

**R D Sharma Solutions For Class 10 Maths Chapter 2-  
Polynomials****Exercise 2.1**

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**1. Find the zeros of each of the following quadratic polynomials and verify the relationship between the zeros and their coefficients:**

(i)  $f(x) = x^2 - 2x - 8$

**Solution:**

Given,

$$f(x) = x^2 - 2x - 8$$

To find the zeros, we put  $f(x) = 0$ 

$$\Rightarrow x^2 - 2x - 8 = 0$$

$$\Rightarrow x^2 - 4x + 2x - 8 = 0$$

$$\Rightarrow x(x - 4) + 2(x - 4) = 0$$

$$\Rightarrow (x - 4)(x + 2) = 0$$

This gives us 2 zeros, for

$$x = 4 \text{ and } x = -2$$

Hence, the zeros of the quadratic equation are 4 and -2.

Now, for verification

Sum of zeros = - coefficient of  $x$  / coefficient of  $x^2$ 

$$4 + (-2) = -(-2) / 1$$

$$2 = 2$$

Product of roots = constant / coefficient of  $x^2$ 

$$4 \times (-2) = (-8) / 1$$

$$-8 = -8$$

Therefore, the relationship between zeros and their coefficients is verified.

(ii)  $g(s) = 4s^2 - 4s + 1$

**Solution:**

Given,

$$g(s) = 4s^2 - 4s + 1$$

To find the zeros, we put  $g(s) = 0$ 

$$\Rightarrow 4s^2 - 4s + 1 = 0$$

$$\Rightarrow 4s^2 - 2s - 2s + 1 = 0$$

$$\Rightarrow 2s(2s - 1) - (2s - 1) = 0$$

$$\Rightarrow (2s - 1)(2s - 1) = 0$$

This gives us 2 zeros, for

$$s = 1/2 \text{ and } s = 1/2$$

Hence, the zeros of the quadratic equation are 1/2 and 1/2.

Now, for verification

Sum of zeros = - coefficient of  $s$  / coefficient of  $s^2$ 

$$1/2 + 1/2 = -(-4) / 4$$

$$1 = 1$$

Product of roots = constant / coefficient of  $s^2$ 

$$1/2 \times 1/2 = 1/4$$

$$1/4 = 1/4$$

Therefore, the relationship between zeros and their coefficients is verified.

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(iii)  $h(t) = t^2 - 15$

**Solution:**

Given,

$$h(t) = t^2 - 15 = t^2 + (0)t - 15$$

To find the zeros, we put  $h(t) = 0$

$$\Rightarrow t^2 - 15 = 0$$

$$\Rightarrow (t + \sqrt{15})(t - \sqrt{15}) = 0$$

This gives us 2 zeros, for

$$t = \sqrt{15} \text{ and } t = -\sqrt{15}$$

Hence, the zeros of the quadratic equation are  $\sqrt{15}$  and  $-\sqrt{15}$ .

Now, for verification

Sum of zeros = - coefficient of  $t$  / coefficient of  $t^2$

$$\sqrt{15} + (-\sqrt{15}) = -(0) / 1$$

$$0 = 0$$

Product of roots = constant / coefficient of  $t^2$

$$\sqrt{15} \times (-\sqrt{15}) = -15 / 1$$

$$-15 = -15$$

Therefore, the relationship between zeros and their coefficients is verified.

(iv)  $f(x) = 6x^2 - 3 - 7x$

**Solution:**

Given,

$$f(x) = 6x^2 - 3 - 7x$$

To find the zeros, we put  $f(x) = 0$

$$\Rightarrow 6x^2 - 3 - 7x = 0$$

$$\Rightarrow 6x^2 - 9x + 2x - 3 = 0$$

$$\Rightarrow 3x(2x - 3) + 1(2x - 3) = 0$$

$$\Rightarrow (2x - 3)(3x + 1) = 0$$

This gives us 2 zeros, for

$$x = 3/2 \text{ and } x = -1/3$$

Hence, the zeros of the quadratic equation are  $3/2$  and  $-1/3$ .

Now, for verification

Sum of zeros = - coefficient of  $x$  / coefficient of  $x^2$

$$3/2 + (-1/3) = -(-7) / 6$$

$$7/6 = 7/6$$

Product of roots = constant / coefficient of  $x^2$

$$3/2 \times (-1/3) = (-3) / 6$$

$$-1/2 = -1/2$$

Therefore, the relationship between zeros and their coefficients is verified.

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(v)  $p(x) = x^2 + 2\sqrt{2}x - 6$

**Solution:**

Given,

$$p(x) = x^2 + 2\sqrt{2}x - 6$$

To find the zeros, we put  $p(x) = 0$

$$\Rightarrow x^2 + 2\sqrt{2}x - 6 = 0$$

$$\Rightarrow x^2 + 3\sqrt{2}x - \sqrt{2}x - 6 = 0$$

$$\Rightarrow x(x + 3\sqrt{2}) - \sqrt{2}(x + 3\sqrt{2}) = 0$$

$$\Rightarrow (x - \sqrt{2})(x + 3\sqrt{2}) = 0$$

This gives us 2 zeros, for

$$x = \sqrt{2} \text{ and } x = -3\sqrt{2}$$

Hence, the zeros of the quadratic equation are  $\sqrt{2}$  and  $-3\sqrt{2}$ .

Now, for verification

Sum of zeros = - coefficient of  $x$  / coefficient of  $x^2$

$$\sqrt{2} + (-3\sqrt{2}) = -(2\sqrt{2}) / 1$$

$$-2\sqrt{2} = -2\sqrt{2}$$

Product of roots = constant / coefficient of  $x^2$

$$\sqrt{2} \times (-3\sqrt{2}) = (-6) / 2\sqrt{2}$$

$$-3 \times 2 = -6/1$$

$$-6 = -6$$

Therefore, the relationship between zeros and their coefficients is verified.

