text{Ar}(\triangle ADE) / \text{Ar}(\text{trap BCED}) = 9x / 16x$
 $\text{Ar}(\triangle ADE) / \text{Ar}(\text{trap BCED}) = 9/16$

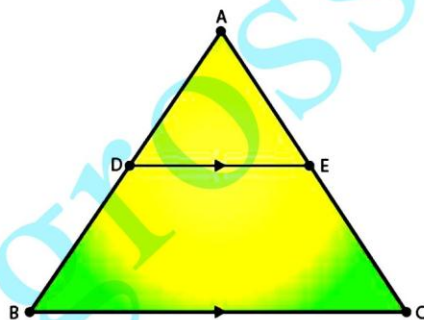
9. In $\triangle ABC$, D and E are the mid-points of AB and AC respectively. Find the ratio of the areas $\triangle ADE$ and $\triangle ABC$.

Solution:

Given:

In $\triangle ABC$, D and E are the midpoints of AB and AC respectively.

Required to find: Ratio of the areas of $\triangle ADE$ and $\triangle ABC$



Since, D and E are the midpoints of AB and AC respectively.

We can say,

$DE \parallel BC$

(By converse of mid-point theorem)

Also, $DE = (1/2) BC$

In $\triangle ADE$ and $\triangle ABC$,

$\angle ADE = \angle B$

(Corresponding angles)

$\angle DAE = \angle BAC$

(common)

Thus, $\triangle ADE \sim \triangle ABC$

(AA Similarity)

Now, we know that

The ratio of areas of two similar triangles is equal to the ratio of square of their corresponding sides, so

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$$\text{Ar}(\triangle ADE) / \text{Ar}(\triangle ABC) = AD^2 / AB^2$$

$$\text{Ar}(\triangle ADE) / \text{Ar}(\triangle ABC) = 1^2 / 2^2$$

$$\text{Ar}(\triangle ADE) / \text{Ar}(\triangle ABC) = 1/4$$

Therefore, the ratio of the areas $\triangle ADE$ and $\triangle ABC$ is 1:4

10. The areas of two similar triangles are 100 cm^2 and 49 cm^2 respectively. If the altitude of the bigger triangles is 5 cm, find the corresponding altitude of the other.

Solution:

Given: The area of the two similar triangles is 100 cm^2 and 49 cm^2 . And the altitude of the bigger triangle is 5cm.

Required to find: The corresponding altitude of the other triangle

We know that,

The ratio of the areas of the two similar triangles is equal to the ratio of squares of their corresponding altitudes.

$\text{ar}(\text{bigger triangle}) / \text{ar}(\text{smaller triangle}) = (\text{altitude of the bigger triangle} / \text{altitude of the smaller triangle})^2$

$$(100 / 49) = (5 / \text{altitude of the smaller triangle})^2$$

Taking square root on LHS and RHS, we get

$$(10 / 7) = (5 / \text{altitude of the smaller triangle}) = 7/2$$

Therefore, altitude of the smaller triangle = 3.5cm

11. The areas of two similar triangles are 121 cm^2 and 64 cm^2 respectively. If the median of the first triangle is 12.1 cm, find the corresponding median of the other.

Solution:

Given: the area of the two triangles is 121 cm^2 and 64 cm^2 respectively and the median of the first triangle is 12.1cm

Required to find: the corresponding median of the other triangle

We know that,

The ratio of the areas of the two similar triangles are equal to the ratio of the squares of their medians.

$$\text{ar}(\text{triangle1}) / \text{ar}(\text{triangle2}) = (\text{median of triangle 1} / \text{median of triangle 2})^2$$

$$121 / 64 = (12.1 / \text{median of triangle 2})^2$$

Taking the square roots on both LHS and RHS, we have

$$11/8 = (12.1 / \text{median of triangle 2}) = (12.1 \times 8) / 11$$

Therefore, Median of the other triangle = 8.8cm

**R D Sharma Solutions For Class 10 Maths Chapter 4 -
Triangles****Exercise 4.7**

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1. If the sides of a triangle are 3 cm, 4 cm, and 6 cm long, determine whether the triangle is a right-angled triangle.

Solution:

We have,

Sides of triangle as

$$AB = 3 \text{ cm}$$

$$BC = 4 \text{ cm}$$

$$AC = 6 \text{ cm}$$

On finding their squares, we get

$$AB^2 = 3^2 = 9$$

$$BC^2 = 4^2 = 16$$

$$AC^2 = 6^2 = 36$$

Since, $AB^2 + BC^2 \neq AC^2$

So, by converse of Pythagoras theorem the given sides cannot be the sides of a right triangle.

2. The sides of certain triangles are given below. Determine which of them are right triangles.

(i) $a = 7 \text{ cm}$, $b = 24 \text{ cm}$ and $c = 25 \text{ cm}$

(ii) $a = 9 \text{ cm}$, $b = 16 \text{ cm}$ and $c = 18 \text{ cm}$

(iii) $a = 1.6 \text{ cm}$, $b = 3.8 \text{ cm}$ and $c = 4 \text{ cm}$

(iv) $a = 8 \text{ cm}$, $b = 10 \text{ cm}$ and $c = 6 \text{ cm}$

Solutions:

(i) Given,

$a = 7 \text{ cm}$, $b = 24 \text{ cm}$ and $c = 25 \text{ cm}$

$$\therefore a^2 = 49, b^2 = 576 \text{ and } c^2 = 625$$

$$\text{Since, } a^2 + b^2 = 49 + 576 = 625 = c^2$$

Then, by converse of Pythagoras theorem

The given sides are of a right triangle.

(ii) Given,

$a = 9 \text{ cm}$, $b = 16 \text{ cm}$ and $c = 18 \text{ cm}$

$$\therefore a^2 = 81, b^2 = 256 \text{ and } c^2 = 324$$

$$\text{Since, } a^2 + b^2 = 81 + 256 = 337 \neq c^2$$

Then, by converse of Pythagoras theorem

The given sides cannot be of a right triangle.

(iii) Given,

$a = 1.6 \text{ cm}$, $b = 3.8 \text{ cm}$ and $C = 4 \text{ cm}$

$$\therefore a^2 = 2.56, b^2 = 14.44 \text{ and } c^2 = 16$$

$$\text{Since, } a^2 + b^2 = 2.56 + 14.44 = 17 \neq c^2$$

Then, by converse of Pythagoras theorem

The given sides cannot be of a right triangle.

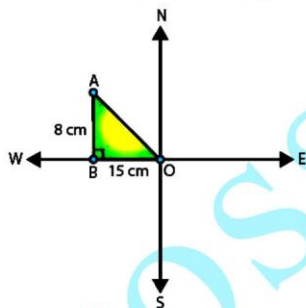
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- (iv) Given,
 $a = 8$ cm, $b = 10$ cm and $C = 6$ cm
 $\therefore a^2 = 64$, $b^2 = 100$ and $c^2 = 36$
Since, $a^2 + c^2 = 64 + 36 = 100 = b^2$
Then, by converse of Pythagoras theorem
The given sides are of a right triangle

3. A man goes 15 metres due west and then 8 metres due north. How far is he from the starting point?

Solution:

Let the starting point of the man be O and final point be A.

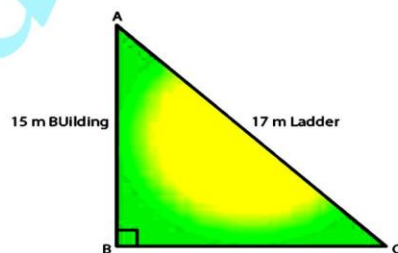


In $\triangle ABO$,
by Pythagoras theorem $AO^2 = AB^2 + BO^2$
 $\Rightarrow AO^2 = 8^2 + 15^2$
 $\Rightarrow AO^2 = 64 + 225 = 289$
 $\Rightarrow AO = \sqrt{289} = 17\text{m}$

\therefore the man is 17m far from the starting point.

4. A ladder 17 m long reaches a window of a building 15 m above the ground. Find the distance of the foot of the ladder from the building.

Solution:



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In $\triangle ABC$, by Pythagoras theorem

$$AB^2 + BC^2 = AC^2$$

$$\Rightarrow 15^2 + BC^2 = 17^2$$

$$225 + BC^2 = 17^2$$

$$BC^2 = 289 - 225$$

$$BC^2 = 64$$

$$\therefore BC = 8 \text{ m}$$

Therefore, the distance of the foot of the ladder from building = 8 m

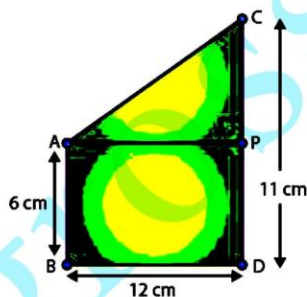
5. Two poles of heights 6 m and 11 m stand on a plane ground. If the distance between their feet is 12 m, find the distance between their tops.