(vi)  $q(x) = \sqrt{3}x^2 + 10x + 7\sqrt{3}$

**Solution:**

Given,

$$q(x) = \sqrt{3}x^2 + 10x + 7\sqrt{3}$$

To find the zeros, we put  $q(x) = 0$

$$\Rightarrow \sqrt{3}x^2 + 10x + 7\sqrt{3} = 0$$

$$\Rightarrow \sqrt{3}x^2 + 3x + 7x + 7\sqrt{3} = 0$$

$$\Rightarrow \sqrt{3}x(x + \sqrt{3}) + 7(x + \sqrt{3}) = 0$$

$$\Rightarrow (x + \sqrt{3})(\sqrt{3}x + 7) = 0$$

This gives us 2 zeros, for

$$x = -\sqrt{3} \text{ and } x = -7/\sqrt{3}$$

Hence, the zeros of the quadratic equation are  $-\sqrt{3}$  and  $-7/\sqrt{3}$ .

Now, for verification

Sum of zeros = - coefficient of  $x$  / coefficient of  $x^2$

$$-\sqrt{3} + (-7/\sqrt{3}) = -(10)/\sqrt{3}$$

$$(-3-7)/\sqrt{3} = -10/\sqrt{3}$$

$$-10/\sqrt{3} = -10/\sqrt{3}$$

Product of roots = constant / coefficient of  $x^2$

$$(-\sqrt{3}) \times (-7/\sqrt{3}) = (7\sqrt{3})/\sqrt{3}$$

$$7 = 7$$

Therefore, the relationship between zeros and their coefficients is verified.

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(vii)  $f(x) = x^2 - (\sqrt{3} + 1)x + \sqrt{3}$

**Solution:**

Given,

$$f(x) = x^2 - (\sqrt{3} + 1)x + \sqrt{3}$$

To find the zeros, we put  $f(x) = 0$

$$\Rightarrow x^2 - (\sqrt{3} + 1)x + \sqrt{3} = 0$$

$$\Rightarrow x^2 - \sqrt{3}x - x + \sqrt{3} = 0$$

$$\Rightarrow x(x - \sqrt{3}) - 1(x - \sqrt{3}) = 0$$

$$\Rightarrow (x - \sqrt{3})(x - 1) = 0$$

This gives us 2 zeros, for

$$x = \sqrt{3} \text{ and } x = 1$$

Hence, the zeros of the quadratic equation are  $\sqrt{3}$  and 1.

Now, for verification

Sum of zeros = - coefficient of  $x$  / coefficient of  $x^2$

$$\sqrt{3} + 1 = -(-(\sqrt{3} + 1)) / 1$$

$$\sqrt{3} + 1 = \sqrt{3} + 1$$

Product of roots = constant / coefficient of  $x^2$

$$1 \times \sqrt{3} = \sqrt{3} / 1$$

$$\sqrt{3} = \sqrt{3}$$

Therefore, the relationship between zeros and their coefficients is verified.

(viii)  $g(x) = a(x^2 + 1) - x(a^2 + 1)$

**Solution:**

Given,

$$g(x) = a(x^2 + 1) - x(a^2 + 1)$$

To find the zeros, we put  $g(x) = 0$

$$\Rightarrow a(x^2 + 1) - x(a^2 + 1) = 0$$

$$\Rightarrow ax^2 + a - a^2x - x = 0$$

$$\Rightarrow ax^2 - a^2x - x + a = 0$$

$$\Rightarrow ax(x - a) - 1(x - a) = 0$$

$$\Rightarrow (x - a)(ax - 1) = 0$$

This gives us 2 zeros, for

$$x = a \text{ and } x = 1/a$$

Hence, the zeros of the quadratic equation are  $a$  and  $1/a$ .

Now, for verification

Sum of zeros = - coefficient of  $x$  / coefficient of  $x^2$

$$a + 1/a = -(-a^2 - 1) / a$$

$$(a^2 + 1)/a = (a^2 + 1)/a$$

Product of roots = constant / coefficient of  $x^2$

$$a \times 1/a = a / a$$

$$1 = 1$$

Therefore, the relationship between zeros and their coefficients is verified.

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(ix)  $h(s) = 2s^2 - (1 + 2\sqrt{2})s + \sqrt{2}$

**Solution:**

Given,

$$h(s) = 2s^2 - (1 + 2\sqrt{2})s + \sqrt{2}$$

To find the zeros, we put  $h(s) = 0$

$$\Rightarrow 2s^2 - (1 + 2\sqrt{2})s + \sqrt{2} = 0$$

$$\Rightarrow 2s^2 - 2\sqrt{2}s - s + \sqrt{2} = 0$$

$$\Rightarrow 2s(s - \sqrt{2}) - 1(s - \sqrt{2}) = 0$$

$$\Rightarrow (2s - 1)(s - \sqrt{2}) = 0$$

This gives us 2 zeros, for

$$x = \sqrt{2} \text{ and } x = 1/2$$

Hence, the zeros of the quadratic equation are  $\sqrt{2}$  and  $1/2$ .

Now, for verification

Sum of zeros = - coefficient of  $s$  / coefficient of  $s^2$

$$\sqrt{2} + 1/2 = -(-(1 + 2\sqrt{2})) / 2$$

$$(2\sqrt{2} + 1)/2 = (2\sqrt{2} + 1)/2$$

Product of roots = constant / coefficient of  $s^2$

$$1/2 \times \sqrt{2} = \sqrt{2} / 2$$

$$\sqrt{2} / 2 = \sqrt{2} / 2$$

Therefore, the relationship between zeros and their coefficients is verified.

(x)  $f(v) = v^2 + 4\sqrt{3}v - 15$

**Solution:**

Given,

$$f(v) = v^2 + 4\sqrt{3}v - 15$$

To find the zeros, we put  $f(v) = 0$

$$\Rightarrow v^2 + 4\sqrt{3}v - 15 = 0$$

$$\Rightarrow v^2 + 5\sqrt{3}v - \sqrt{3}v - 15 = 0$$

$$\Rightarrow v(v + 5\sqrt{3}) - \sqrt{3}(v + 5\sqrt{3}) = 0$$

$$\Rightarrow (v - \sqrt{3})(v + 5\sqrt{3}) = 0$$

This gives us 2 zeros, for

$$v = \sqrt{3} \text{ and } v = -5\sqrt{3}$$

Hence, the zeros of the quadratic equation are  $\sqrt{3}$  and  $-5\sqrt{3}$ .