Solution:

Let CD and AB be the poles of height 11 m and 6 m.

Then, it is seen that $CP = 11 - 6 = 5 \text{ m}$.

From the figure, AP should be 12 m (given)



In triangle APC, by applying Pythagoras theorem, we have

$$AP^2 + PC^2 = AC^2$$

$$12^2 + 5^2 = AC^2$$

$$AC^2 = 144 + 25 = 169$$

$$\therefore AC = 13 \text{ (by taking sq. root on both sides)}$$

Thus, the distance between their tops = 13 m.

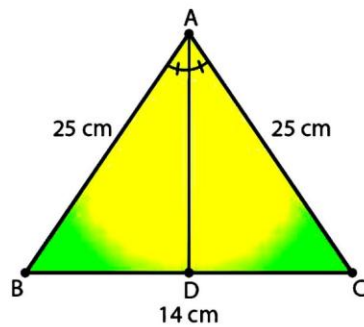
6. In an isosceles triangle ABC, $AB = AC = 25 \text{ cm}$, $BC = 14 \text{ cm}$. Calculate the altitude from A on BC.

Solution:

Given,

$$\triangle ABC, AB = AC = 25 \text{ cm and } BC = 14.$$

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In $\triangle ABD$ and $\triangle ACD$, we see that

$$\angle ADB = \angle ADC$$

[Each = 90°]

$$AB = AC$$

[Given]

$$AD = AD$$

[Common]

Then, $\triangle ABD \cong \triangle ACD$

[By RHS condition]

Thus, $BD = CD = 7$ cm

[By corresponding parts of congruent triangles]

Finally,

In $\triangle ADB$, by Pythagoras theorem

$$AD^2 + BD^2 = AB^2$$

$$\Rightarrow AD^2 + 7^2 = 25^2$$

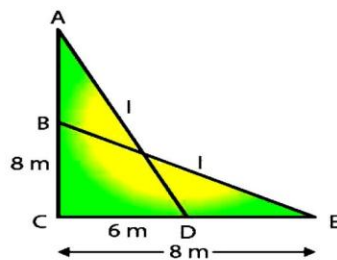
$$AD^2 = 625 - 49 = 576$$

$$\therefore AD = \sqrt{576} = 24 \text{ cm}$$

7. The foot of a ladder is 6 m away from a wall and its top reaches a window 8 m above the ground. If the ladder is shifted in such a way that its foot is 8 m away from the wall, to what height does its tip reach?

Solution:

Let's assume the length of ladder to be, $AD = BE = x$ m



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So, in $\triangle ACD$, by Pythagoras theorem

We have,

$$\begin{aligned} AD^2 &= AC^2 + CD^2 \\ \Rightarrow x^2 &= 8^2 + 6^2 \dots (i) \end{aligned}$$

Also, in $\triangle BCE$, by Pythagoras theorem

$$\begin{aligned} BE^2 &= BC^2 + CE^2 \\ \Rightarrow x^2 &= BC^2 + 8^2 \dots (ii) \end{aligned}$$

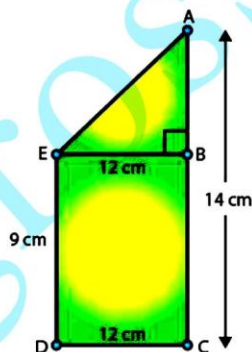
Compare (i) and (ii)

$$\begin{aligned} BC^2 + 8^2 &= 8^2 + 6^2 \\ \Rightarrow BC^2 + 6^2 & \\ \Rightarrow BC &= 6 \text{ m} \end{aligned}$$

Therefore, the tip of the ladder reaches to a height of 6m.

8. Two poles of height 9 m and 14 m stand on a plane ground. If the distance between their feet is 12 m, find the distance between their tops.

Solution:



Comparing with the figure, it's given that
 $AC = 14 \text{ m}$, $DC = 12 \text{ m}$ and $ED = BC = 9 \text{ m}$

Construction: Draw $EB \perp AC$

Now,

It's seen that $AB = AC - BC = (14 - 9) = 5 \text{ m}$

And, $EB = DC = 12 \text{ m}$ [distance between their feet]

Thus,

In $\triangle ABE$, by Pythagoras theorem, we have

$$AE^2 = AB^2 + BE^2$$

$$AE^2 = 5^2 + 12^2$$

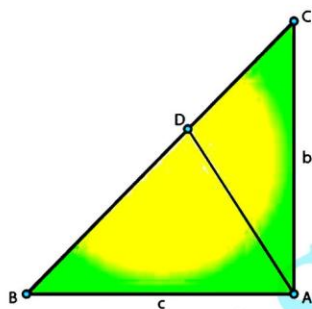
$$AE^2 = 25 + 144 = 169$$

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$$\Rightarrow AE = \sqrt{169} = 13 \text{ m}$$