Now, for verification

Sum of zeros = - coefficient of  $v$  / coefficient of  $v^2$

$$\sqrt{3} + (-5\sqrt{3}) = -(4\sqrt{3}) / 1$$

$$-4\sqrt{3} = -4\sqrt{3}$$

Product of roots = constant / coefficient of  $v^2$

$$\sqrt{3} \times (-5\sqrt{3}) = (-15) / 1$$

$$-5 \times 3 = -15$$

$$-15 = -15$$

Therefore, the relationship between zeros and their coefficients is verified.

(xi)  $p(y) = y^2 + (3\sqrt{5}/2)y - 5$



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**Solution:**

Given,

$$p(y) = y^2 + (3\sqrt{5}/2)y - 5$$

To find the zeros, we put  $f(y) = 0$

$$\Rightarrow y^2 + (3\sqrt{5}/2)y - 5 = 0$$

$$\Rightarrow y^2 - \sqrt{5}/2 y + 2\sqrt{5}y - 5 = 0$$

$$\Rightarrow y(y - \sqrt{5}/2) + 2\sqrt{5}(y - \sqrt{5}/2) = 0$$

$$\Rightarrow (y + 2\sqrt{5})(y - \sqrt{5}/2) = 0$$

This gives us 2 zeros, for

$$y = \sqrt{5}/2 \text{ and } y = -2\sqrt{5}$$

Hence, the zeros of the quadratic equation are  $\sqrt{5}/2$  and  $-2\sqrt{5}$ .

Now, for verification

Sum of zeros = - coefficient of  $y$  / coefficient of  $y^2$

$$\sqrt{5}/2 + (-2\sqrt{5}) = -(3\sqrt{5}/2) / 1$$

$$-3\sqrt{5}/2 = -3\sqrt{5}/2$$

Product of roots = constant / coefficient of  $y^2$

$$\sqrt{5}/2 \times (-2\sqrt{5}) = (-5) / 1$$

$$-(\sqrt{5})^2 = -5$$

$$-5 = -5$$

Therefore, the relationship between zeros and their coefficients is verified.

**(xii)  $q(y) = 7y^2 - (11/3)y - 2/3$**

**Solution:**

Given,

$$q(y) = 7y^2 - (11/3)y - 2/3$$

To find the zeros, we put  $q(y) = 0$

$$\Rightarrow 7y^2 - (11/3)y - 2/3 = 0$$

$$\Rightarrow (21y^2 - 11y - 2)/3 = 0$$

$$\Rightarrow 21y^2 - 11y - 2 = 0$$

$$\Rightarrow 21y^2 - 14y + 3y - 2 = 0$$

$$\Rightarrow 7y(3y - 2) - 1(3y + 2) = 0$$

$$\Rightarrow (3y - 2)(7y + 1) = 0$$

This gives us 2 zeros, for

$$y = 2/3 \text{ and } y = -1/7$$

Hence, the zeros of the quadratic equation are  $2/3$  and  $-1/7$ .

Now, for verification

Sum of zeros = - coefficient of  $y$  / coefficient of  $y^2$

$$2/3 + (-1/7) = -(-11/3) / 7$$

$$-11/21 = -11/21$$

Product of roots = constant / coefficient of  $y^2$

$$2/3 \times (-1/7) = (-2/3) / 7$$

$$-2/21 = -2/21$$

Therefore, the relationship between zeros and their coefficients is verified.

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2. For each of the following, find a quadratic polynomial whose sum and product respectively of the zeros are as given. Also, find the zeros of these polynomials by factorization.

(i)  $-8/3, 4/3$

**Solution:**

A quadratic polynomial formed for the given sum and product of zeros is given by:

$$f(x) = x^2 - (\text{sum of zeros})x + (\text{product of roots})$$

Here, the sum of zeros is  $= -8/3$  and product of zero  $= 4/3$

Thus,

The required polynomial  $f(x)$  is,

$$\Rightarrow x^2 - (-8/3)x + (4/3)$$

$$\Rightarrow x^2 + 8/3x + (4/3)$$

So, to find the zeros we put  $f(x) = 0$

$$\Rightarrow x^2 + 8/3x + (4/3) = 0$$

$$\Rightarrow 3x^2 + 8x + 4 = 0$$

$$\Rightarrow 3x^2 + 6x + 2x + 4 = 0$$

$$\Rightarrow 3x(x + 2) + 2(x + 2) = 0$$

$$\Rightarrow (x + 2)(3x + 2) = 0$$

$$\Rightarrow (x + 2) = 0 \text{ and, or } (3x + 2) = 0$$

Therefore, the two zeros are  $-2$  and  $-2/3$ .

(ii)  $21/8, 5/16$

**Solution:**

A quadratic polynomial formed for the given sum and product of zeros is given by:

$$f(x) = x^2 - (\text{sum of zeros})x + (\text{product of roots})$$

Here, the sum of zeros is  $= 21/8$  and product of zero  $= 5/16$

Thus,

The required polynomial  $f(x)$  is,

$$\Rightarrow x^2 - (21/8)x + (5/16)$$

$$\Rightarrow x^2 - 21/8x + 5/16$$

So, to find the zeros we put  $f(x) = 0$

$$\Rightarrow x^2 - 21/8x + 5/16 = 0$$

$$\Rightarrow 16x^2 - 42x + 5 = 0$$

$$\Rightarrow 16x^2 - 40x - 2x + 5 = 0$$

$$\Rightarrow 8x(2x - 5) - 1(2x - 5) = 0$$

$$\Rightarrow (2x - 5)(8x - 1) = 0$$

$$\Rightarrow (2x - 5) = 0 \text{ and, or } (8x - 1) = 0$$

Therefore, the two zeros are  $5/2$  and  $1/8$ .

(iii)  $-2\sqrt{3}, -9$

**Solution:**

A quadratic polynomial formed for the given sum and product of zeros is given by:

$$f(x) = x^2 - (\text{sum of zeros})x + (\text{product of roots})$$

Here, the sum of zeros is  $= -2\sqrt{3}$  and product of zero  $= -9$

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Thus,

The required polynomial  $f(x)$  is,

$$\Rightarrow x^2 - (-2\sqrt{3})x + (-9)$$

$$\Rightarrow x^2 + 2\sqrt{3}x - 9$$

So, to find the zeros we put  $f(x) = 0$

$$\Rightarrow x^2 + 2\sqrt{3}x - 9 = 0$$

$$\Rightarrow x^2 + 3\sqrt{3}x - \sqrt{3}x - 9 = 0$$

$$\Rightarrow x(x + 3\sqrt{3}) - \sqrt{3}(x + 3\sqrt{3}) = 0$$

$$\Rightarrow (x + 3\sqrt{3})(x - \sqrt{3}) = 0$$

$$\Rightarrow (x + 3\sqrt{3}) = 0 \text{ and, or } (x - \sqrt{3}) = 0$$

Therefore, the two zeros are  $-3\sqrt{3}$  and  $\sqrt{3}$ .

(iv)  $-3/2\sqrt{5}$ ,  $-1/2$

**Solution:**

A quadratic polynomial formed for the given sum and product of zeros is given by:

$$f(x) = x^2 - (\text{sum of zeros})x + (\text{product of roots})$$

Here, the sum of zeros is  $-3/2\sqrt{5}$  and product of zero  $= -1/2$

Thus,

The required polynomial  $f(x)$  is,

$$\Rightarrow x^2 - (-3/2\sqrt{5})x + (-1/2)$$

$$\Rightarrow x^2 + 3/2\sqrt{5}x - 1/2$$

So, to find the zeros we put  $f(x) = 0$

$$\Rightarrow x^2 + 3/2\sqrt{5}x - 1/2 = 0$$

$$\Rightarrow 2\sqrt{5}x^2 + 3x - \sqrt{5} = 0$$

$$\Rightarrow 2\sqrt{5}x^2 + 5x - 2x - \sqrt{5} = 0$$

$$\Rightarrow \sqrt{5}x(2x + \sqrt{5}) - 1(2x + \sqrt{5}) = 0$$

$$\Rightarrow (2x + \sqrt{5})(\sqrt{5}x - 1) = 0$$

$$\Rightarrow (2x + \sqrt{5}) = 0 \text{ and, or } (\sqrt{5}x - 1) = 0$$

Therefore, the two zeros are  $-\sqrt{5}/2$  and  $1/\sqrt{5}$ .

**3. If  $\alpha$  and  $\beta$  are the zeros of the quadratic polynomial  $f(x) = x^2 - 5x + 4$ , find the value of  $1/\alpha + 1/\beta - 2\alpha\beta$ .**

**Solution:**

From the question, it's given that:

$\alpha$  and  $\beta$  are the roots of the quadratic polynomial  $f(x)$  where  $a = 1$ ,  $b = -5$  and  $c = 4$

So, we can find

$$\text{Sum of the roots} = \alpha + \beta = -b/a = -(-5)/1 = -5$$

$$\text{Product of the roots} = \alpha\beta = c/a = 4/1 = 4$$

To find,  $1/\alpha + 1/\beta - 2\alpha\beta$

$$\Rightarrow [(\alpha + \beta)/\alpha\beta] - 2\alpha\beta$$

$$\Rightarrow (-5)/4 - 2(4) = -5/4 - 8 = -27/4$$

**4. If  $\alpha$  and  $\beta$  are the zeros of the quadratic polynomial  $p(y) = 5y^2 - 7y + 1$ , find the value of  $1/\alpha + 1/\beta$ .**

**Solution:**



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From the question, it's given that:

$\alpha$  and  $\beta$  are the roots of the quadratic polynomial  $f(x)$  where  $a=5$ ,  $b=-7$  and  $c=1$

So, we can find

Sum of the roots  $= \alpha + \beta = -b/a = -(-7)/5 = 7/5$

Product of the roots  $= \alpha\beta = c/a = 1/5$

To find,  $1/\alpha + 1/\beta$

$$\Rightarrow (\alpha + \beta) / \alpha\beta$$

$$\Rightarrow (7/5) / (1/5) = 7$$

**5. If  $\alpha$  and  $\beta$  are the zeros of the quadratic polynomial  $f(x) = x^2 - x - 4$ , find the value of  $1/\alpha + 1/\beta - \alpha\beta$ .**  
**Solution:**

From the question, it's given that:

$\alpha$  and  $\beta$  are the roots of the quadratic polynomial  $f(x)$  where  $a=1$ ,  $b=-1$  and  $c=-4$

So, we can find

Sum of the roots  $= \alpha + \beta = -b/a = -(-1)/1 = 1$

Product of the roots  $= \alpha\beta = c/a = -4/1 = -4$

To find,  $1/\alpha + 1/\beta - \alpha\beta$

$$\Rightarrow [(\alpha + \beta) / \alpha\beta] - \alpha\beta$$

$$\Rightarrow [(1) / (-4)] - (-4) = -1/4 + 4 = 15/4$$

**6. If  $\alpha$  and  $\beta$  are the zeroes of the quadratic polynomial  $f(x) = x^2 + x - 2$ , find the value of  $1/\alpha - 1/\beta$ .**  
**Solution:**

From the question, it's given that:

$\alpha$  and  $\beta$  are the roots of the quadratic polynomial  $f(x)$  where  $a=1$ ,  $b=1$  and  $c=-2$

So, we can find

Sum of the roots  $= \alpha + \beta = -b/a = -(1)/1 = -1$

Product of the roots  $= \alpha\beta = c/a = -2/1 = -2$

To find,  $1/\alpha - 1/\beta$

$$\Rightarrow [(\beta - \alpha) / \alpha\beta]$$

$$\Rightarrow \frac{\beta - \alpha}{\alpha\beta} = \frac{\beta - \alpha}{\alpha\beta} \times \frac{(\alpha + \beta)}{\alpha + \beta} = \frac{\sqrt{(\alpha + \beta)^2 - 4\alpha\beta}}{\alpha\beta} = \frac{\sqrt{1 + 8}}{2} = \frac{\sqrt{9}}{2} = \frac{3}{2}$$

**7. If one of the zero of the quadratic polynomial  $f(x) = 4x^2 - 8kx - 9$  is negative of the other, then find the value of  $k$ .**  
**Solution:**

From the question, it's given that:

The quadratic polynomial  $f(x)$  where  $a=4$ ,  $b=-8k$  and  $c=-9$

And, for roots to be negative of each other, let the roots be  $\alpha$  and  $-\alpha$ .