Therefore, the distance between their tops = 13 m

9. Using Pythagoras theorem determine the length of AD in terms of b and c shown in Fig. 4.219
Solution:



We have,

In $\triangle BAC$, by Pythagoras theorem, we have

$$BC^2 = AB^2 + AC^2$$

$$\Rightarrow BC^2 = c^2 + b^2$$

$$\Rightarrow BC = \sqrt{c^2 + b^2}$$

In $\triangle ABD$ and $\triangle CBA$

$$\angle B = \angle B$$

[Common]

$$\angle ADB = \angle BAC$$

[Each 90°]

Then, $\triangle ABD \sim \triangle CBA$

[By AA similarity]

Thus,

$$AB/BC = AD/CA$$

[Corresponding parts of similar triangles are proportional]

$$c/\sqrt{c^2 + b^2} = AD/b$$

$$\therefore AD = bc/\sqrt{c^2 + b^2}$$

10. A triangle has sides 5 cm, 12 cm and 13 cm. Find the length to one decimal place, of the perpendicular from the opposite vertex to the side whose length is 13 cm.

Solution:

From the fig. $AB = 5 \text{ cm}$, $BC = 12 \text{ cm}$ and $AC = 13 \text{ cm}$.

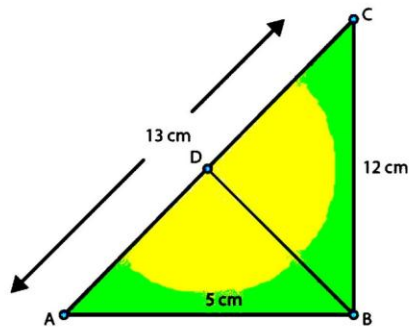
Then, $AC^2 = AB^2 + BC^2$.

$$\Rightarrow (13)^2 = (5)^2 + (12)^2 = 25 + 144 = 169 = 13^2$$

This proves that $\triangle ABC$ is a right triangle, right angled at B.

Let BD be the length of perpendicular from B on AC.

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$$\begin{aligned} \text{So, area of } \triangle ABC &= (BC \times BA) / 2 && \text{[Taking BC as the altitude]} \\ &= (12 \times 5) / 2 \\ &= 30 \text{ cm}^2 \end{aligned}$$

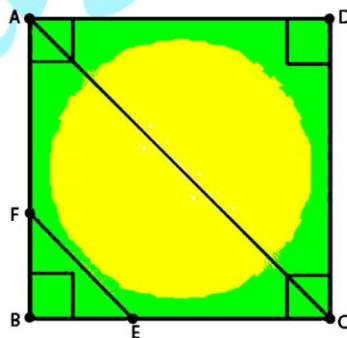
$$\begin{aligned} \text{Also, area of } \triangle ABC &= (AC \times BD) / 2 && \text{[Taking BD as the altitude]} \\ &= (13 \times BD) / 2 \end{aligned}$$

$$\begin{aligned} \Rightarrow (13 \times BD) / 2 &= 30 \\ BD &= 60 / 13 = 4.6 \text{ (to one decimal place)} \end{aligned}$$

11. ABCD is a square. F is the mid-point of AB. BE is one third of BC. If the area of $\triangle FBE = 108\text{cm}^2$, find the length of AC.

Solution:

Given,
ABCD is a square. And, F is the mid-point of AB.
BE is one third of BC.
Area of $\triangle FBE = 108\text{cm}^2$
Required to find: length of AC



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Let's assume the sides of the square to be x .

$$\Rightarrow AB = BC = CD = DA = x \text{ cm}$$

$$\text{And, } AF = FB = x/2 \text{ cm}$$

$$\text{So, } BE = x/3 \text{ cm}$$

Now, the area of $\Delta FBE = 1/2 \times BE \times FB$

$$\Rightarrow 108 = (1/2) \times (x/3) \times (x/2)$$

$$\Rightarrow x^2 = 108 \times 2 \times 3 \times 2 = 1296$$

$$\Rightarrow x = \sqrt{1296}$$

[taking square roots of both the sides]

$$\therefore x = 36 \text{ cm}$$

Further in ΔABC , by Pythagoras theorem, we have

$$AC^2 = AB^2 + BC^2$$

$$\Rightarrow AC^2 = x^2 + x^2 = 2x^2$$

$$\Rightarrow AC^2 = 2 \times (36)^2$$

$$\Rightarrow AC = 36\sqrt{2} = 36 \times 1.414 = 50.904 \text{ cm}$$

Therefore, the length of AC is 50.904 cm.