So, we can find

Sum of the roots  $= \alpha - \alpha = -b/a = -(-8k)/4 = 8k = 0 \quad [\because \alpha - \alpha = 0]$

$$\Rightarrow k = 0$$

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8. If the sum of the zeroes of the quadratic polynomial  $f(t) = kt^2 + 2t + 3k$  is equal to their product, then find the value of  $k$ .

**Solution:**

Given,

The quadratic polynomial  $f(t) = kt^2 + 2t + 3k$ , where  $a = k$ ,  $b = 2$  and  $c = 3k$ .

And,

Sum of the roots = Product of the roots

$$\Rightarrow \quad (-b/a) = (c/a)$$

$$\Rightarrow \quad (-2/k) = (3k/k)$$

$$\Rightarrow \quad (-2/k) = 3$$

$$\therefore k = -2/3$$

9. If  $\alpha$  and  $\beta$  are the zeros of the quadratic polynomial  $p(x) = 4x^2 - 5x - 1$ , find the value of  $\alpha^2\beta + \alpha\beta^2$ .

**Solution:**

From the question, it's given that:

$\alpha$  and  $\beta$  are the roots of the quadratic polynomial  $p(x)$  where  $a = 4$ ,  $b = -5$  and  $c = -1$

So, we can find

Sum of the roots  $= \alpha + \beta = -b/a = -(-5)/4 = 5/4$

Product of the roots  $= \alpha\beta = c/a = -1/4$

To find,  $\alpha^2\beta + \alpha\beta^2$

$$\Rightarrow \quad \alpha\beta(\alpha + \beta)$$

$$\Rightarrow \quad (-1/4)(5/4) = -5/16$$

10. If  $\alpha$  and  $\beta$  are the zeros of the quadratic polynomial  $f(t) = t^2 - 4t + 3$ , find the value of  $\alpha^4\beta^3 + \alpha^3\beta^4$ .

**Solution:**

From the question, it's given that:

$\alpha$  and  $\beta$  are the roots of the quadratic polynomial  $f(t)$  where  $a = 1$ ,  $b = -4$  and  $c = 3$

So, we can find

Sum of the roots  $= \alpha + \beta = -b/a = -(-4)/1 = 4$

Product of the roots  $= \alpha\beta = c/a = 3/1 = 3$

To find,  $\alpha^4\beta^3 + \alpha^3\beta^4$

$$\Rightarrow \quad \alpha^3\beta^3(\alpha + \beta)$$

$$\Rightarrow \quad (\alpha\beta)^3(\alpha + \beta)$$

$$\Rightarrow \quad (3)^3(4) = 27 \times 4 = 108$$

## R D Sharma Solutions For Class 10 Maths Chapter 2- Polynomials

### Exercise 2.2

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1. Verify that the numbers given alongside of the cubic polynomials below are their zeroes. Also, verify the relationship between the zeros and coefficients in each of the following cases:

(i)  $f(x) = 2x^3 + x^2 - 5x + 2$ ;  $1/2, 1, -2$

**Solution:**

Given,  $f(x) = 2x^3 + x^2 - 5x + 2$ , where  $a = 2, b = 1, c = -5$  and  $d = 2$

For  $x = 1/2$

$$f(1/2) = 2(1/2)^3 + (1/2)^2 - 5(1/2) + 2$$

$$= 1/4 + 1/4 - 5/2 + 2 = 0$$

$\Rightarrow f(1/2) = 0$ , hence  $x = 1/2$  is a root of the given polynomial.

For  $x = 1$

$$f(1) = 2(1)^3 + (1)^2 - 5(1) + 2$$

$$= 2 + 1 - 5 + 2 = 0$$

$\Rightarrow f(1) = 0$ , hence  $x = 1$  is also a root of the given polynomial.

For  $x = -2$

$$f(-2) = 2(-2)^3 + (-2)^2 - 5(-2) + 2$$

$$= -16 + 4 + 10 + 2 = 0$$

$\Rightarrow f(-2) = 0$ , hence  $x = -2$  is also a root of the given polynomial.

Now,

Sum of zeros =  $-b/a$

$$1/2 + 1 - 2 = -(1)/2$$

$$-1/2 = -1/2$$

Sum of the products of the zeros taken two at a time =  $c/a$

$$(1/2 \times 1) + (1 \times -2) + (1/2 \times -2) = -5/2$$

$$1/2 - 2 + (-1) = -5/2$$

$$-5/2 = -5/2$$

Product of zeros =  $-d/a$

$$1/2 \times 1 \times (-2) = -(2)/2$$

$$-1 = -1$$

Hence, the relationship between the zeros and coefficients is verified.

(ii)  $g(x) = x^3 - 4x^2 + 5x - 2$ ;  $2, 1, 1$

**Solution:**

Given,  $g(x) = x^3 - 4x^2 + 5x - 2$ , where  $a = 1, b = -4, c = 5$  and  $d = -2$

For  $x = 2$

$$g(2) = (2)^3 - 4(2)^2 + 5(2) - 2$$

$$= 8 - 16 + 10 - 2 = 0$$

$\Rightarrow g(2) = 0$ , hence  $x = 2$  is a root of the given polynomial.

For  $x = 1$

$$g(1) = (1)^3 - 4(1)^2 + 5(1) - 2$$

$$= 1 - 4 + 5 - 2 = 0$$

$\Rightarrow g(1) = 0$ , hence  $x = 1$  is also a root of the given polynomial.

Now,

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Sum of zeros =  $-b/a$

$$1 + 1 + 2 = -(-4)/1$$

$$4 = 4$$

Sum of the products of the zeros taken two at a time =  $c/a$

$$(1 \times 1) + (1 \times 2) + (2 \times 1) = 5/1$$

$$1 + 2 + 2 = 5$$

$$5 = 5$$

Product of zeros =  $-d/a$

$$1 \times 1 \times 2 = -(-2)/1$$

$$2 = 2$$

Hence, the relationship between the zeros and coefficients is verified.

**2. Find a cubic polynomial with the sum, sum of the product of its zeroes taken two at a time, and product of its zeros as 3, -1 and -3 respectively.**

**Solution:**

Generally,

A cubic polynomial say,  $f(x)$  is of the form  $ax^3 + bx^2 + cx + d$ .

And, can be shown w.r.t its relationship between roots as.

$$\Rightarrow f(x) = k [x^3 - (\text{sum of roots})x^2 + (\text{sum of products of roots taken two at a time})x - (\text{product of roots})]$$

Where,  $k$  is any non-zero real number.

Here,

$$f(x) = k [x^3 - (3)x^2 + (-1)x - (-3)]$$

$$\therefore f(x) = k [x^3 - 3x^2 - x + 3]$$

where,  $k$  is any non-zero real number.

**3. If the zeros of the polynomial  $f(x) = 2x^3 - 15x^2 + 37x - 30$  are in A.P., find them.**

**Solution:**

Let the zeros of the given polynomial be  $\alpha$ ,  $\beta$  and  $\gamma$ . (3 zeros as it's a cubic polynomial)

And given, the zeros are in A.P.

So, let's consider the roots as

$$\alpha = a - d, \beta = a \text{ and } \gamma = a + d$$

Where,  $a$  is the first term and  $d$  is the common difference.

From given  $f(x)$ ,  $a = 2$ ,  $b = -15$ ,  $c = 37$  and  $d = 30$

$$\Rightarrow \text{Sum of roots} = \alpha + \beta + \gamma = (a - d) + a + (a + d) = 3a = (-b/a) = -(-15/2) = 15/2$$

So, calculating for  $a$ , we get  $3a = 15/2 \Rightarrow a = 5/2$

$$\Rightarrow \text{Product of roots} = (a - d) \times a \times (a + d) = a(a^2 - d^2) = -d/a = -(30)/2 = 15$$

$$\Rightarrow a(a^2 - d^2) = 15$$

Substituting the value of  $a$ , we get

$$\Rightarrow (5/2)[(5/2)^2 - d^2] = 15$$

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$$\begin{aligned}\Rightarrow & 5[(25/4) - d^2] = 30 \\ \Rightarrow & (25/4) - d^2 = 6 \\ \Rightarrow & 25 - 4d^2 = 24 \\ \Rightarrow & 1 = 4d^2 \\ \therefore d &= 1/2 \text{ or } -1/2\end{aligned}$$

Taking  $d = 1/2$  and  $a = 5/2$   
We get,  
the zeros as 2,  $5/2$  and 3

Taking  $d = -1/2$  and  $a = 5/2$   
We get,  
the zeros as 3,  $5/2$  and 2



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### Exercise 2.3

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1. Apply division algorithm to find the quotient  $q(x)$  and remainder  $r(x)$  on dividing  $f(x)$  by  $g(x)$  in each of the following:

(i)  $f(x) = x^3 - 6x^2 + 11x - 6$ ,  $g(x) = x^2 + x + 1$

**Solution:**

Given,

$$f(x) = x^3 - 6x^2 + 11x - 6, \quad g(x) = x^2 + x + 1$$

$$\begin{array}{r}
 \phantom{x^2 + x + 1} \quad \quad \quad x \quad -7 \\
 x^2 + x + 1 \overline{) x^3 - 6x^2 + 11x - 6} \\
 \underline{-(x^3 + x^2 + x)} \phantom{-6} \\
 -7x^2 + 10x - 6 \\
 \underline{-( -7x^2 - 7x - 7)} \\
 17x + 1
 \end{array}$$

Thus,

$$q(x) = x - 7 \text{ and } r(x) = 17x - 1$$

(ii)  $f(x) = 10x^4 + 17x^3 - 62x^2 + 30x - 3$ ,  $g(x) = 2x^2 + 7x + 1$

**Solution:**

Given,

$$f(x) = 10x^4 + 17x^3 - 62x^2 + 30x - 3 \text{ and } g(x) = 2x^2 + 7x + 1$$

$$\begin{array}{r}
 \phantom{2x^2 + 7x + 1} \quad \quad \quad 5x^2 \quad -9x \quad -2 \\
 2x^2 + 7x + 1 \overline{) 10x^4 + 17x^3 - 62x^2 + 30x - 3} \\
 \underline{-(10x^4 + 35x^3 + 5x^2)} \phantom{-3} \\
 -18x^3 - 67x^2 + 30x - 3 \\
 \underline{-( -18x^3 - 63x^2 - 9x)} \phantom{-3} \\
 -4x^2 + 39x - 3 \\
 \underline{-( -4x^2 - 14x - 2)} \\
 53x - 1
 \end{array}$$

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Thus,

$$q(x) = 5x^2 - 9x - 2 \text{ and } r(x) = 53x - 1$$

(iii)  $f(x) = 4x^3 + 8x^2 + 8x + 7$ ,  $g(x) = 2x^2 - x + 1$

**Solution:**

Given,

$$f(x) = 4x^3 + 8x^2 + 8x + 7 \text{ and } g(x) = 2x^2 - x + 1$$

$$\begin{array}{r}
 2x^2 - x + 1 \overline{) 4x^3 + 8x^2 + 8x + 7} \\
 \underline{4x^3 \quad - 2x^2 + 2x} \phantom{+ 7} \\
 10x^2 + 6x + 7 \\
 \underline{10x^2 - 5x + 5} \\
 11x + 2
 \end{array}$$