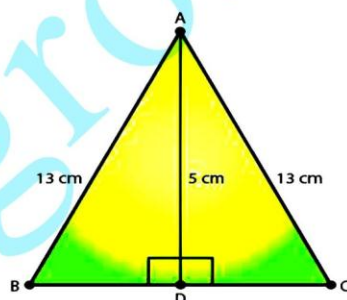
12. In an isosceles triangle ABC , if $AB = AC = 13 \text{ cm}$ and the altitude from A on BC is 5 cm, find BC .

Solution:

Given,

An isosceles triangle ABC , $AB = AC = 13 \text{ cm}$, $AD = 5 \text{ cm}$

Required to find: BC



In ΔADB , by using Pythagoras theorem, we have

$$AD^2 + BD^2 = AB^2$$

$$5^2 + BD^2 = 13^2$$

$$BD^2 = 169 - 25 = 144$$

$$\Rightarrow BD = \sqrt{144} = 12 \text{ cm}$$

Similarly, applying Pythagoras theorem in ΔADC we can have,

$$AC^2 = AD^2 + DC^2$$

$$13^2 = 5^2 + DC^2$$

$$\Rightarrow DC = \sqrt{144} = 12 \text{ cm}$$

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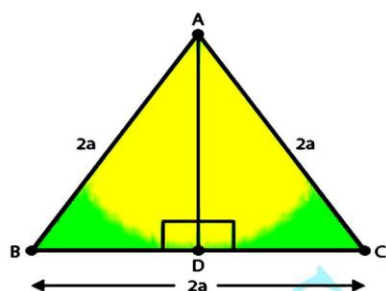
Thus, $BC = BD + DC = 12 + 12 = 24$ cm

13. In a $\triangle ABC$, $AB = BC = CA = 2a$ and $AD \perp BC$. Prove that

(i) $AD = a\sqrt{3}$

(ii) $\text{Area}(\triangle ABC) = \sqrt{3} a^2$

Solution:



- (i) In $\triangle ABD$ and $\triangle ACD$, we have
 $\angle ADB = \angle ADC = 90^\circ$
 $AB = AC$ [Given]
 $AD = AD$ [Common]
 So, $\triangle ABD \cong \triangle ACD$ [By RHS condition]
 Hence, $BD = CD = a$ [By C.P.C.T]

Now, in $\triangle ABD$, by Pythagoras theorem

$$AD^2 + BD^2 = AB^2$$

$$AD^2 + a^2 = 2a^2$$

$$AD^2 = 2a^2 - a^2 = a^2$$

$$AD = a$$

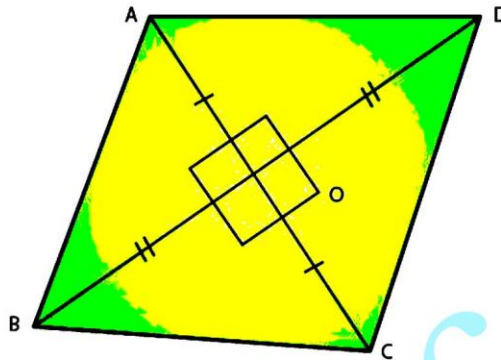
- (ii) $\text{Area}(\triangle ABC) = \frac{1}{2} \times BC \times AD$
 $= \frac{1}{2} \times (2a) \times (a\sqrt{3})$
 $= \sqrt{3} a^2$

14. The lengths of the diagonals of a rhombus is 24cm and 10cm. Find each side of the rhombus.

Solution:

Let ABCD be a rhombus and AC and BD be the diagonals of ABCD.

So, AC = 24cm and BD = 10cm

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Triangles**

We know that diagonals of a rhombus bisect each other at right angle. (Perpendicular to each other)

So,

AO = OC = 12cm and BO = OD = 3cm

In $\triangle AOB$, by Pythagoras theorem, we have

$$AB^2 = AO^2 + BO^2$$

$$= 12^2 + 3^2$$

$$= 144 + 25$$

$$= 169$$

$$\Rightarrow AB = \sqrt{169} = 13\text{cm}$$

Since, the sides of rhombus are all equal.

Therefore, $AB = BC = CD = AD = 13\text{cm}$.