Thus,

$$q(x) = 15x + 10 \text{ and } r(x) = 3x - 32$$

(iv)  $f(x) = 15x^3 - 20x^2 + 13x - 12$ ,  $g(x) = x^2 - 2x + 2$

**Solution:**

Given,

$$f(x) = 15x^3 - 20x^2 + 13x - 12 \text{ and } g(x) = x^2 - 2x + 2$$

$$\begin{array}{r}
 x^2 - 2x + 2 \overline{) 15x^3 - 20x^2 + 13x - 12} \\
 \underline{15x^3 \quad - 30x^2 + 30x} \phantom{- 12} \\
 10x^2 - 17x - 12 \\
 \underline{10x^2 \quad - 20x + 20} \\
 3x - 32
 \end{array}$$

Thus,

$$q(x) = 15x + 10 \text{ and } r(x) = 3x - 32$$

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2. Check whether the first polynomial is a factor of the second polynomial by applying the division algorithm:

(i)  $g(t) = t^2 - 3$ ;  $f(t) = 2t^4 + 3t^3 - 2t^2 - 9t - 12$

**Solution:**

Given,

$$g(t) = t^2 - 3; f(t) = 2t^4 + 3t^3 - 2t^2 - 9t - 12$$

$$\begin{array}{r}
 \phantom{t^2 - 3} \overline{2t^4 + 3t^3 - 2t^2 - 9t - 12} \\
 \phantom{t^2 - 3} \underline{2t^4 + 0t^3 - 6t^2} \phantom{- 9t - 12} \\
 \phantom{t^2 - 3} \phantom{2t^4 +} 3t^3 + 4t^2 - 9t - 12 \\
 \phantom{t^2 - 3} \phantom{2t^4 +} \underline{3t^3 + 0t^2 - 9t} \phantom{- 12} \\
 \phantom{t^2 - 3} \phantom{2t^4 +} \phantom{3t^3 +} 4t^2 + 0t - 12 \\
 \phantom{t^2 - 3} \phantom{2t^4 +} \phantom{3t^3 +} \underline{4t^2 + 0t - 12} \\
 \phantom{t^2 - 3} \phantom{2t^4 +} \phantom{3t^3 +} \phantom{4t^2 +} 0
 \end{array}$$

Since, the remainder  $r(t) = 0$  we can say that the first polynomial is a factor of the second polynomial.

(ii)  $g(x) = x^3 - 3x + 1$ ;  $f(x) = x^5 - 4x^3 + x^2 + 3x + 1$

**Solution:**

Given,

$$g(x) = x^3 - 3x + 1; f(x) = x^5 - 4x^3 + x^2 + 3x + 1$$

$$\begin{array}{r}
 \phantom{x^3 - 3x + 1} \overline{x^5 + 0x^4 - 4x^3 + x^2 + 3x + 1} \\
 \phantom{x^3 - 3x + 1} \underline{x^5 + 0x^4 - 3x^3 + x^2} \phantom{+ 3x + 1} \\
 \phantom{x^3 - 3x + 1} \phantom{x^5 +} 0x^3 + 0x^2 + 3x + 1 \\
 \phantom{x^3 - 3x + 1} \phantom{x^5 +} \underline{-x^3 + 0x^2 + 3x - 1} \\
 \phantom{x^3 - 3x + 1} \phantom{x^5 +} \phantom{0x^3 +} 2
 \end{array}$$

Since, the remainder  $r(x) = 2$  and not equal to zero we can say that the first polynomial is not a factor of the second polynomial.

(iii)  $g(x) = 2x^2 - x + 3$ ;  $f(x) = 6x^5 - x^4 + 4x^3 - 5x^2 - x - 15$

**Solution:**

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Given,

$$g(x) = 2x^2 - x + 3; f(x) = 6x^5 - x^4 + 4x^3 - 5x^2 - x - 15$$

$$\begin{array}{r}
 3x^3 + x^2 - 2x - 5 \\
 2x^2 - x + 3 \overline{) 6x^5 - x^4 + 4x^3 - 5x^2 - x - 15} \\
 \underline{6x^5 - 3x^4 + 9x^3} \phantom{- 5x^2 - x - 15} \\
 2x^4 - 5x^3 - 5x^2 - x - 15 \\
 \underline{2x^4 - x^3 + 3x^2} \phantom{- x - 15} \\
 -4x^3 - 8x^2 - x - 15 \\
 \underline{-4x^3 + 2x^2 - 6x} \phantom{- 15} \\
 -10x^2 + 5x - 15 \\
 \underline{-10x^2 + 5x - 15} \\
 0
 \end{array}$$

Since, the remainder  $r(x) = 0$  we can say that the first polynomial is not a factor of the second polynomial.

**3. Obtain all zeroes of the polynomial  $f(x) = 2x^4 + x^3 - 14x^2 - 19x - 6$ , if two of its zeroes are -2 and -1.**  
**Solution:**

Given,

$$f(x) = 2x^4 + x^3 - 14x^2 - 19x - 6$$

If the two zeros of the polynomial are -2 and -1, then its factors are  $(x + 2)$  and  $(x + 1)$

$$\Rightarrow (x+2)(x+1) = x^2 + x + 2x + 2 = x^2 + 3x + 2 \dots\dots (i)$$

This means that (i) is a factor of  $f(x)$ . So, performing division algorithm we get,

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$$\begin{array}{r}
 x^2 + 3x + 2 \quad \overline{) \begin{array}{r} 2x^4 - 5x^3 - 14x^2 - 19x - 6 \\ 2x^4 + 6x^3 + 4x^2 \\ \hline -5x^3 - 18x^2 - 19x - 6 \\ -5x^3 - 15x^2 - 10x \\ \hline -3x^2 - 9x - 6 \\ -3x^2 - 9x - 6 \\ \hline 0 \end{array}} \\
 \hline
 \end{array}$$

The quotient is  $2x^2 - 5x - 3$ .

$$\Rightarrow f(x) = (2x^2 - 5x - 3)(x^2 + 3x + 2)$$

For obtaining the other 2 zeros of the polynomial

We put,

$$2x^2 - 5x - 3 = 0$$

$$\Rightarrow (2x + 1)(x - 3) = 0$$

$$\therefore x = -1/2 \text{ or } 3$$

Hence, all the zeros of the polynomial are -2, -1, -1/2 and 3.

**4. Obtain all zeroes of  $f(x) = x^3 + 13x^2 + 32x + 20$ , if one of its zeros is -2.**

**Solution:**

Given,

$$f(x) = x^3 + 13x^2 + 32x + 20$$

And, -2 is one of the zeros. So,  $(x + 2)$  is a factor of  $f(x)$ ,

Performing division algorithm, we get



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$$\begin{array}{r}
 x^2 + 11x + 10 \\
 x + 2 \overline{) x^3 + 13x^2 + 32x + 20} \\
 \underline{-(x^3 + 2x^2)} \phantom{+ 20} \\
 11x^2 + 32x + 20 \\
 \underline{-(11x^2 + 22x)} \phantom{+ 20} \\
 10x + 20 \\
 \underline{-(10x + 20)} \\
 0
 \end{array}$$

$$\Rightarrow f(x) = (x^2 + 11x + 10)(x + 2)$$

So, putting  $x^2 + 11x + 10 = 0$  we can get the other 2 zeros.

$$\Rightarrow (x + 10)(x + 1) = 0$$

$$\therefore x = -10 \text{ or } -1$$

Hence, all the zeros of the polynomial are -10, -2 and -1.

**5. Obtain all zeroes of the polynomial  $f(x) = x^4 - 3x^3 - x^2 + 9x - 6$ , if the two of its zeroes are  $-\sqrt{3}$  and  $\sqrt{3}$ .**

**Solution:**

Given,

$$f(x) = x^4 - 3x^3 - x^2 + 9x - 6$$

Since, two of the zeroes of polynomial are  $-\sqrt{3}$  and  $\sqrt{3}$  so,  $(x + \sqrt{3})$  and  $(x - \sqrt{3})$  are factors of  $f(x)$ .

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$\Rightarrow x^2 - 3$  is a factor of  $f(x)$ . Hence, performing division algorithm, we get

$$\begin{array}{r}
 x^2 - 3x + 2 \\
 x^2 - 3 \overline{) x^4 - 3x^3 - x^2 + 9x - 6} \\
 \underline{-(x^4 - 3x^3 + 2x^2 + 9x - 6)} \\
 -3x^3 + 0x^2 + 9x - 6 \\
 \underline{-(3x^3 + 0x^2 + 9x - 6)} \\
 0
 \end{array}$$

$$\Rightarrow f(x) = (x^2 - 3x + 2)(x^2 - 3)$$

So, putting  $x^2 - 3x + 2 = 0$  we can get the other 2 zeros.

$$\Rightarrow (x - 2)(x - 1) = 0$$

$$\therefore x = 2 \text{ or } 1$$

Hence, all the zeros of the polynomial are  $-\sqrt{3}$ ,  $1$ ,  $\sqrt{3}$  and  $2$ .

**6. Obtain all zeroes of the polynomial  $f(x) = 2x^4 - 2x^3 - 7x^2 + 3x + 6$ , if the two of its zeroes are  $-\sqrt{3/2}$  and  $\sqrt{3/2}$ .**

**Solution:**

Given,

$$f(x) = 2x^4 - 2x^3 - 7x^2 + 3x + 6$$

Since, two of the zeroes of polynomial are  $-\sqrt{3/2}$  and  $\sqrt{3/2}$  so,  $(x + \sqrt{3/2})$  and  $(x - \sqrt{3/2})$  are factors of  $f(x)$ .

$\Rightarrow x^2 - (3/2)$  is a factor of  $f(x)$ . Hence, performing division algorithm, we get

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$$\begin{array}{r}
 x^2 - \frac{3}{2} \quad \overline{) 2x^4 - 2x^3 - 7x^2 + 3x + 6} \\
 \underline{2x^4 - 2x^3 - 3x^2} \phantom{+ 6} \\
 -4x^2 + 3x + 6 \\
 \underline{-4x^2 + 0x + 6} \\
 0
 \end{array}$$

$$\Rightarrow f(x) = (2x^2 - 2x - 4)(x^2 - 3/2) = 2(x^2 - x - 2)(x^2 - 3/2)$$

So, putting  $x^2 - x - 2 = 0$  we can get the other 2 zeros.

$$\Rightarrow (x - 2)(x + 1) = 0$$

$$\therefore x = 2 \text{ or } -1$$

Hence, all the zeros of the polynomial are  $-\sqrt{3/2}$ ,  $-1$ ,  $\sqrt{3/2}$  and  $2$ .

7. Find all the zeroes of the polynomial  $x^4 + x^3 - 34x^2 - 4x + 120$ , if the two of its zeros are  $2$  and  $-2$ .

**Solution:**

Let,

$$f(x) = x^4 + x^3 - 34x^2 - 4x + 120$$

Since, two of the zeroes of polynomial are  $-2$  and  $2$  so,  $(x + 2)$  and  $(x - 2)$  are factors of  $f(x)$ .

$\Rightarrow x^2 - 4$  is a factor of  $f(x)$ . Hence, performing division algorithm, we get

$$\begin{array}{r}
 x^2 - 4 \quad \overline{) x^4 + x^3 - 34x^2 - 4x + 120} \\
 \underline{x^4 + x^3 - 4x^2} \phantom{- 4x + 120} \\
 -30x^2 - 4x + 120 \\
 \underline{-30x^2 + 0x + 120} \\
 0
 \end{array}$$

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$$\Rightarrow f(x) = (x^2 + x - 30)(x^2 - 4)$$

So, putting  $x^2 + x - 30 = 0$  we can get the other 2 zeros.

$$\Rightarrow (x - 6)(x + 5) = 0$$

$$\therefore x = 6 \text{ or } -5$$

Hence, all the zeros of the polynomial are -5, -2, 2 and 6.